

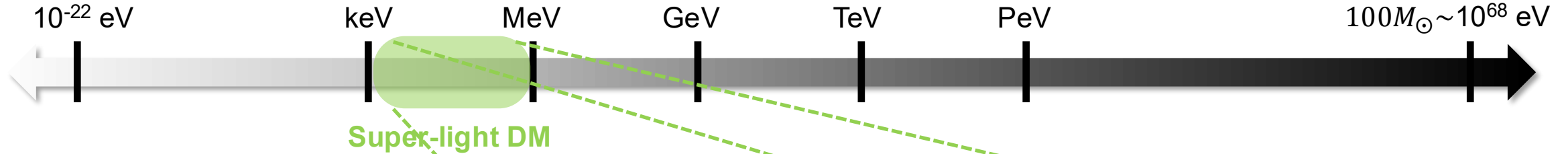
Calibration of Graphene-based Josephson Junction Detector for Dark Matter Search

Seunghan Lee

Dept. of Physics, POSTECH, Korea



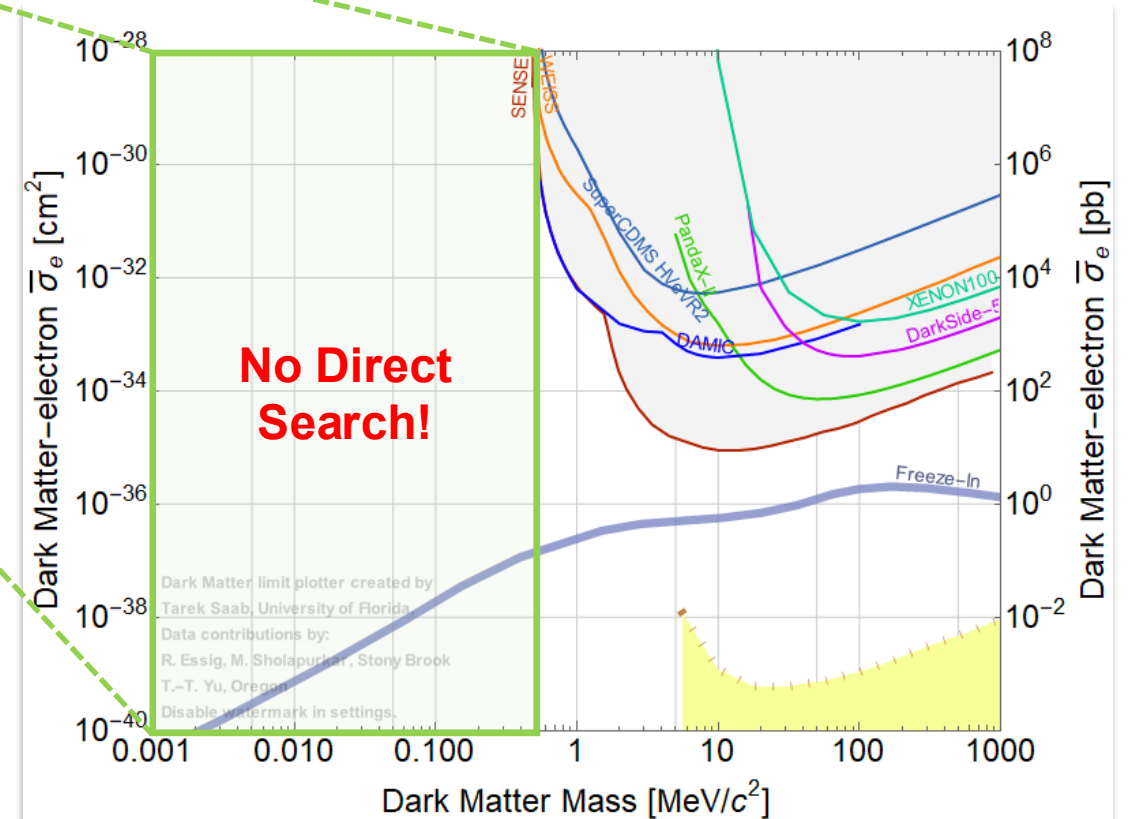
Necessity of a sensitive Detector for Dark Matter Search



❖ $E_k \sim mv^2 \sim \mathbf{O(meV)}$ with $m \sim \text{keV}$ & $v \sim 10^{-3}c$

❖ **New approaches** are required!

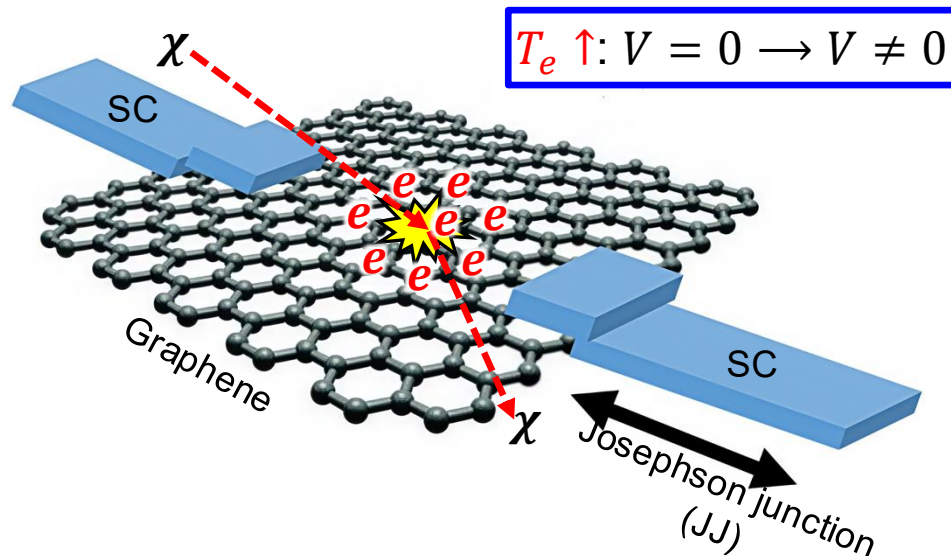
- ✓ KID [arXiv:2403.19739 (2024)]
- ✓ SNSPD [PRL (2025)]
- ✓ TES [arXiv:2506.18982 (2025)]
- ✓ Superconducting Qubit [PRL (2021)]
- ✓ **Graphene Josephson Junction (GJJ)** [PRD 2025]



Our DM Search Strategy with GJJ

Graphene-based super-light invisible matter particle search

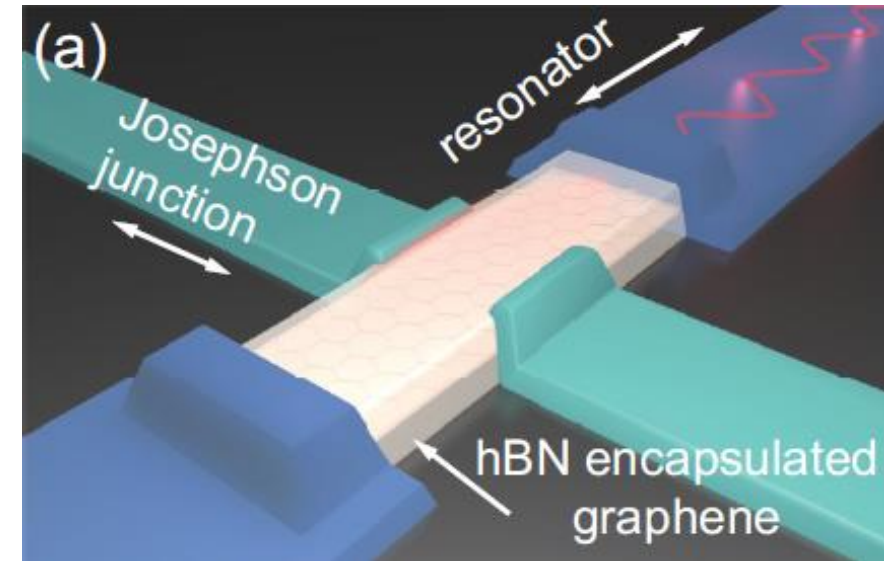
[J.C. Park](#) et al., PHYSICAL REVIEW D 112, 015002 (2025)



Super-light DM interacting with π -bond electrons

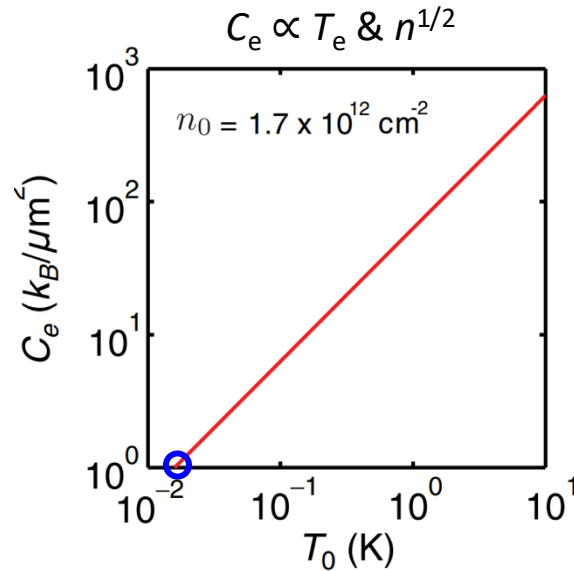
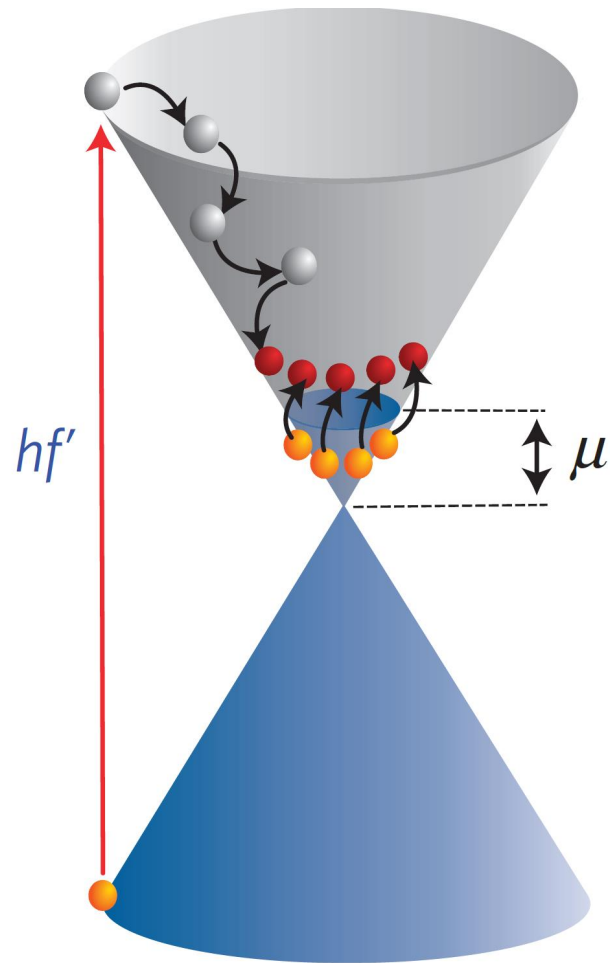
Graphene-based Josephson junction microwave bolometer

[G.-H. Lee](#) et al., Nature volume 586, pages42–46 (2020)

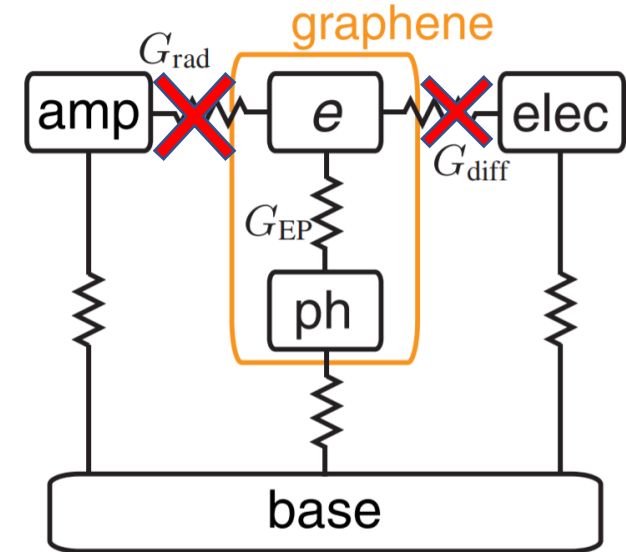
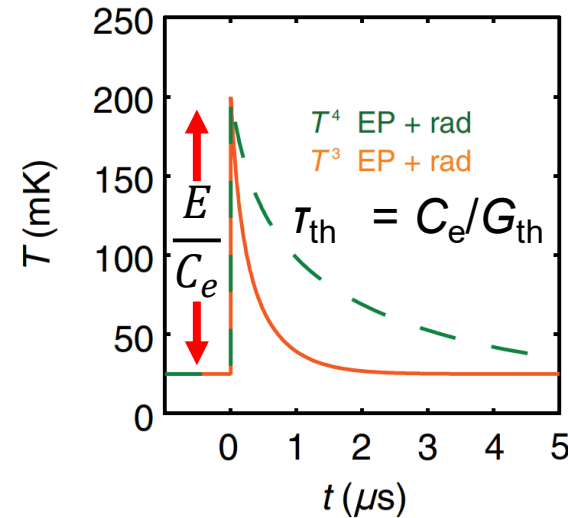


Expected $E_{\text{thres}} = 0.13 \text{ meV}$ (32 GHz)

Graphene's Advantages: Focus on Thermal Properties



PHYSICAL REVIEW APPLIED 8, 024022 (2017)



[PRX 3, 041008 (2013)]

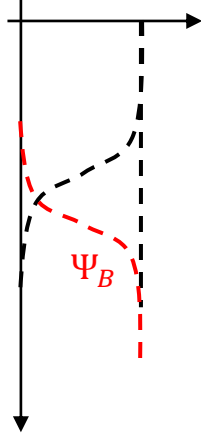
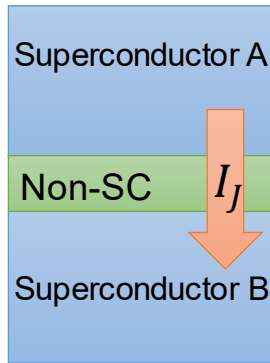
- Shrinking density of state near the CNP → **small C_e** → **Higher** temperature rise
- weak thermal interaction by electron-phonon coupling (G_{EP}) → Low cooling power

∴ **Graphene is a highly promising material for thermal sensor**

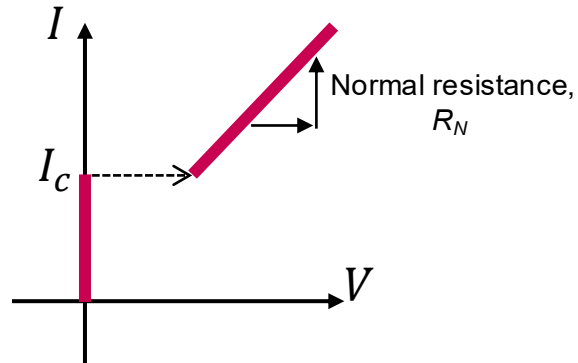
Nature Physics volume 9, pages248–252 (2013)

Graphene Josephson Junction

Josephson coupling

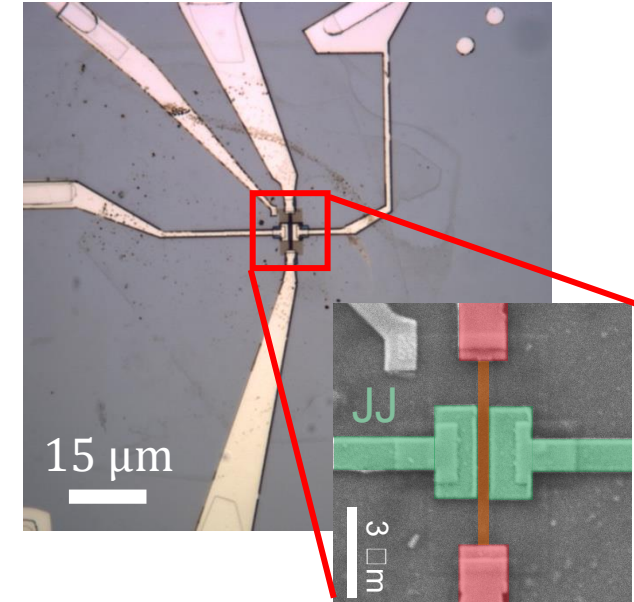
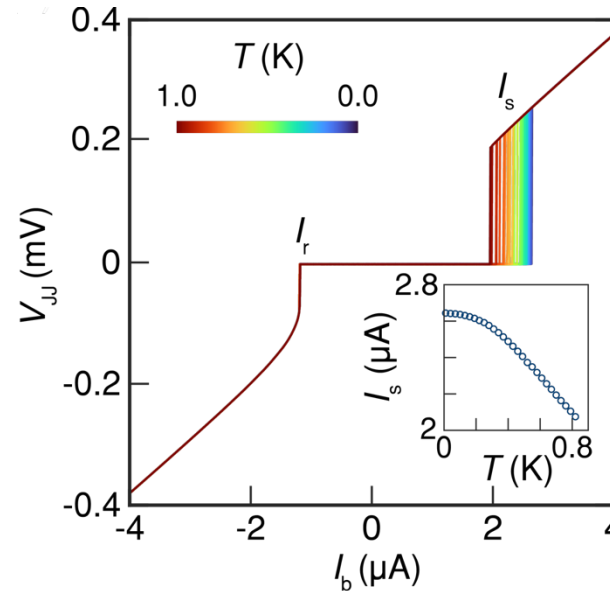


- **DC Josephson relation:** $I_J = I_c \sin \phi$
- AC Josephson relation: $\frac{d\phi}{dt} = 2eV/\hbar$



- *Phase difference: $\phi \equiv \phi_B - \phi_A$
- *critical current: I_c
- *flux quantum: $\Phi_0 = h/2e$

Graphene Josephson Junction(GJJ) critical current **Temp. Dep.**



- Switching current, $\langle I_s \rangle$, strongly depends on **electron temperature of graphene.**

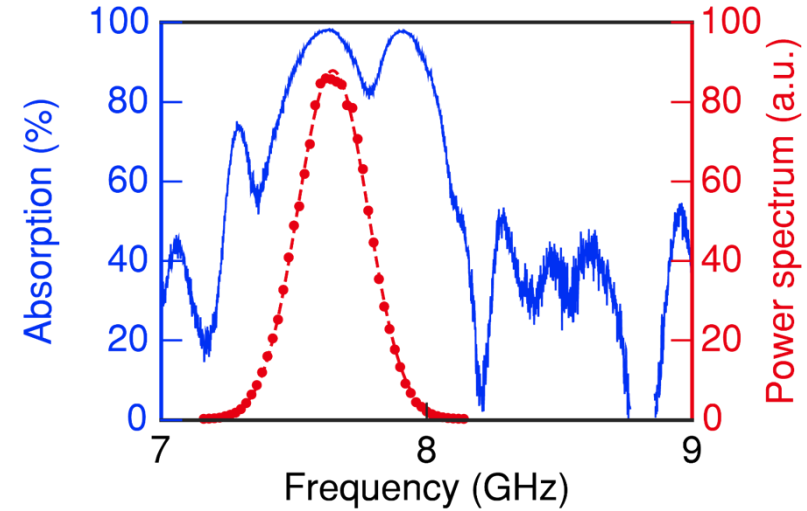
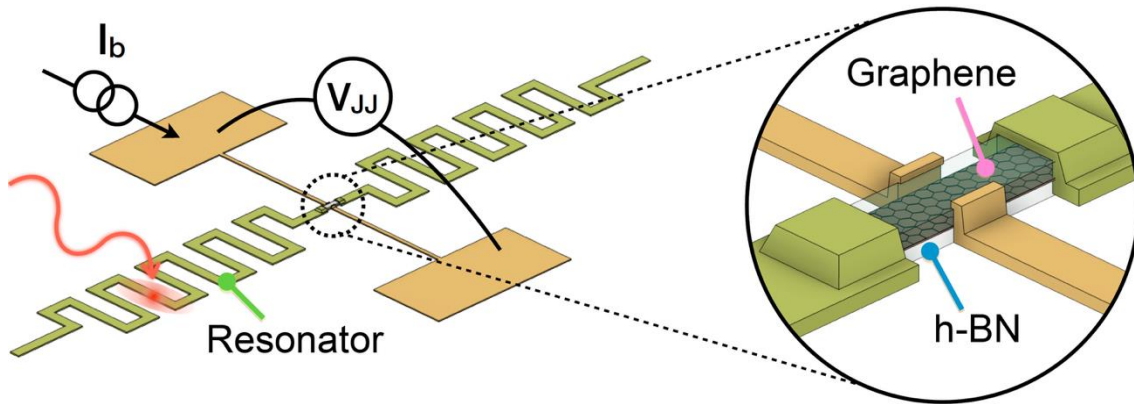
$$d\langle I_s \rangle / dT \sim -0.5 \mu\text{A/K}$$

- Switching happens very fast, **within ~10 ps.**

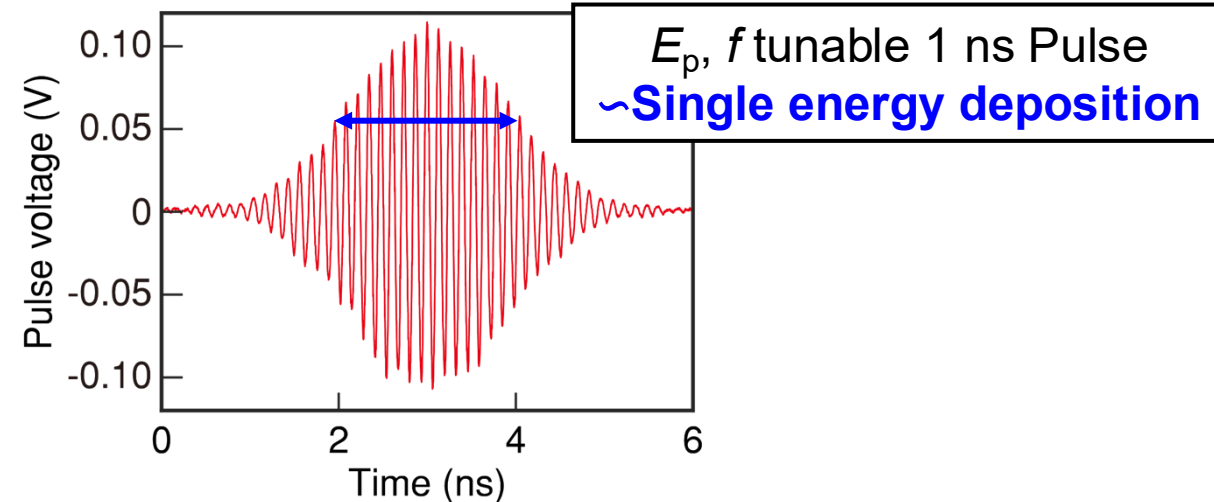
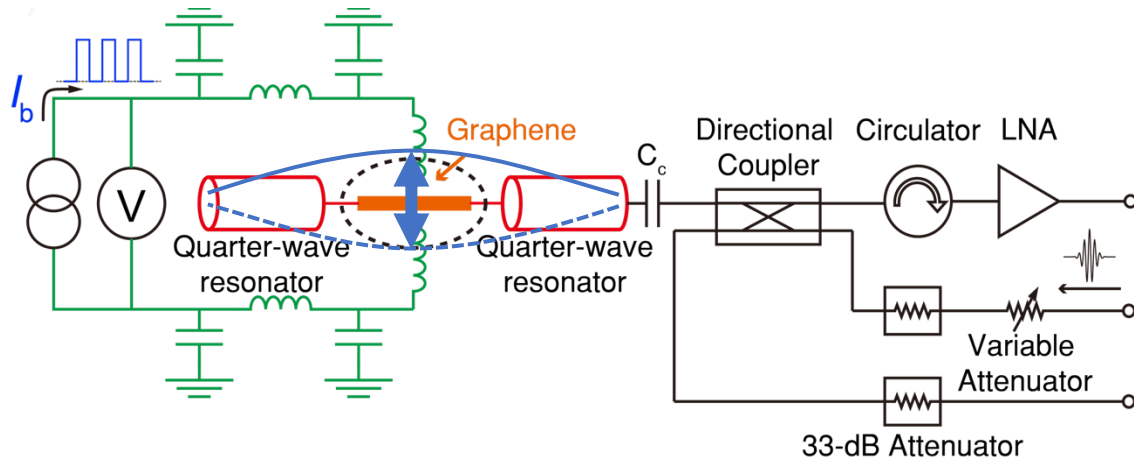
$$\omega_p \sim 100 \text{ GHz}$$

Proposal: Calibration of GJJ Detector with Microwave Pulse

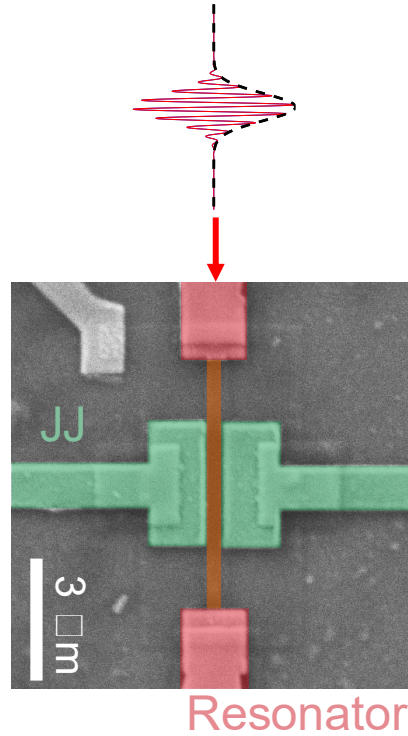
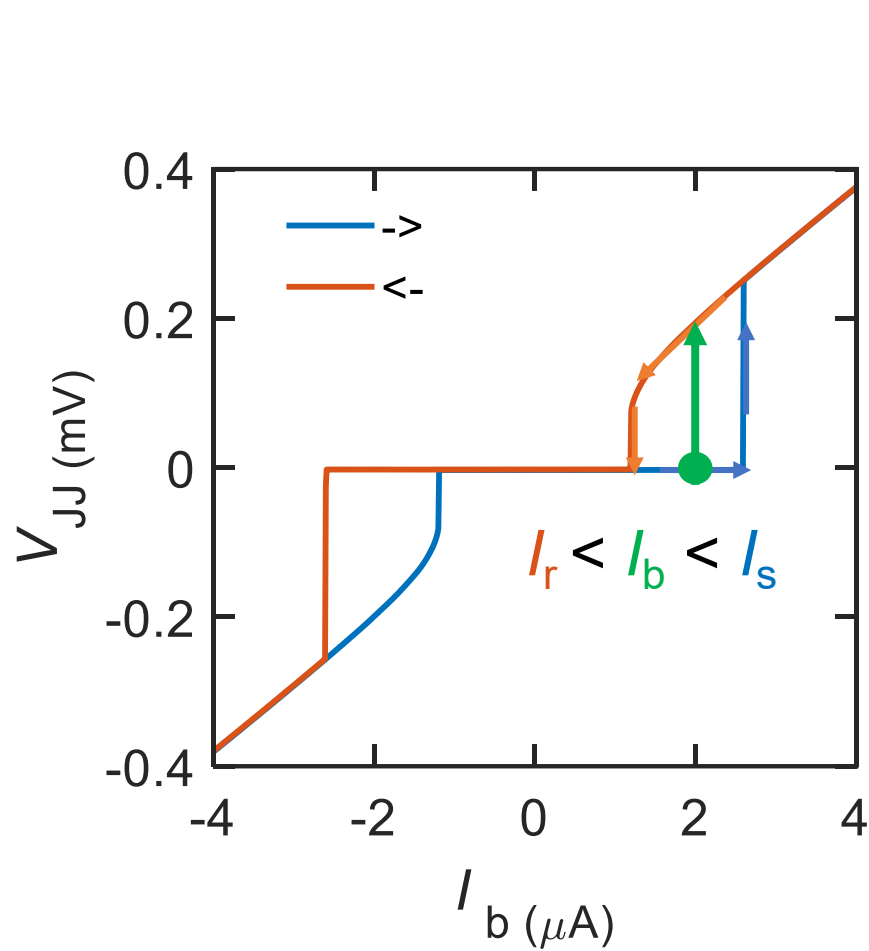
Josephson Junctions in the Age of Quantum Discovery
arXiv:2505.12724 [quant-ph]



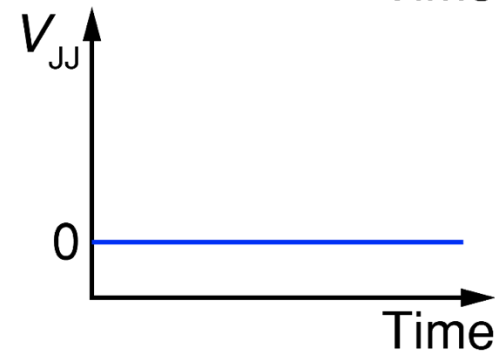
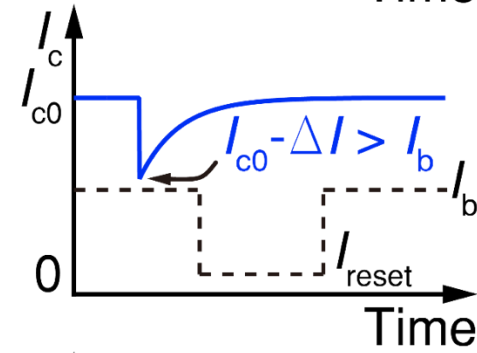
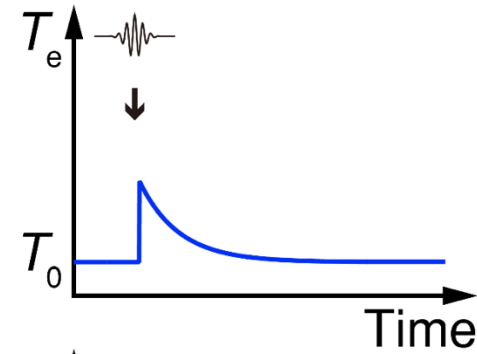
$$t_p = 2 \text{ ns} \ll \tau_{th} = C_e / G_{th} = 18.5 \text{ ns}$$



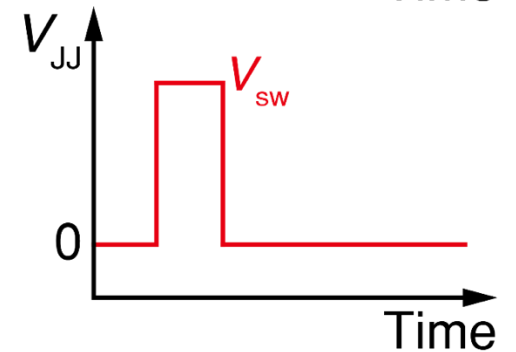
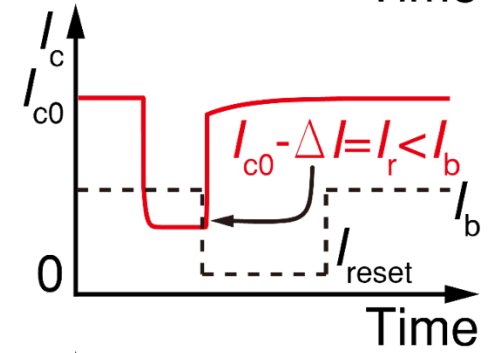
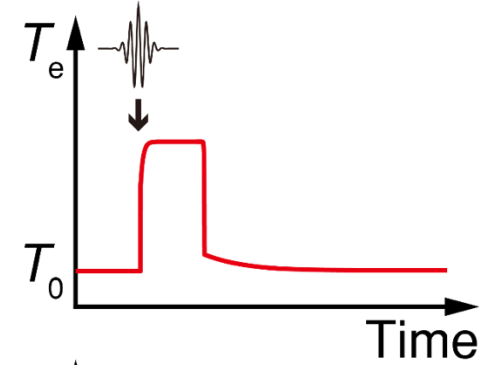
Proposal: Calibration of GJJ Detector with Microwave Pulse



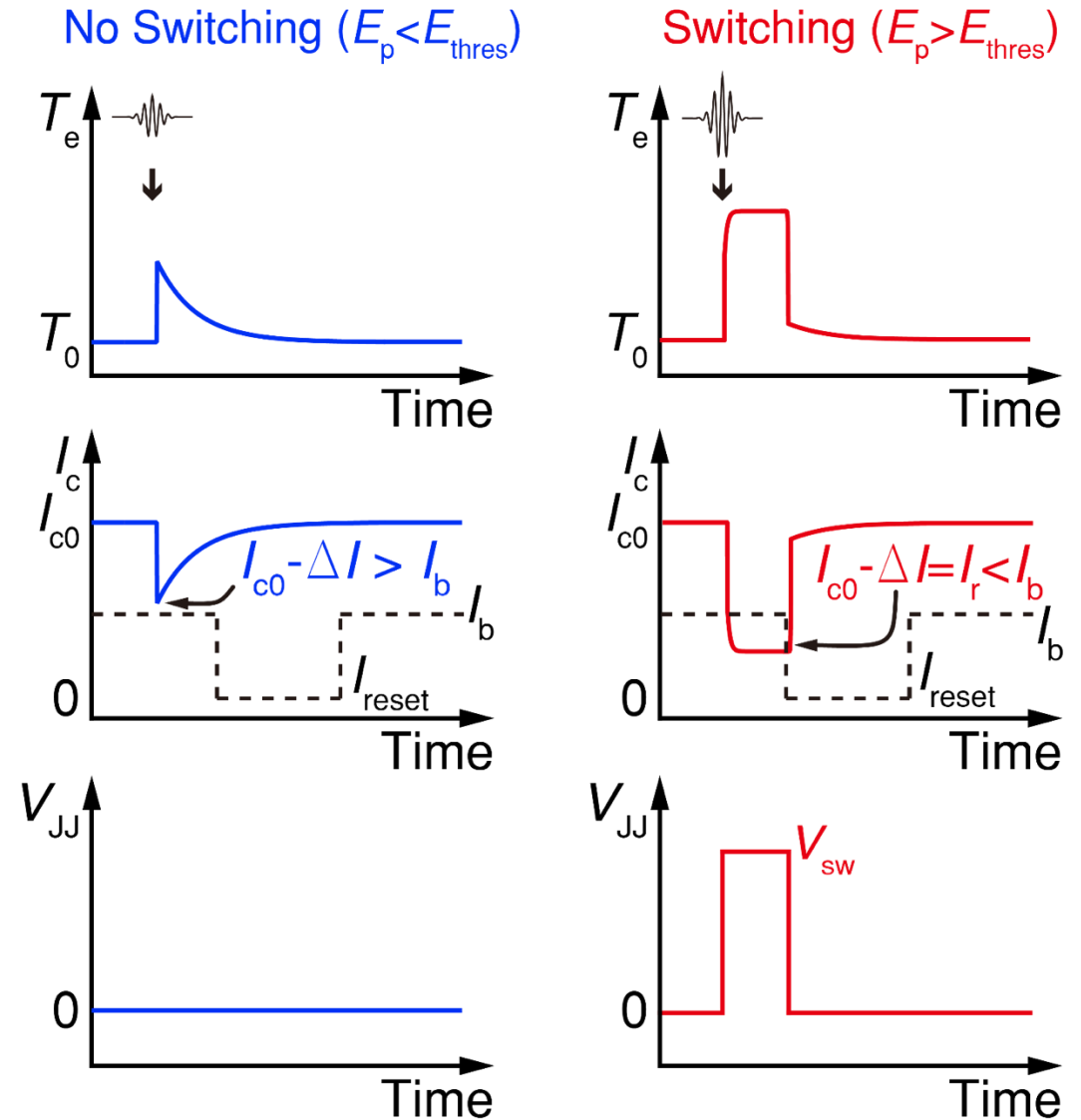
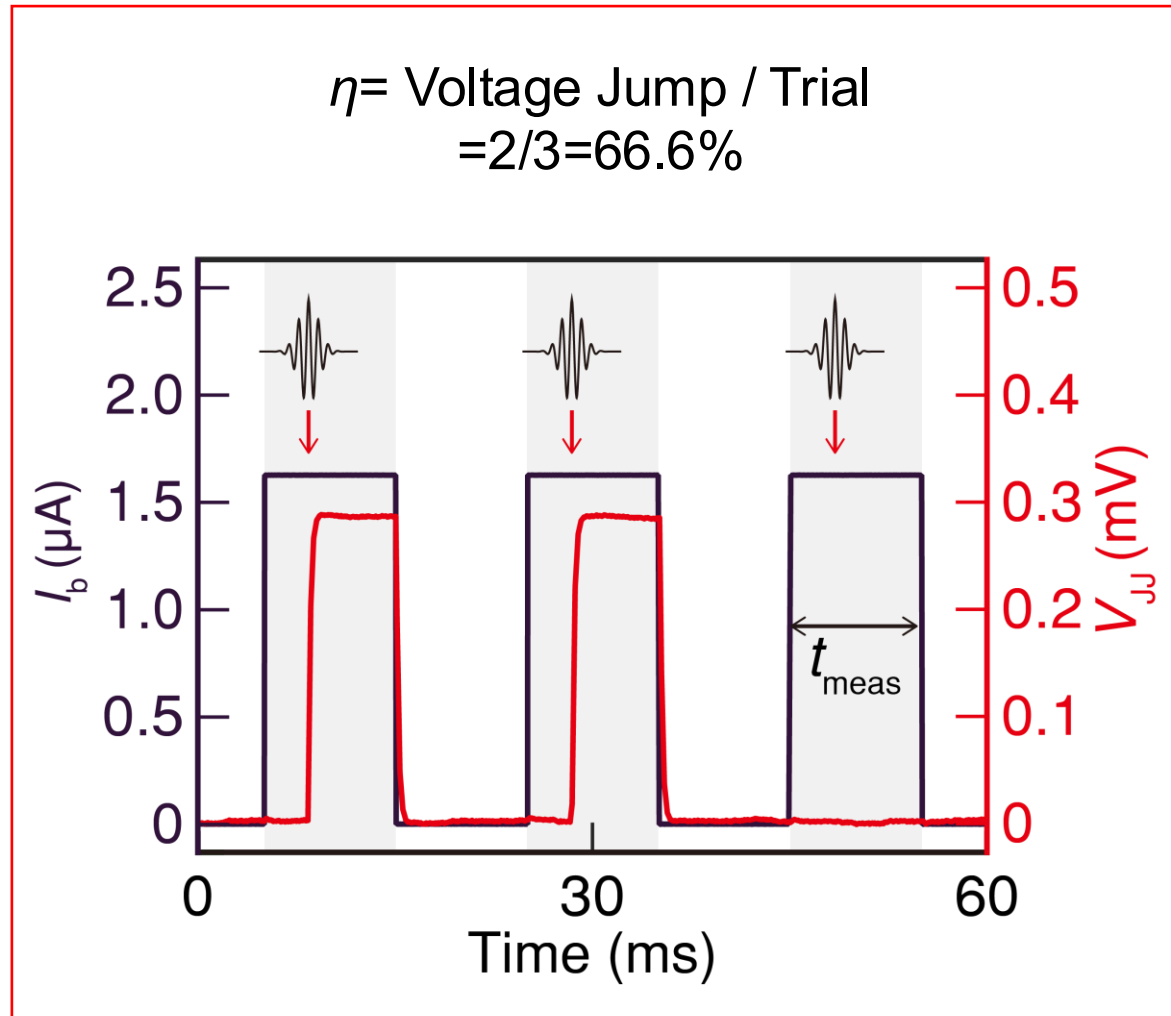
No Switching ($E_p < E_{thres}$)



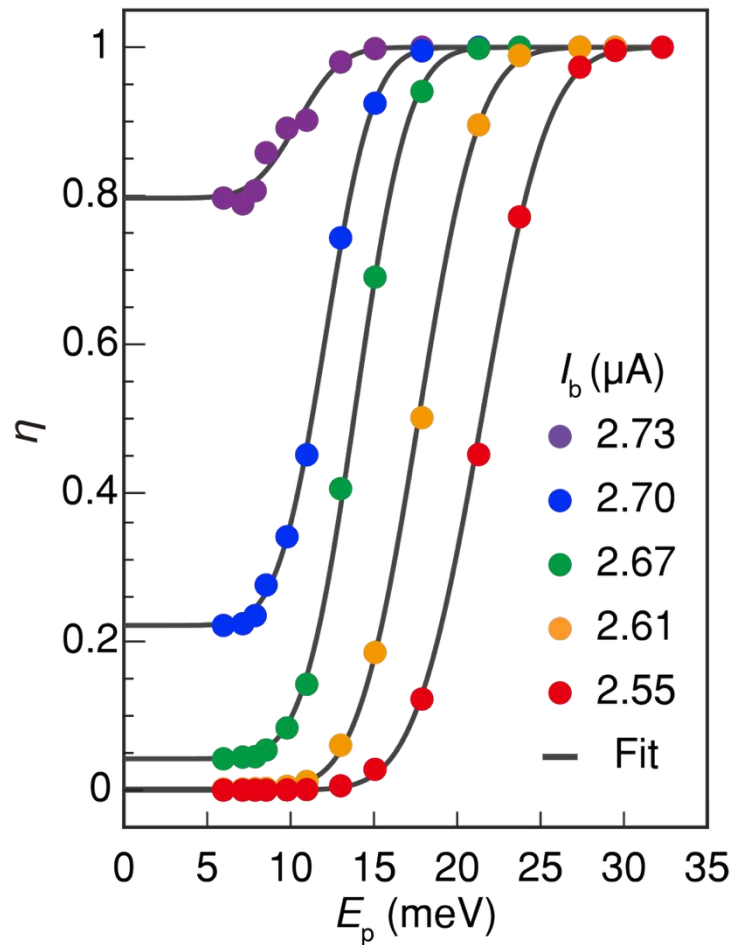
Switching ($E_p > E_{thres}$)



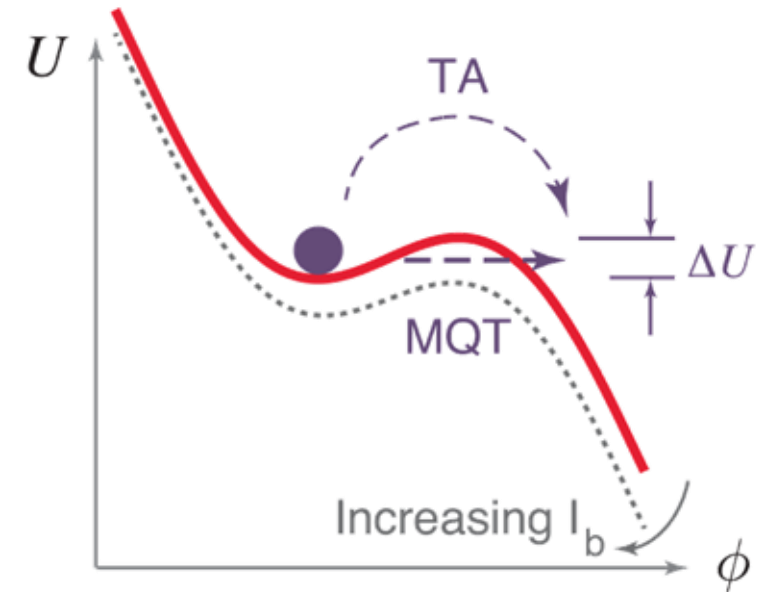
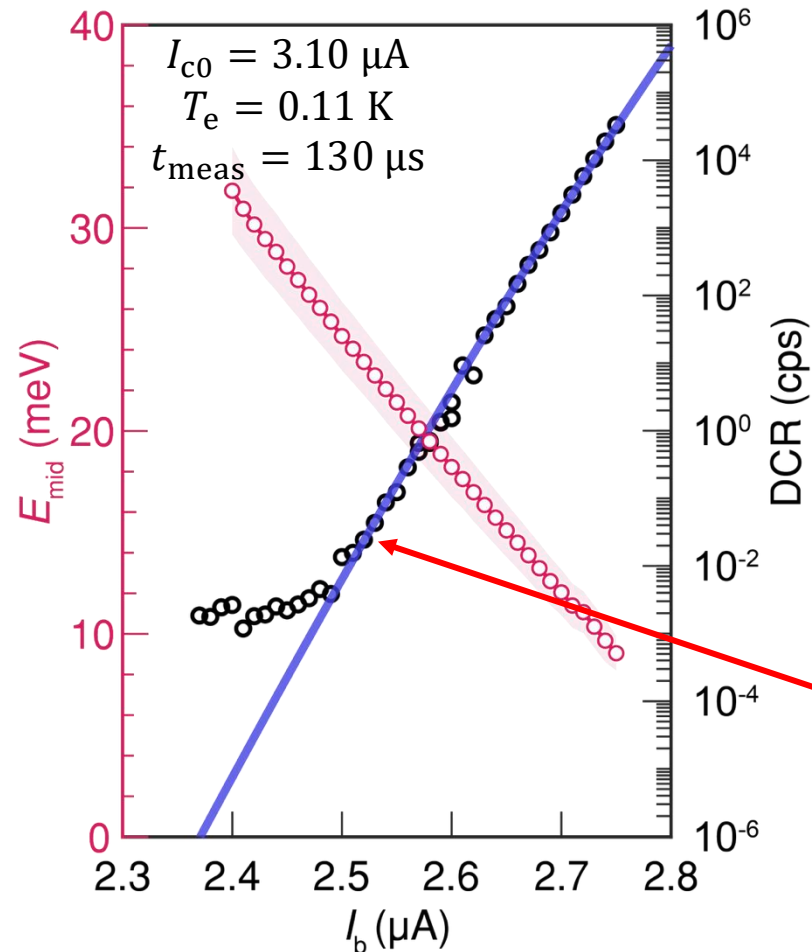
Proposal: Calibration of GJJ Detector with Microwave Pulse



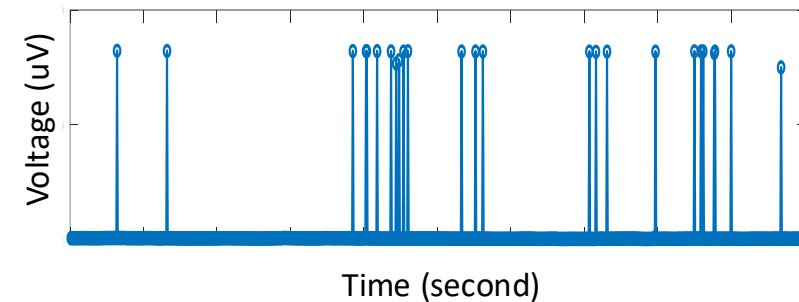
Calibration of GJJ Detector with Microwave Pulse & Dark count



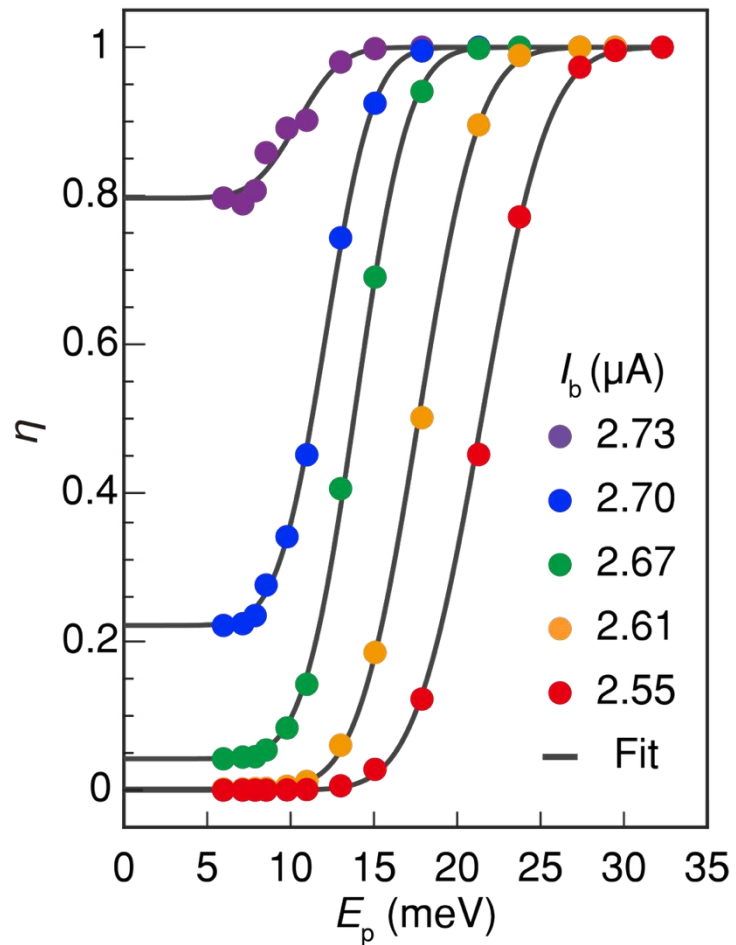
$$\eta(E_p) = \eta_{\text{floor}} + \frac{A}{2} \left[1 + \text{erf} \left(\frac{E_p - E_{\text{mid}}}{\sqrt{2}\sigma} \right) \right]$$



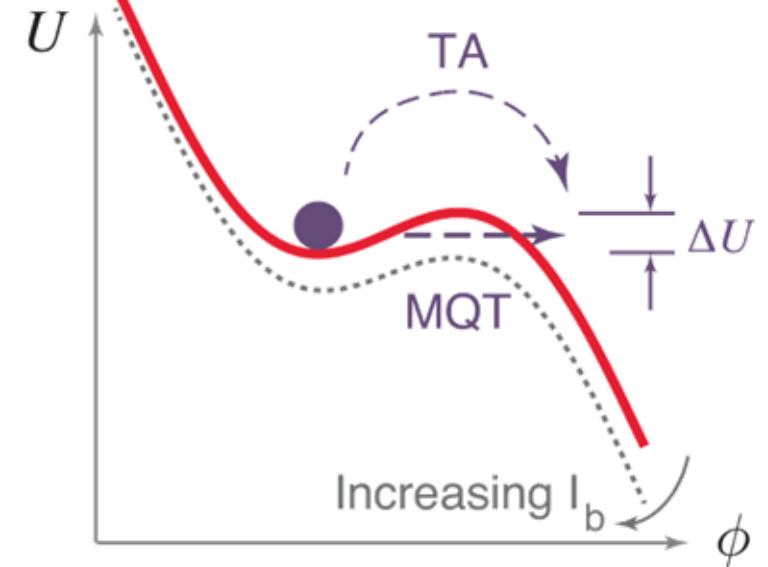
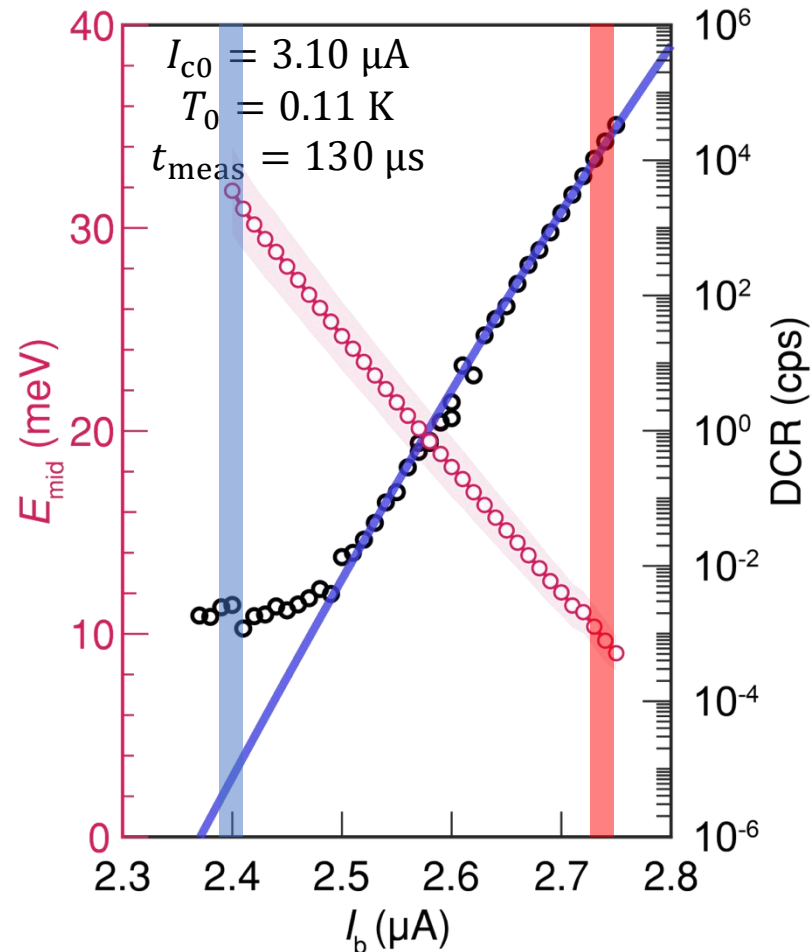
❖ Fix I_b and wait JJ switches



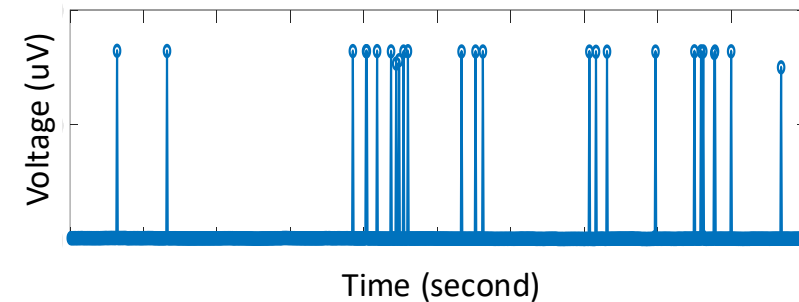
Calibration of GJJ Detector with Microwave Pulse & Dark count



$$\eta(E_p) = \eta_{\text{floor}} + \frac{A}{2} \left[1 + \text{erf} \left(\frac{E_p - E_{\text{mid}}}{\sqrt{2}\sigma} \right) \right]$$

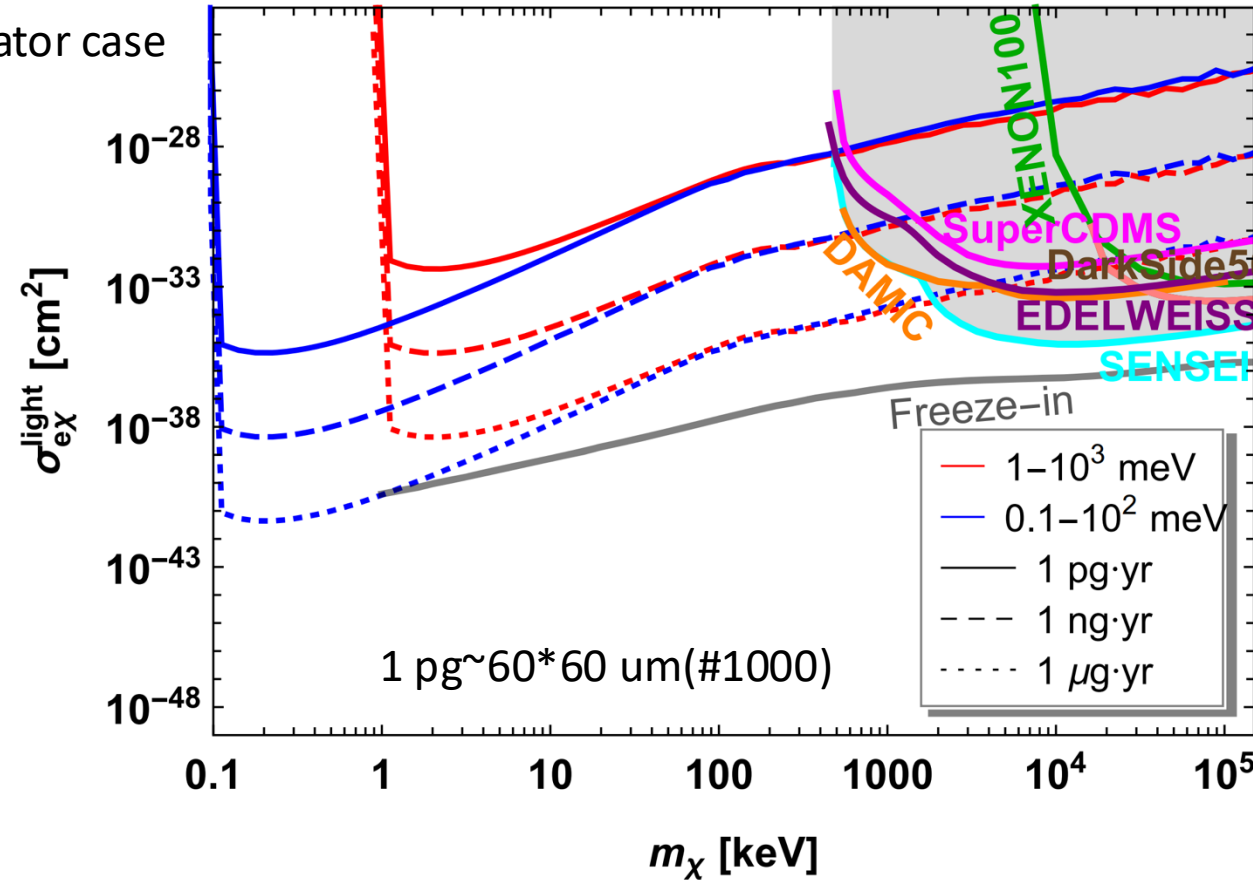


❖ Fix I_b and wait JJ switches



Path to a dark matter science run

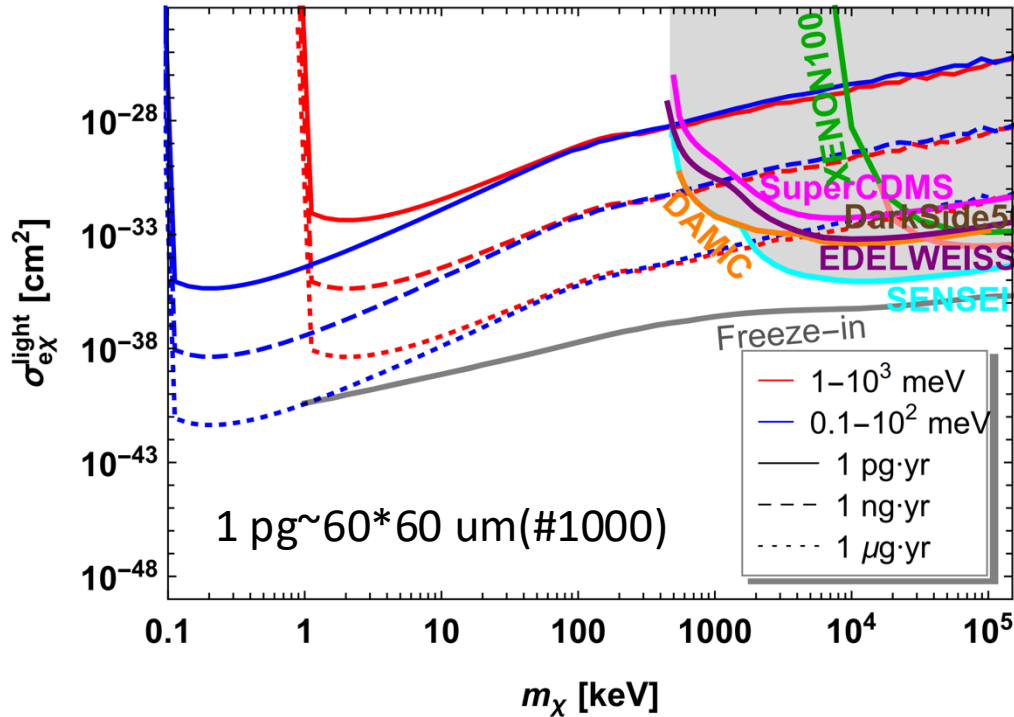
Light mediator case



2. Longer **measurement time**
3. larger-scale detector

1. Better Detector **Sensitivity**

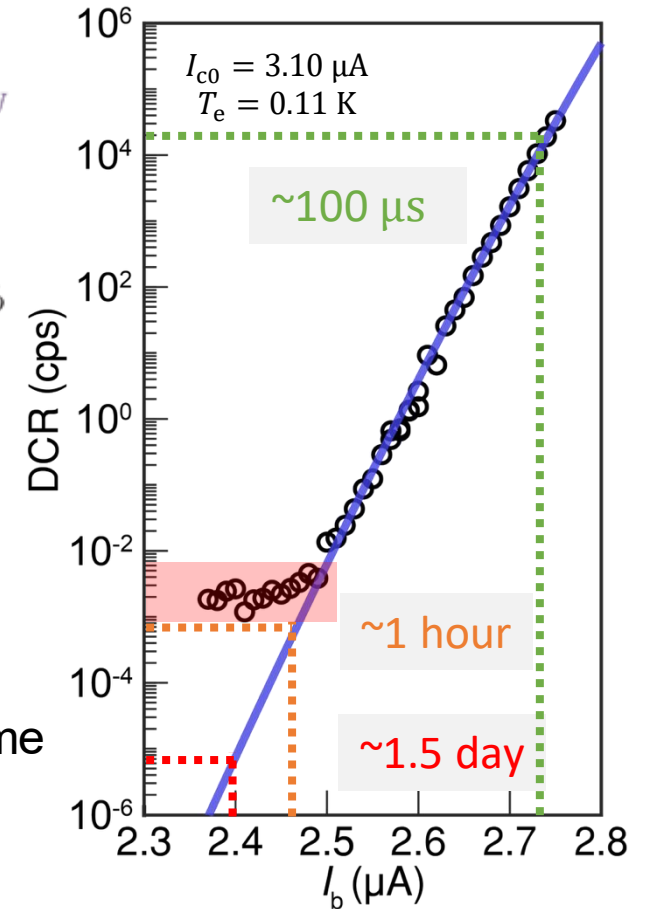
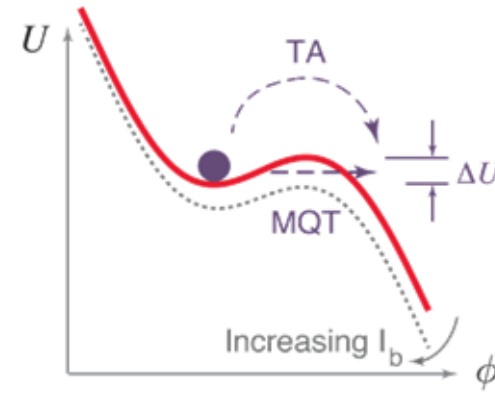
Path to a dark matter science run



1. Better Detector Sensitivity

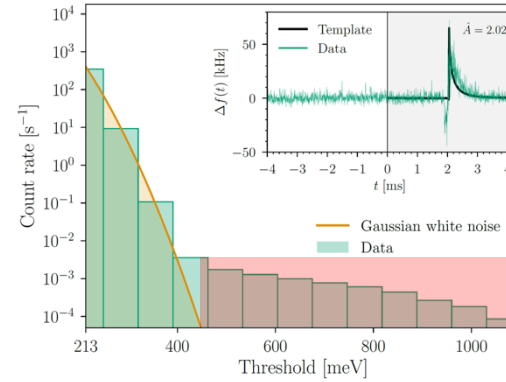
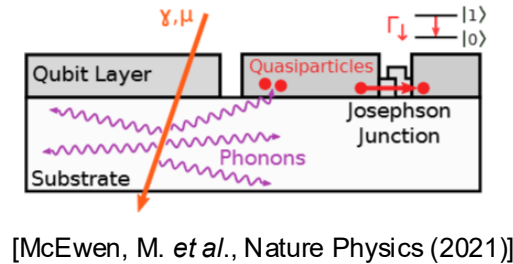
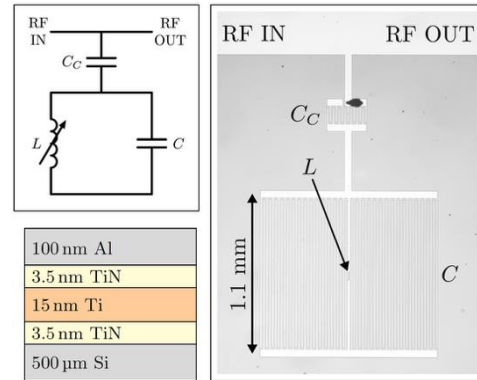
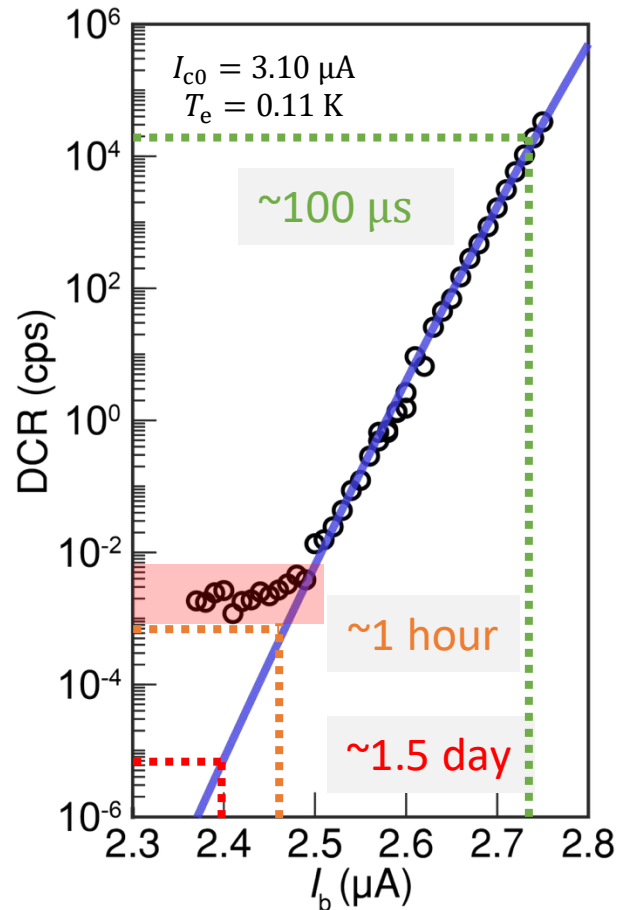
2. Longer **measurement time**
3. larger-scale detector

Limited measurement time
by **LEE**

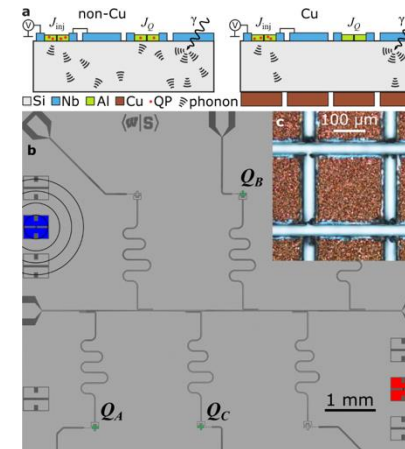


Why?

Low Energy Excess (LEE) Background



arXiv:2403.19739v1 [hep-ph]



Nature Communications
volume 13, Article number: 6425 (2022)

Cosmic rays & Chip interaction



High energy phonon



Excess Quasiparticles

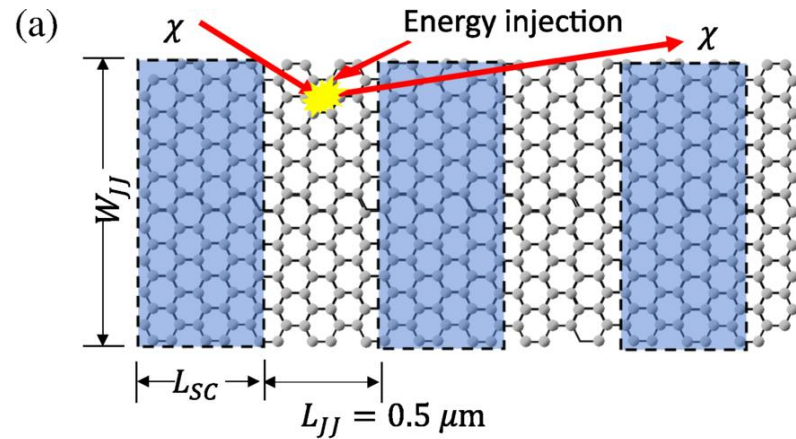


Strategy: Reducing area of SC

Why? → quasiparticles can tunnel through Josephson junctions → Decoherence/Dark count

Scaling Up: Larger-Scale Detector Arrays (# of JJ)

1 pg ~ 60*60 μm (#1000)



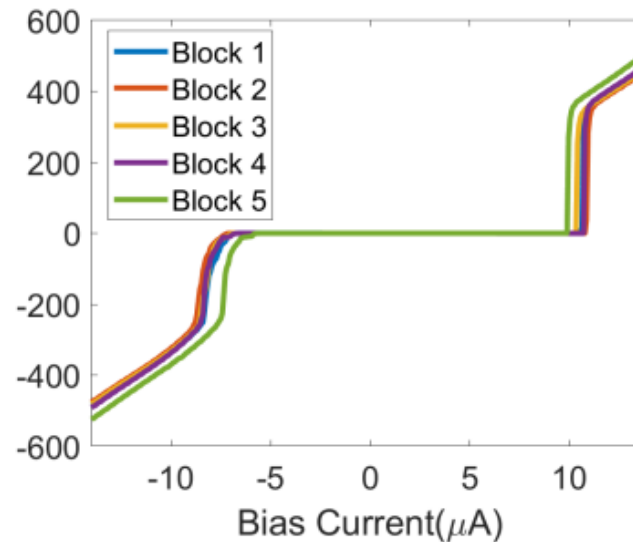
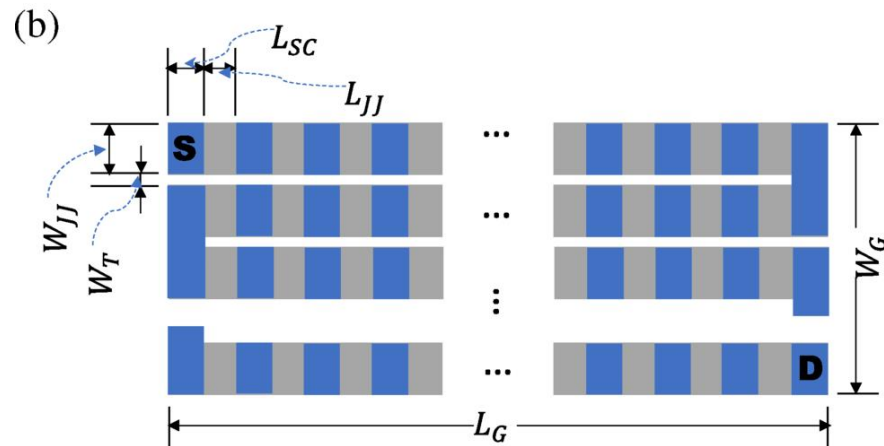
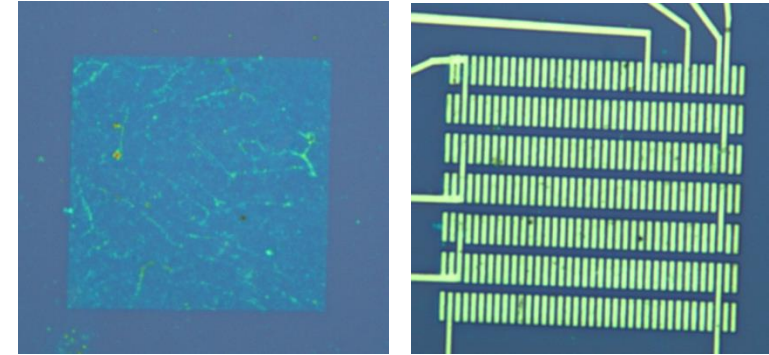
Uniform Josephson junctions in series
→ nanofabrication technology

216 GJJs connected in series

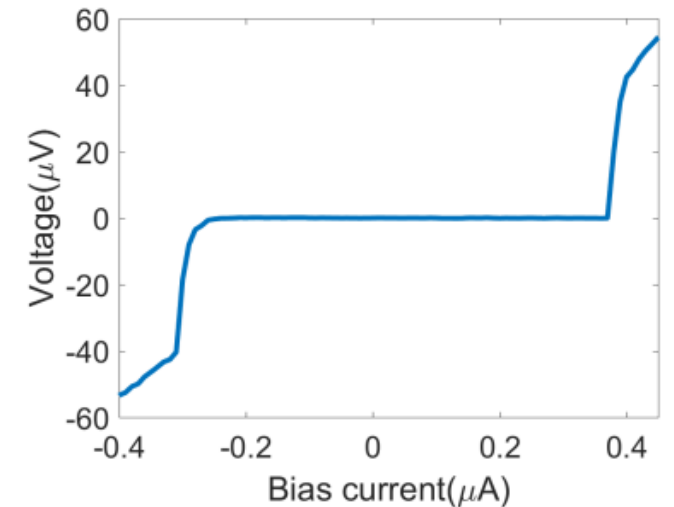


large-scale graphene sheet
→ CVD graphene

231 GJJs connected in series



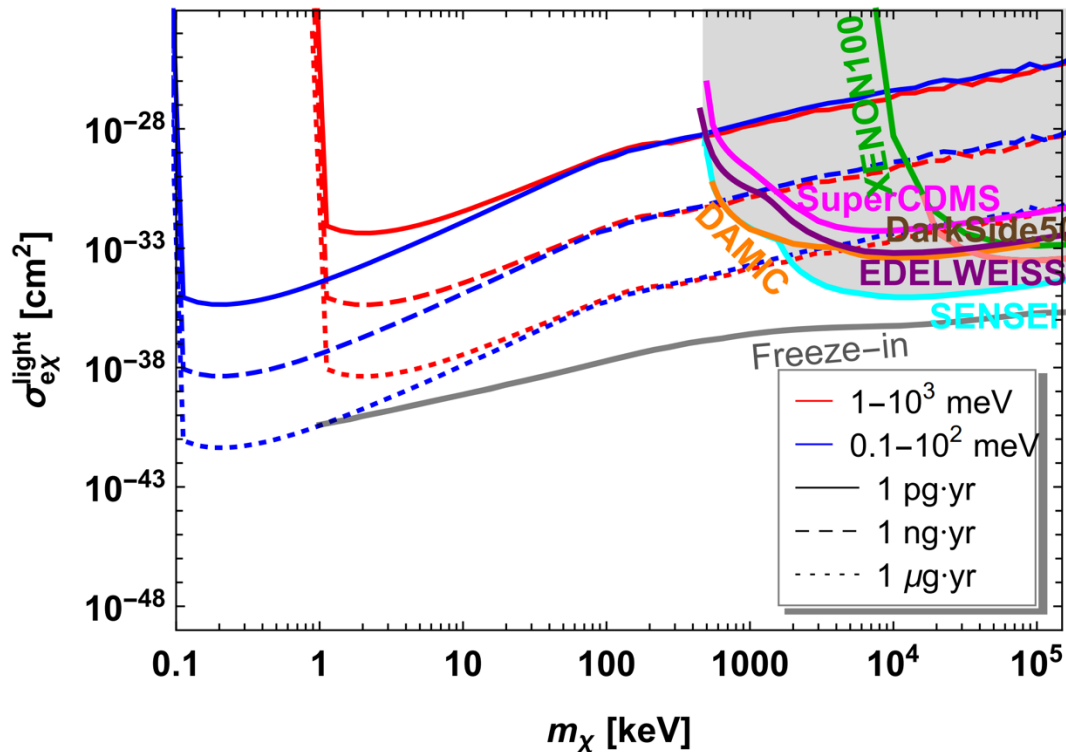
Almost same I-V curve when scaled



Conclusion

• Calibration of GJJ Detector

- ✓ $E_{\text{mid}} \doteq 9.7 \text{ meV}$ with $\text{DCR} \sim 3 \cdot 10^4 \text{ Hz}$, $E_{\text{mid}} \doteq 31 \text{ meV}$ with $\text{DCR} \sim 1 \cdot 10^{-3} \text{ Hz}$
- ✓ Thermal parameter extraction $C_e = 12.5 \pm 1.69 \text{ yJ/K}(16.1)$ & $\tau_{\text{th}} = 18.5 \text{ ns}$ & $\Sigma_{\text{ep}} = 0.81 \text{ Wm}^{-2}\text{K}^{-3}$



Path to a dark matter science run

1. Better Detector Sensitivity

- Optimization of $|dI_c/dT|$ for GJJ
- Reduce G_{EP} & C_e

2. Scaling Up: Larger-Scale Detector Arrays

- large-scale graphene sheet
- Uniform GJJ in series

3. Low energy excess background

- Reducing area of SC

Acknowledgement

POSTECH, Korea

- Seunghan Lee
- Gil-Ho Lee



- Seong Jang • Woochan Jung • Jayeon Kim • Seongeun Jeon



Northeastern University, USA

- Kin Chung Fong



Chungnam National University, Korea

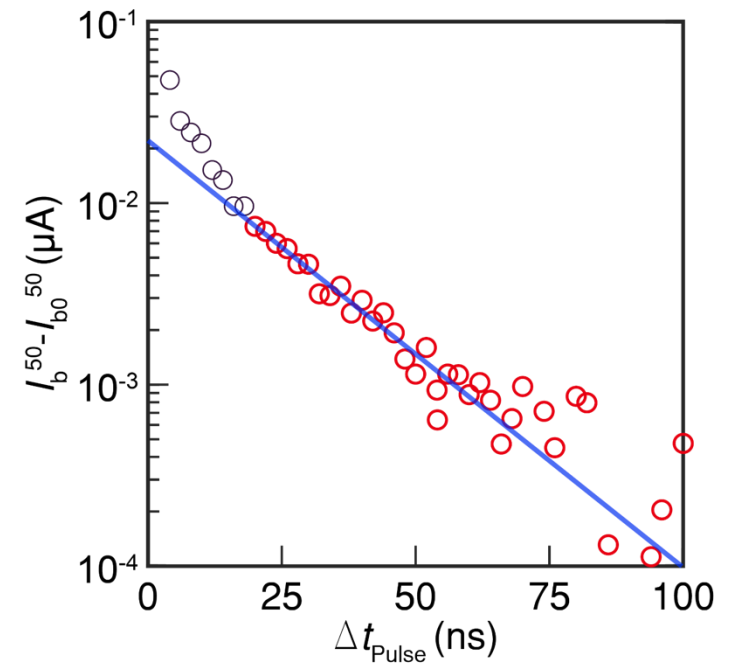
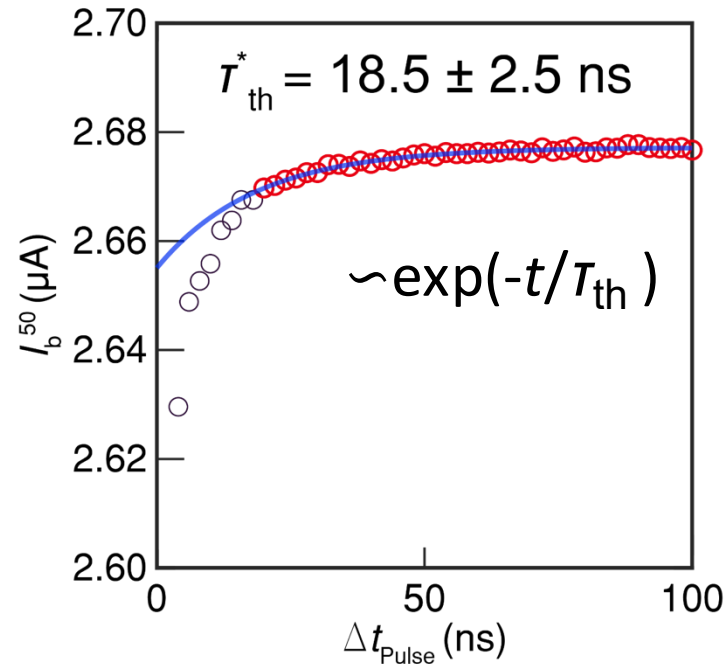
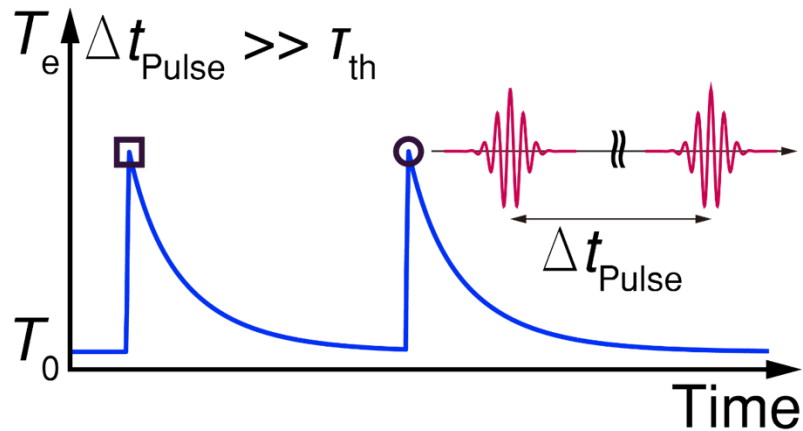
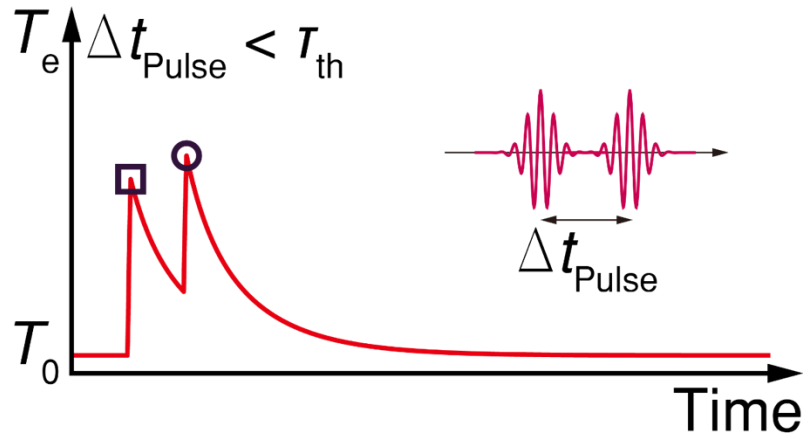
- Jong-Chul Park



Thank you!

Supple.

Thermal Relaxation Time Measurement: Time-Resolved Two Pulse Method



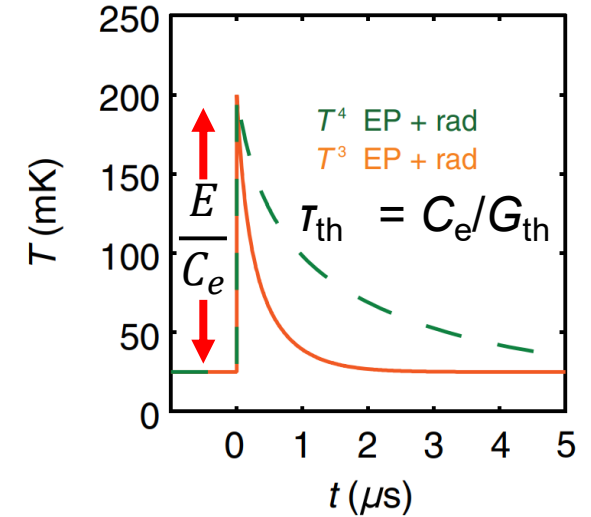
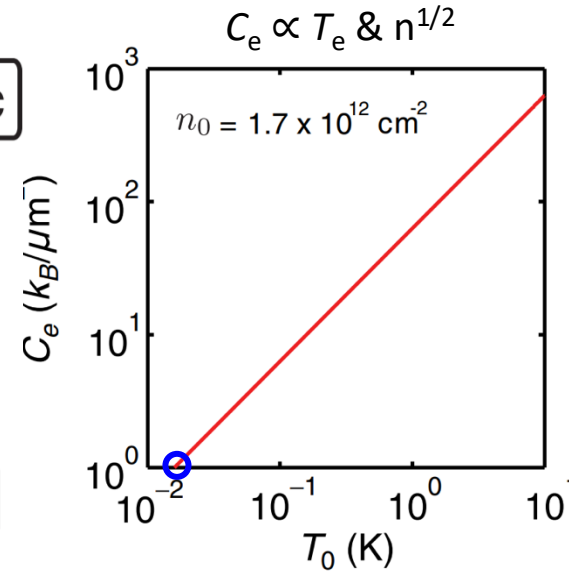
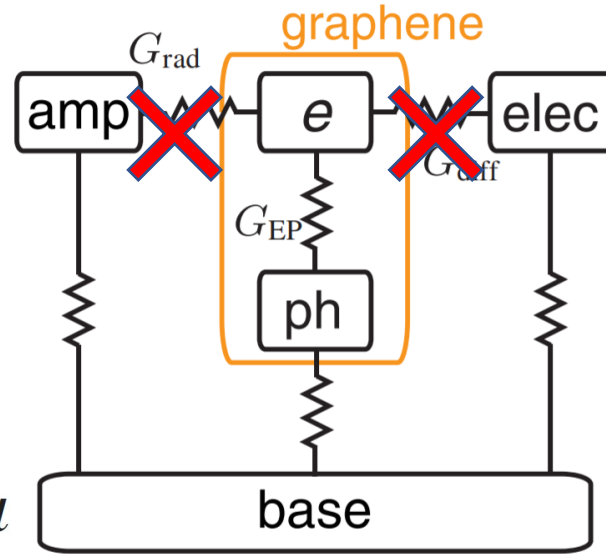
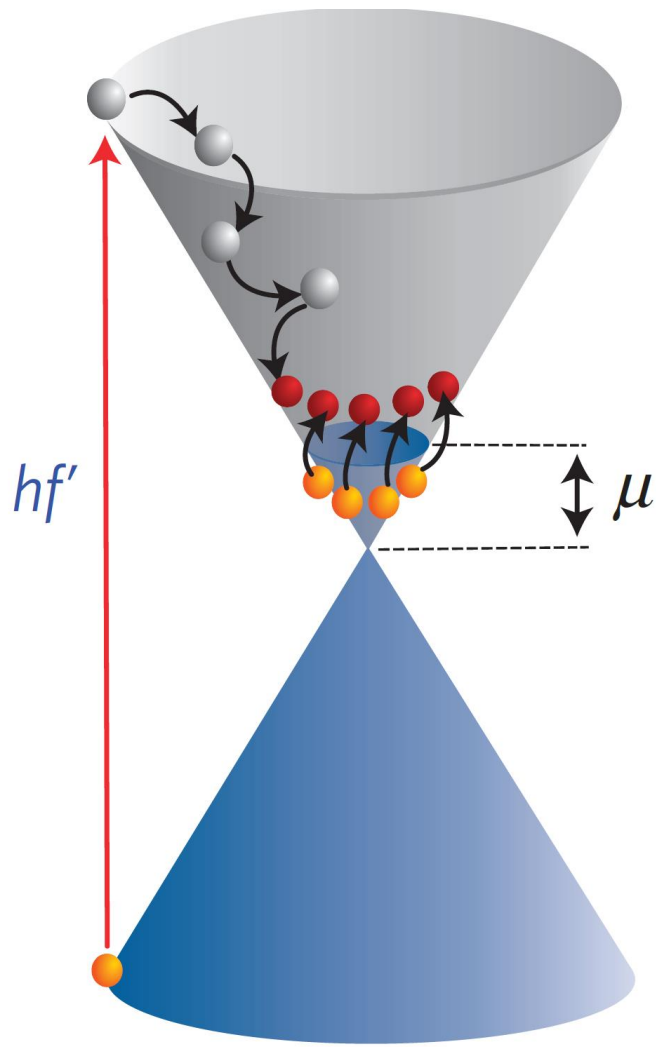
$$C_e = G_{\text{th}} * \tau_{\text{th}}$$

$$= 12.5 \pm 1.69 \text{ yJ/K} (16.1) = 0.9 \pm 0.1 k_B (1.2)$$

Measure the switching probability varying Δt
 → Estimate the **thermal relaxation time**

Graphene's Advantages: Focus on Thermal Properties

PHYSICAL REVIEW APPLIED 8, 024022 (2017)



- Linear Dispersion Relation → Broad absorption bandwidth
- Fast electron–electron interaction time (~10 fs)

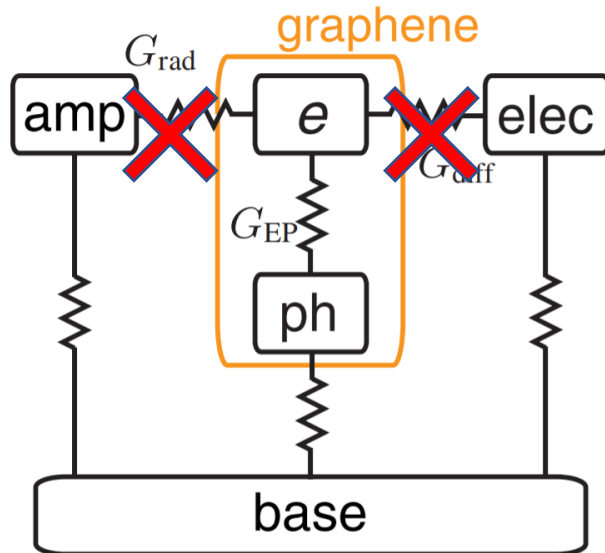
[Nat.Phys. 9, 248 (2013)]

- Shrinking density of state near the CNP
- small C_e → **Higher** temperature rise & **Faster** cooldown
- graphene enables good SC contacts

[PRX 3, 041008 (2013)]

Graphene's Advantages: Focus on Thermal Properties

PHYSICAL REVIEW APPLIED 8, 024022 (2017)



G_{ep}

The thermal interaction by electron-phonon coupling

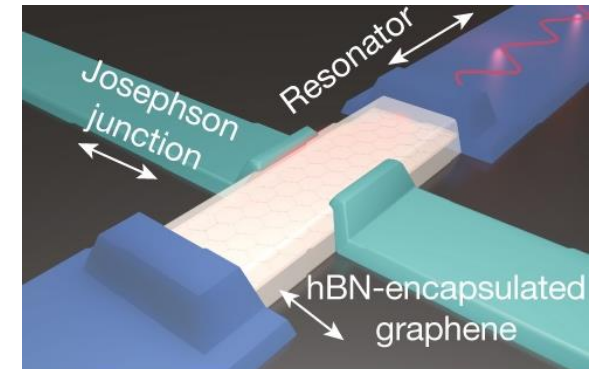
$$G_{rad} \cong r_0 k_B B, \text{ for } B < k_B T / h$$

very small

G_{diff}

Andreev reflection suppress the thermal diffusion at the superconductor to graphene contact.

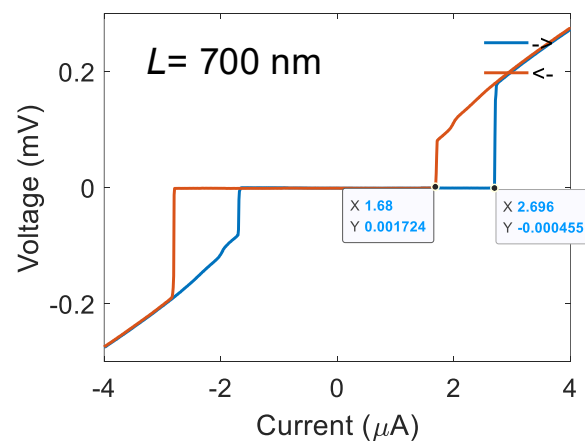
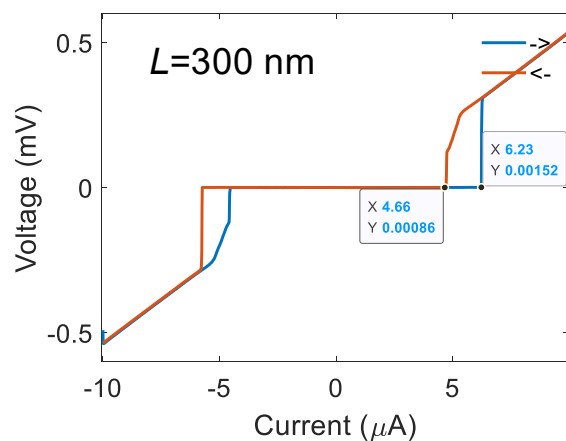
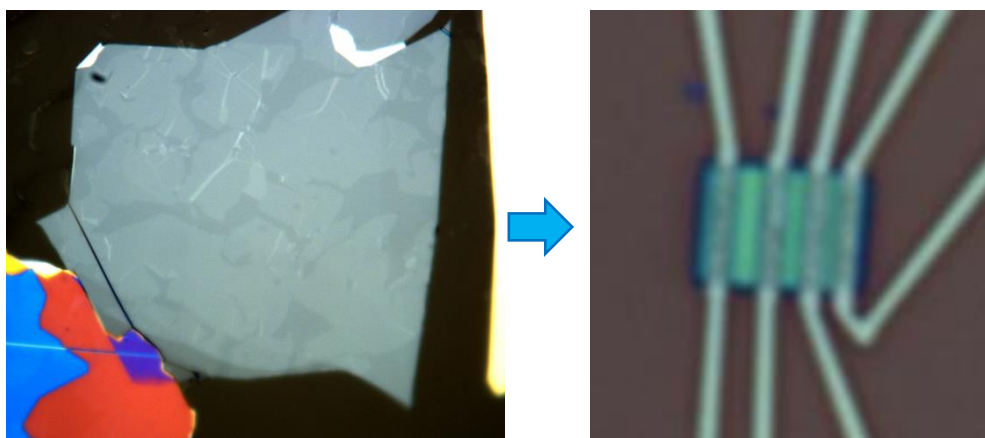
$$G_{th} = (\cancel{G_{diff}} + \cancel{G_{rad}} + G_{ep}) \sim G_{ep}$$



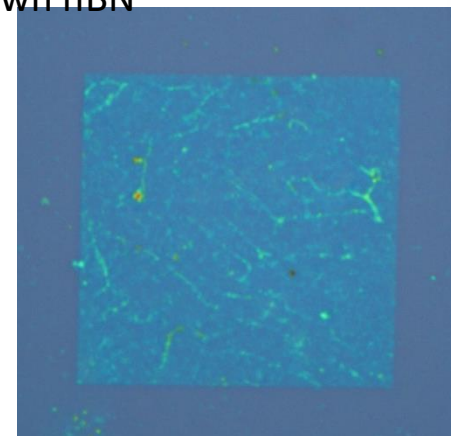
∴ Weak electron-phonon coupling + Small heat capacity
→ **Graphene is a highly promising material for Sensor**

Fabrication of Large-scale Graphene

❖ CVD-grown Graphene with exfoliated hBN

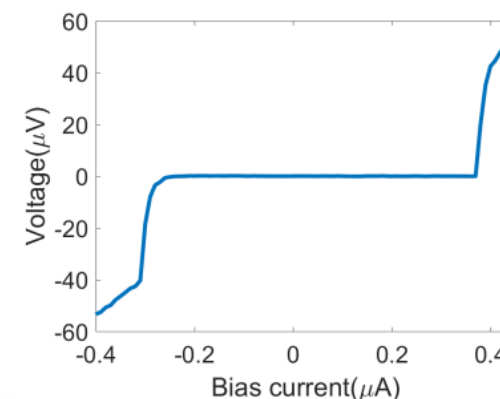
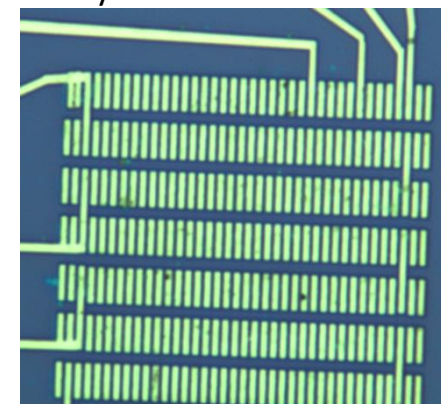


❖ CVD-grown Graphene with CVD grown hBN



hBN/Graphene/hBN stack

231 GJJ array



Seong Jang

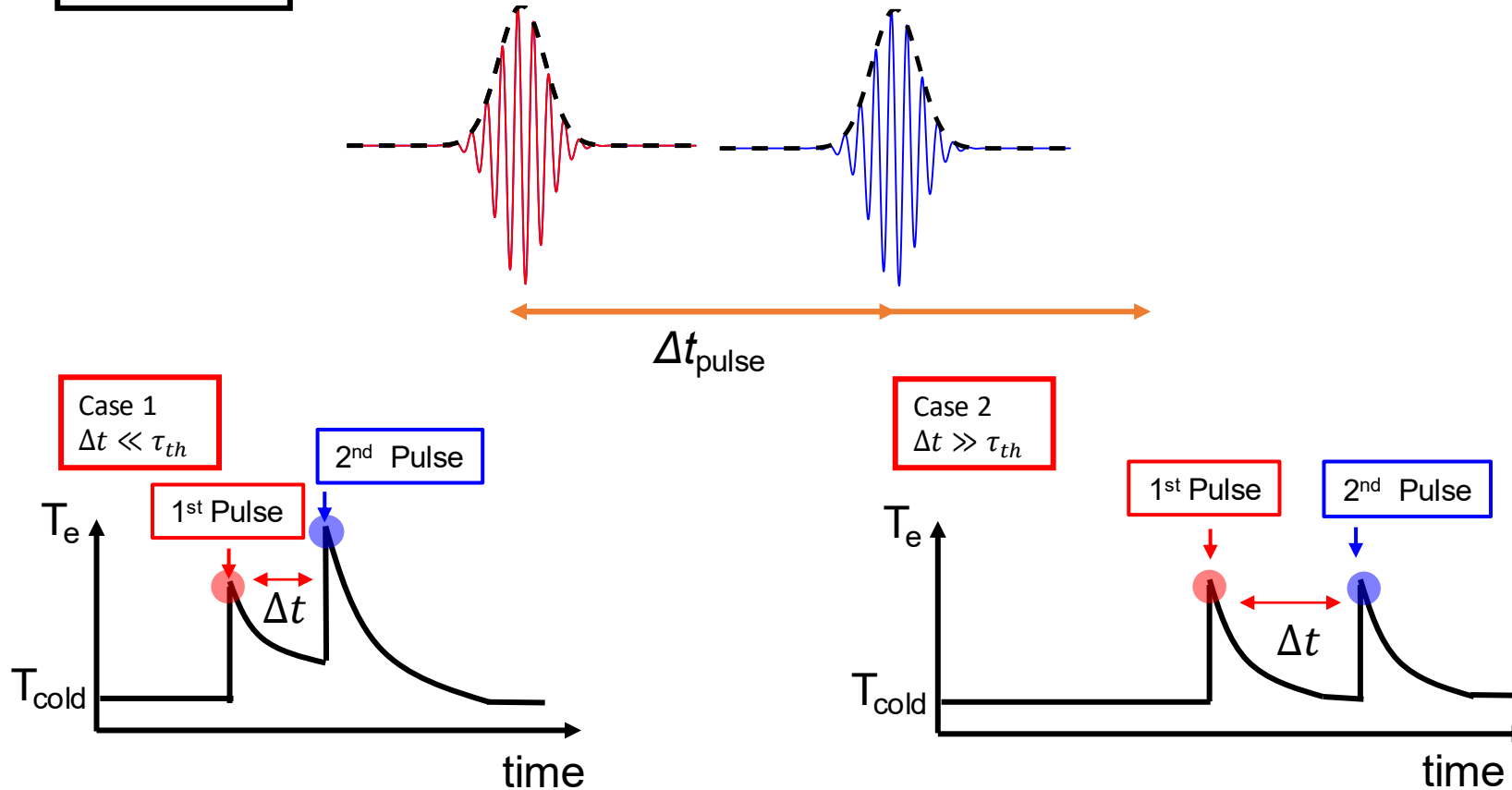


Chae-Gun Lee

GJJs were demonstrated with CVD-grown **large-scale graphene**.

Thermal Relaxation Time Measurement

Method



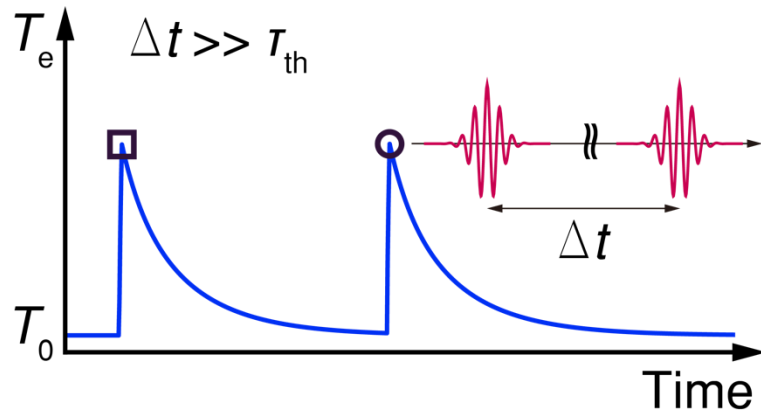
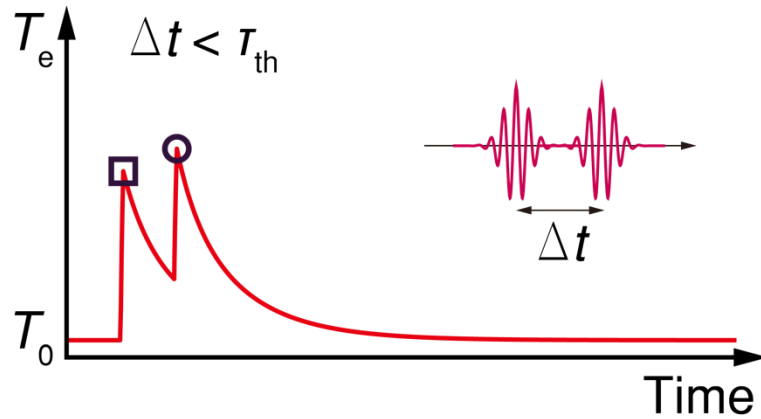
Measure the detection eff. varying Δt_{pulse}

→ Estimated the τ_{th}

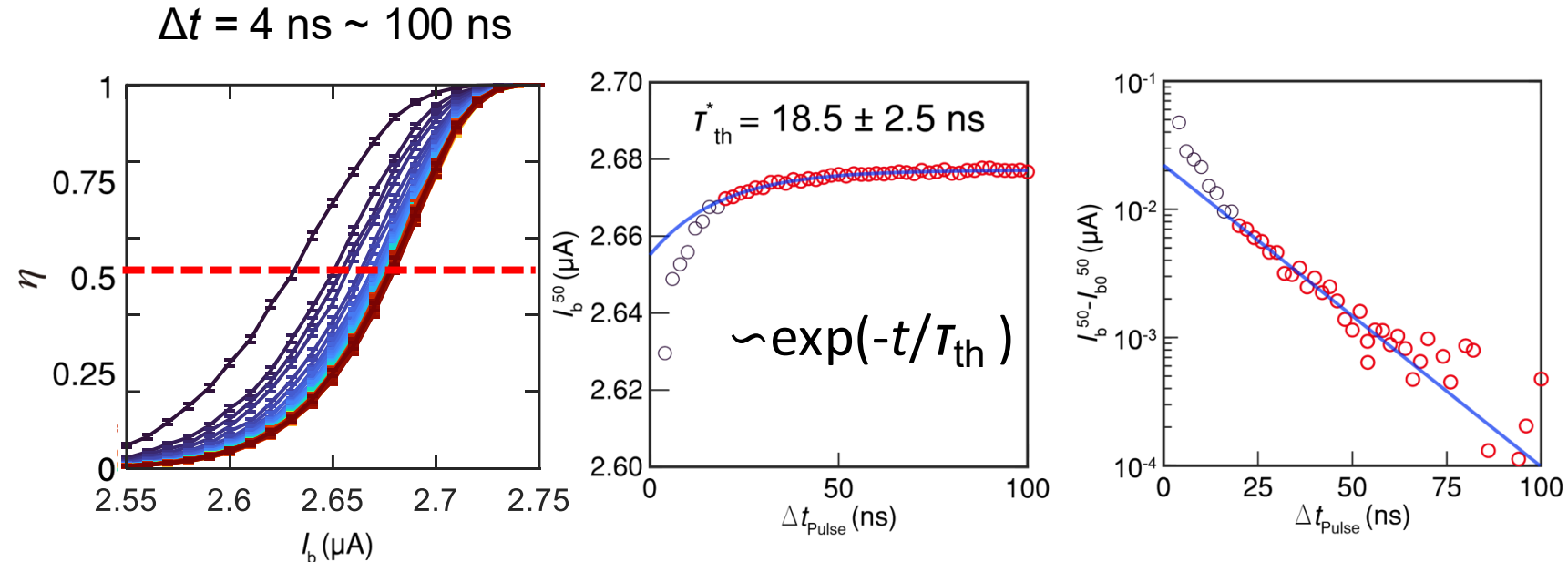
Thermal Relaxation Time Measurement: Time-Resolved Two Pulse Method

$T_0 = 110 \text{ mK}$

$T_e \text{ vs } t \rightarrow T_{\text{peak}} \text{ vs } t \rightarrow \eta \text{ vs } t$



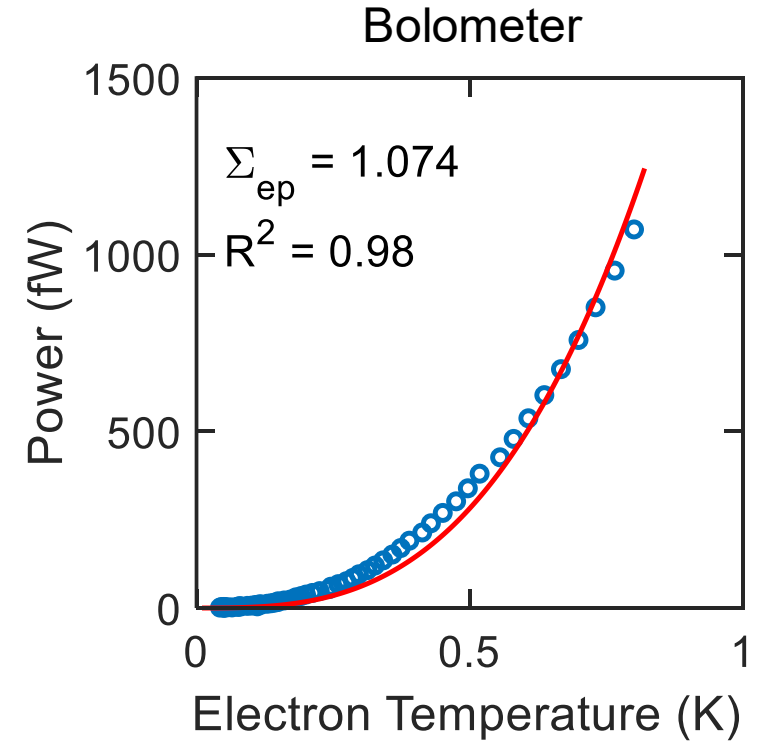
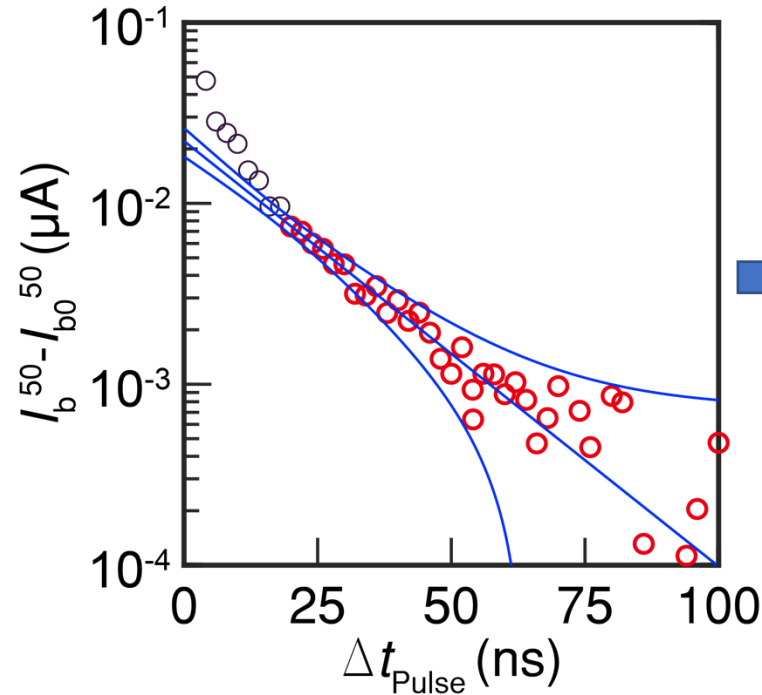
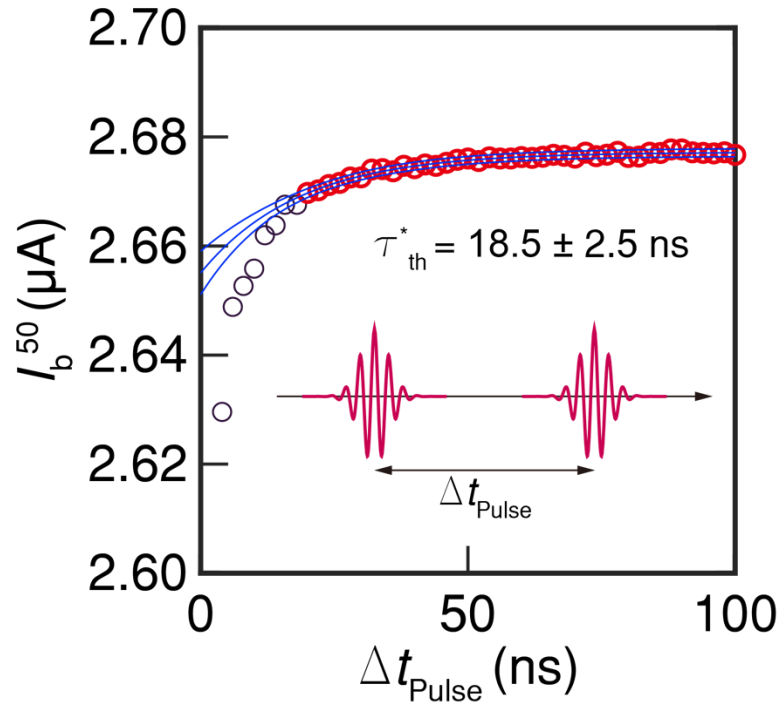
Measure η varying Δt
 $\rightarrow$ Estimate the τ_{th}



$$C_e = G_{\text{th}} * \tau_{\text{th}} = 61.7 \text{ fW/K} * 18.5 \text{ ns}$$

$$= 1.14 \text{ zJ/K} (= 82.6 k_B) \gg C_{e,\text{th}} = 0.177 \text{ zJ/K} (= 12.8 k_B)$$

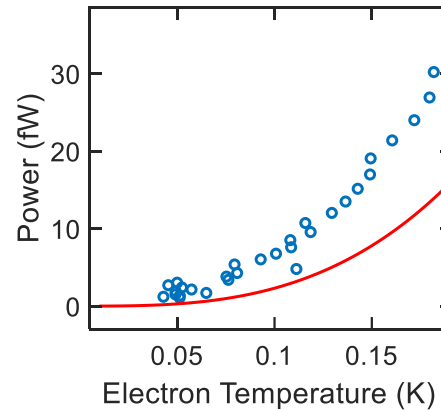
Thermal Relaxation Time Measurement



$$T_e^1 \quad T_e^2 \quad T_e^{-1}$$

$$C_e = G_{\text{th}} * T_{\text{th}}$$

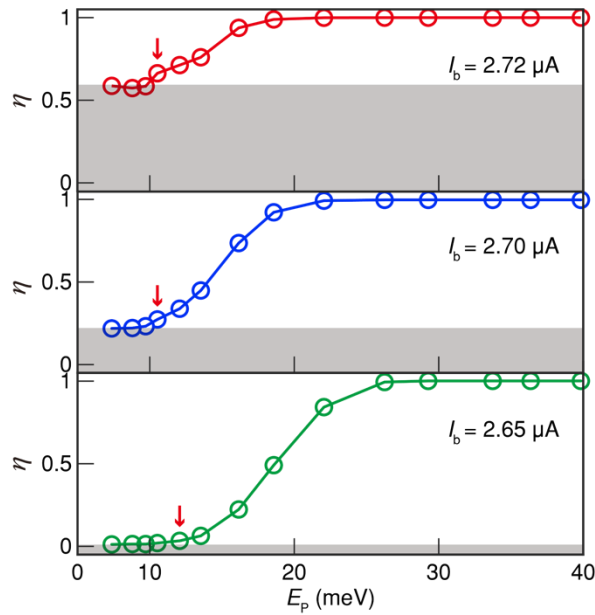
$$= 12.5 \pm 1.69 \text{ yJ/K} (16.1) = 0.9 \pm 0.1 \text{ k}_B (1.2)$$



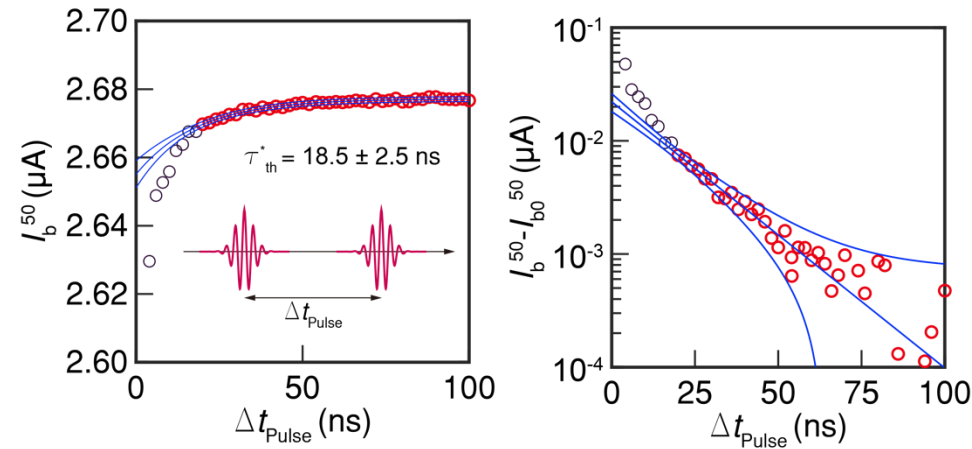
$$\Sigma_{\text{ep}} = 1.07 \text{ W/m}^2\text{K}^3 (0.01)$$

$$\rightarrow G_{\text{th}} = A \Sigma_{\text{ep}} T_e^2 = 674 \text{ aW/K}$$

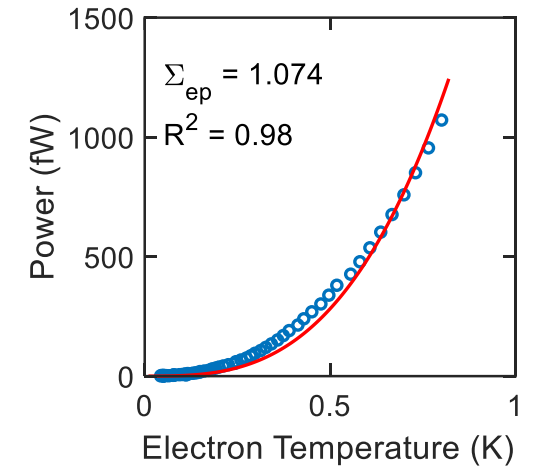
Summary



Calorimeter $\rightarrow E_{\text{thres}} = 10.5 \text{ meV}$ (2.2 meV)



Two-pulse method $\rightarrow \tau_{\text{th}} = 18.5 \text{ ns}$



Bolometer

$\rightarrow G_{\text{th}} = 674 \text{ aW/K}$

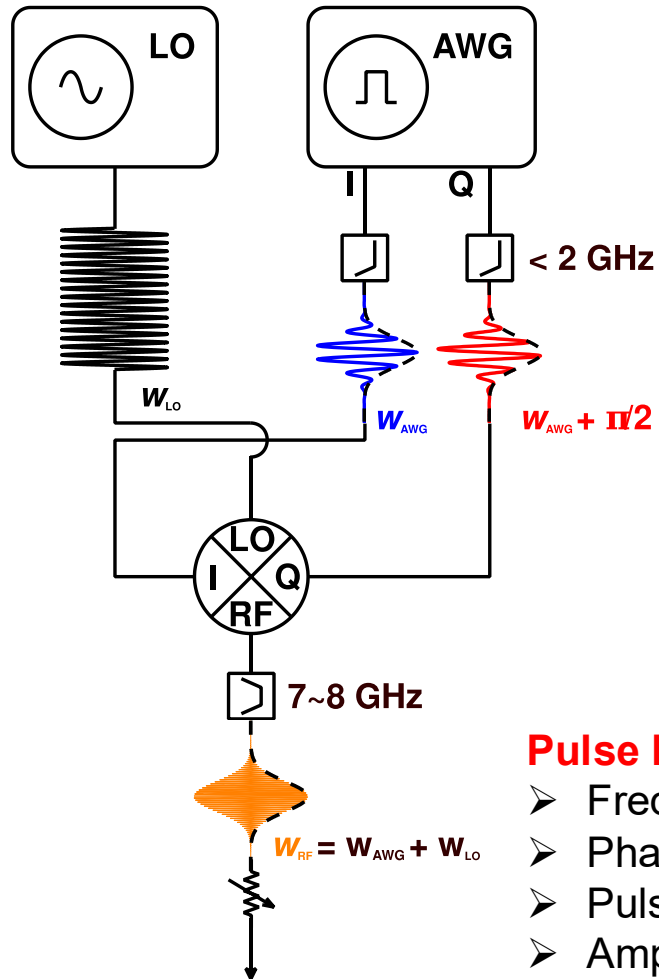
$\Sigma_{\text{ep}} = 1.1 \text{ W/m}^2\text{K}^3$ (0.01)

$$C_e = G_{\text{th}} * \tau_{\text{th}} = 12.5 \pm 1.69 \text{ yJ/K} \text{ (16.1)} = 0.9 \pm 0.1 k_B \text{ (1.2)}$$

The system that enables **these measurements to be performed simultaneously.**

Pulse Generation

Single sideband mixing

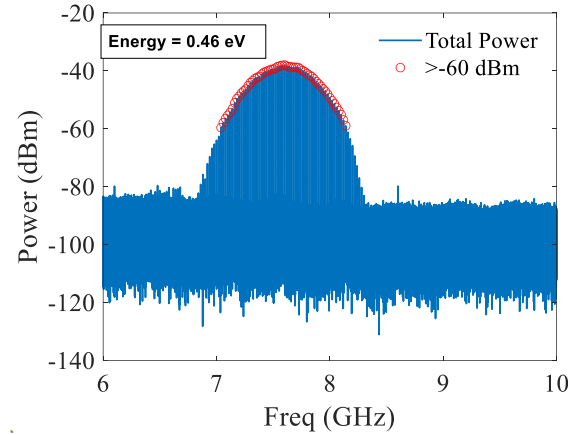


Pulse Parameters

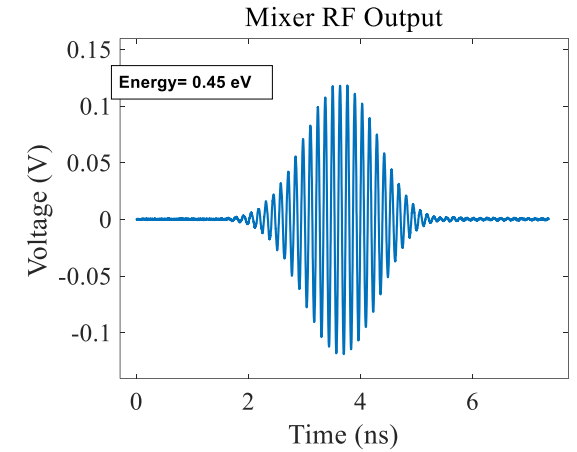
- Frequency
- Phase
- Pulse shape
- Amplitude

Graphene Resonator

Spectrum Analyzer



Oscilloscope

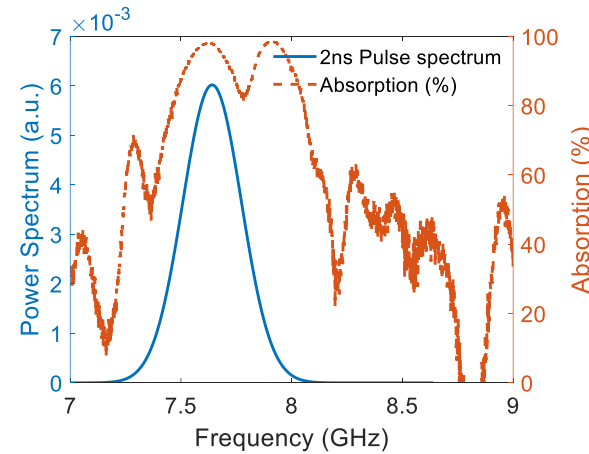


Pulse Energy Calculation

Effective Power = Power > -60 dBm
Sum(Effective Power) * Repetition Time

Pulse Energy Calculation

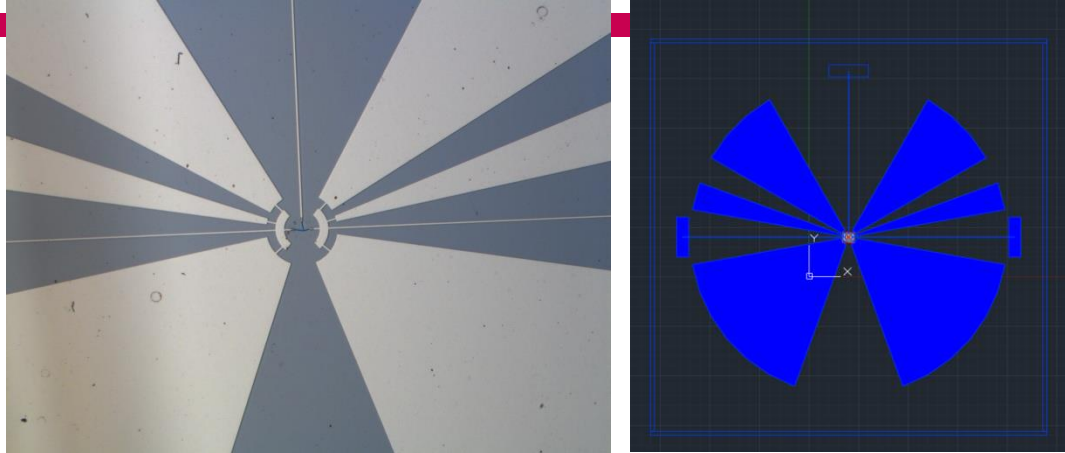
$$\text{Energy} = \sum \frac{V^2}{R} \Delta t$$



Absorption Ratio Cal.

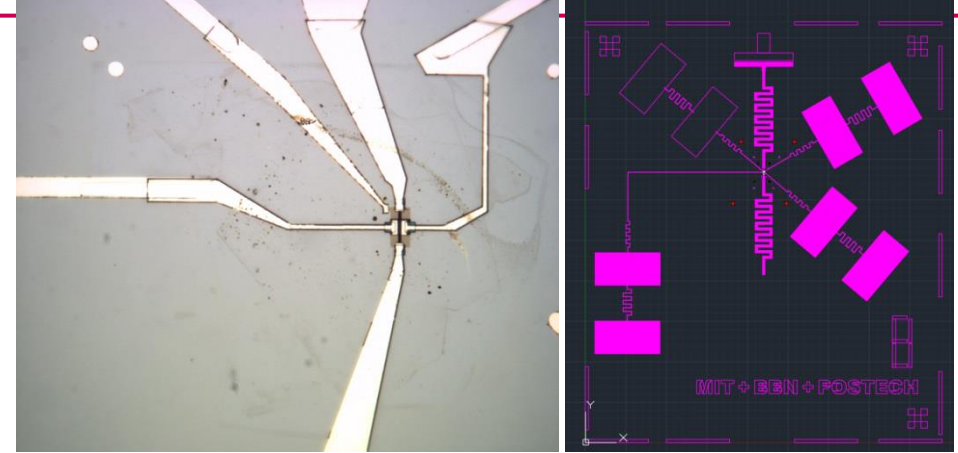
$$E_{\text{absorption}} = E_{\text{Input}} * \text{Absorption Ratio}$$

[LEE03]



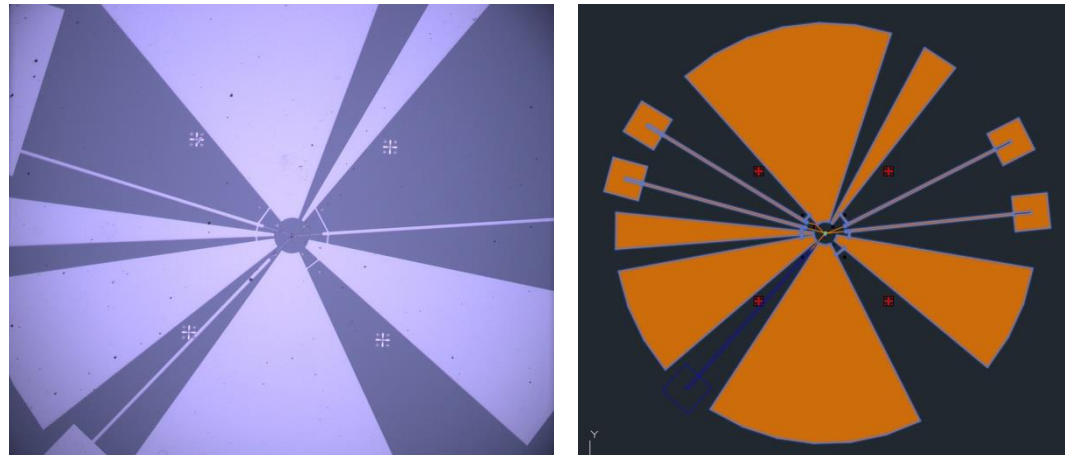
10 mm

[mSPD12]



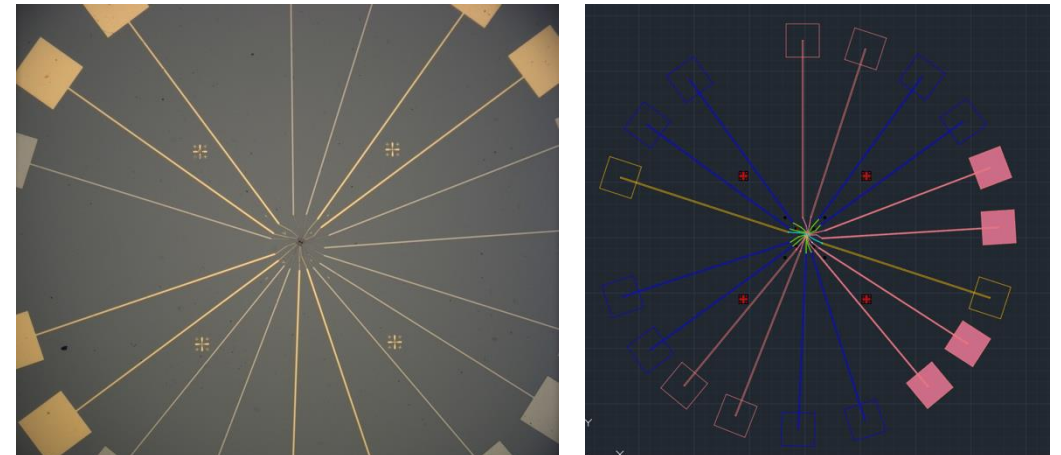
10.9 mm

[LEE02]



2 mm

[LEE01]



2 mm

* SC 면적비 : mSPD12 : LEE03 : LEE02 : LEE01 = 0.36 : 1 : 0.11 : 0.002
mSPD: $1.0 \times 10^7 \text{ um}^2$, LEE03 : $2.8 \times 10^7 \text{ um}^2$, LEE02 : $2.98 \times 10^6 \text{ um}^2$, LEE#1 : $5.2 \times 10^4 \text{ um}^2$

그래핀과 contact이 된 전극은 색을 채워 표시

Future Directions

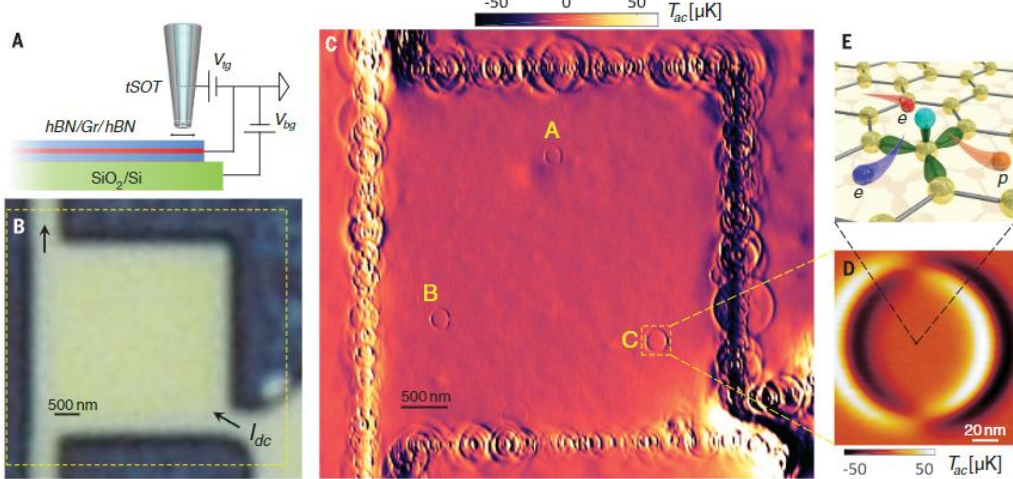
- **Sensitivity Enhancement**

- Reduce electron–phonon coupling
- Improve $dI_c dT$

Thermal Properties

- Exploration of alternative 2D materials (e.g., twisted graphene)

Halbertal et al., Science 358, 1303–1306 (2017)
Local temperature visualized by scanning SQUID thermometry



Atomic disorders at the edges could greatly enhance the value of Σ .

