

Beyond standard dark matter phenomenology with quantum sensors

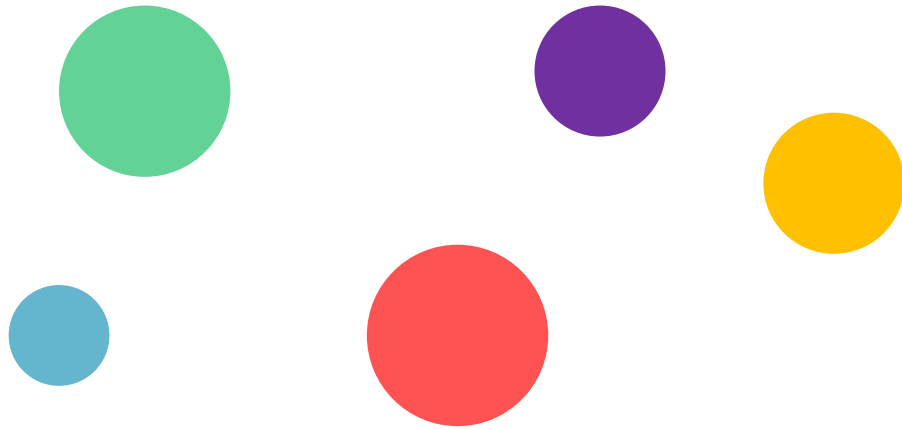
John Carlton

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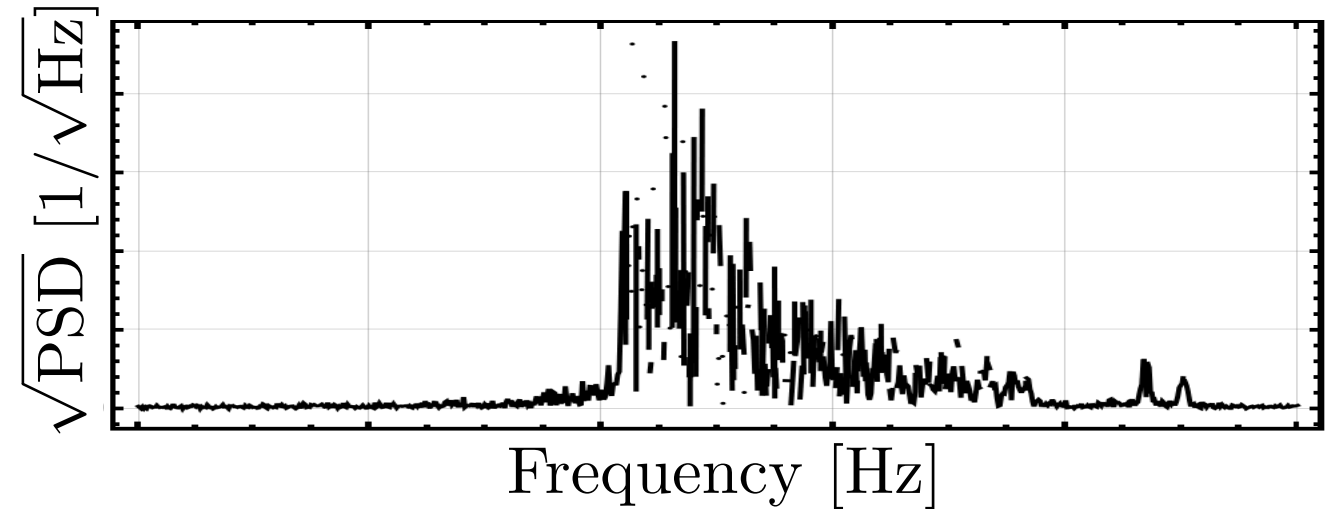


Let's maximise quantum sensor phenomenology

New couplings



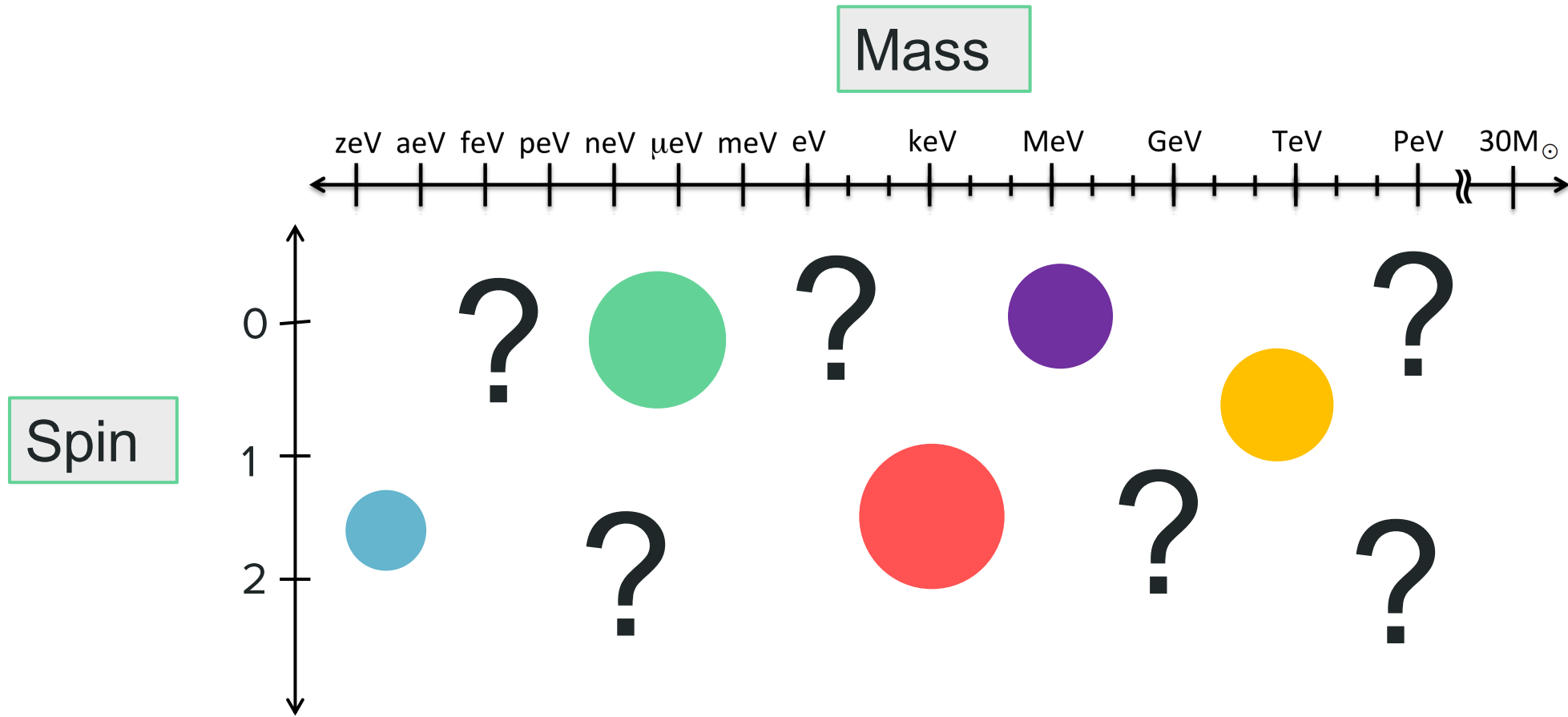
New signatures



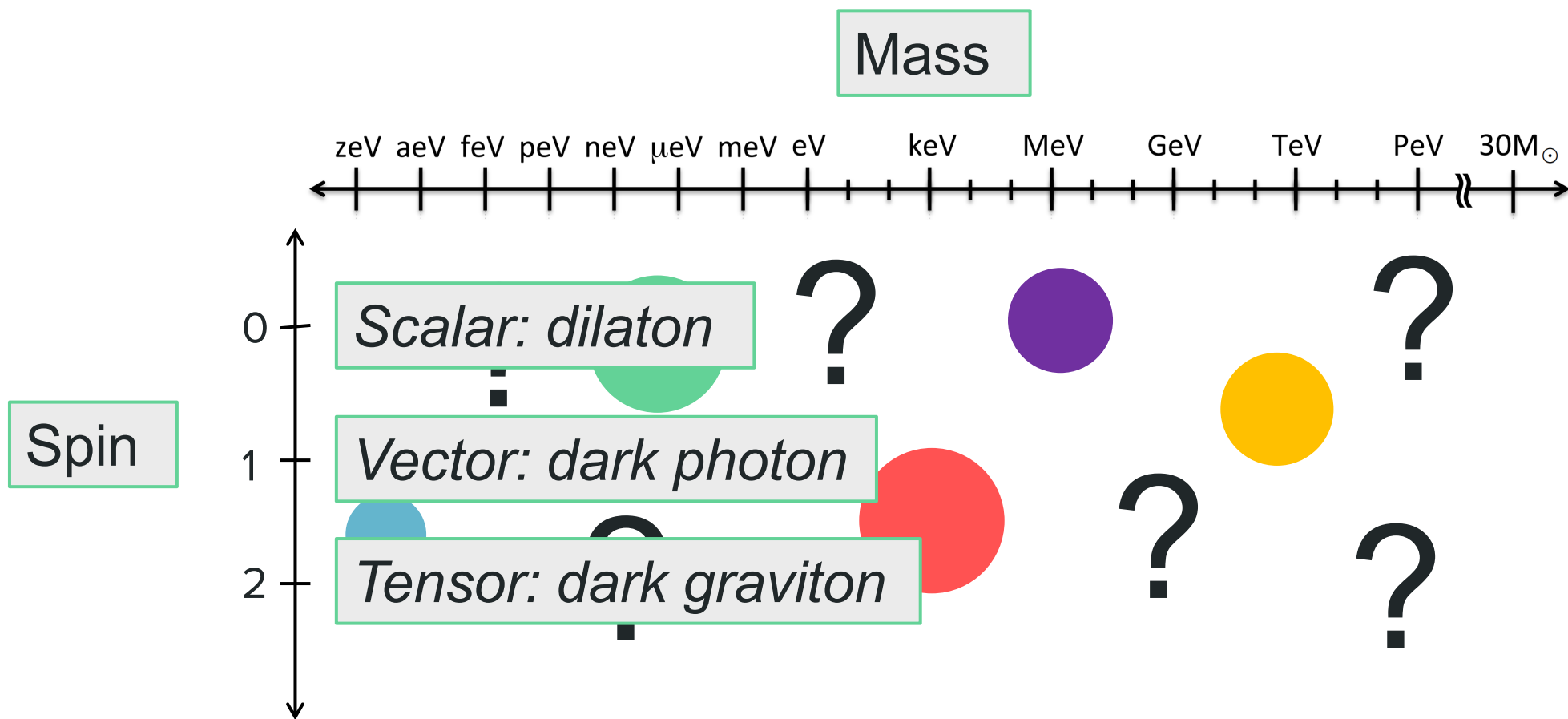
Massive graviton dark matter

Based on D. Blas, J. Carlton, C. McCabe. arXiv: 2412.14282

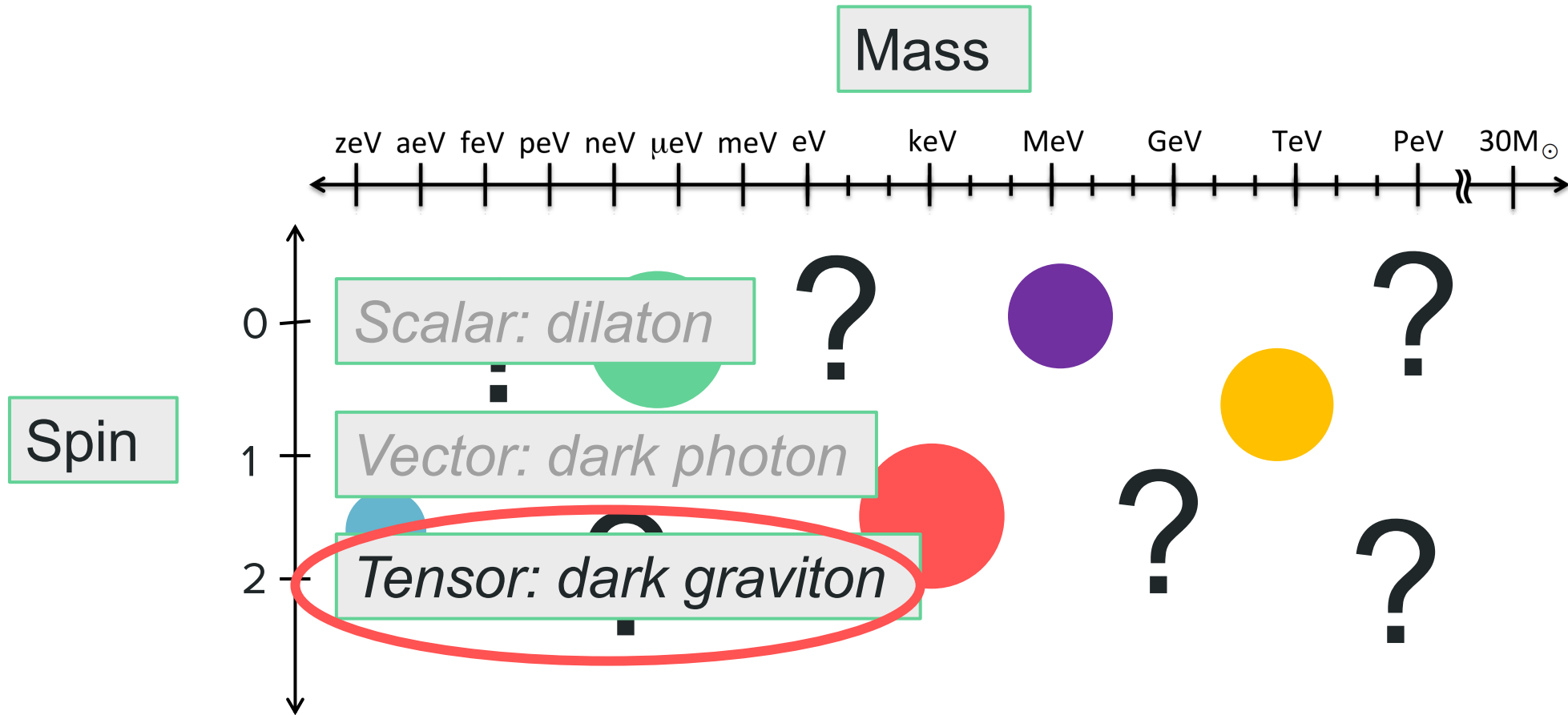
A lot of parameter space!



A lot of parameter space!



What about spin-2?



Massive gravity field theory

Let's consider a massive spin-2 ultra-light field $\varphi_{\mu\nu}$

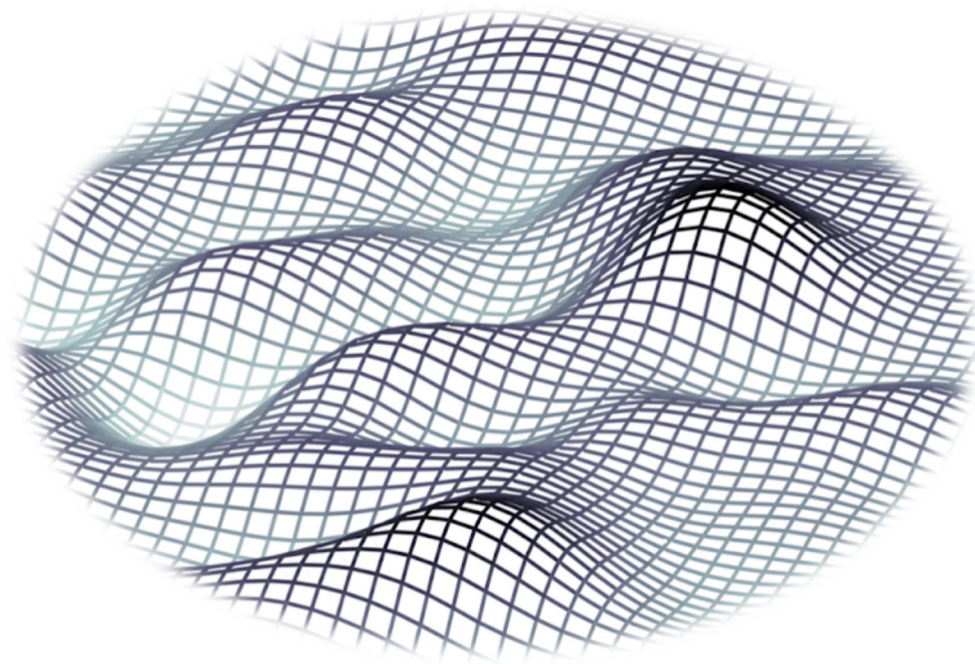
Lorentz *invariant* massive spin-2 field

$$\mathcal{L}_{\text{FP}} = \mathcal{L}_{\text{EH}} - \frac{1}{4}m^2 (\varphi_{\mu\nu}\varphi^{\mu\nu} - \varphi^2)$$

Fierz-Pauli Lagrangian

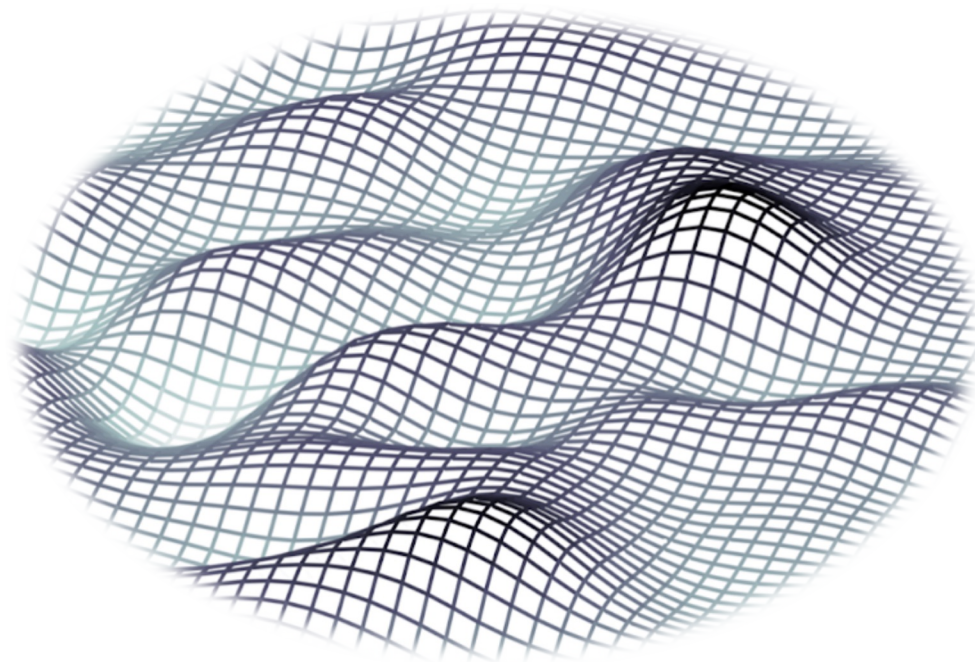
Lorentz *violating* massive spin-2 field

$$\mathcal{L} = \mathcal{L}_{\text{EH}} - \frac{1}{4} \left(m_0^2 \varphi_{00}^2 + 2m_1^2 \varphi_{0i}^2 - m_2^2 \varphi_{ij}^2 + m_3^2 \varphi_i^i \varphi_j^j - 2m_4^2 \varphi_{00} \varphi_i^i \right)$$



Massive gravity field theory

Let's consider a massive spin-2 ultra-light field $\varphi_{\mu\nu}$



Express as irreducible fields:

$$\varphi_{00} = \Psi$$

$$\varphi_{0i} = u_i + \partial_i v$$

$$\varphi_{ij} = \varphi_{ij}^{\text{TT}} + 2\partial_{(i} A_{j)} + \partial_i \partial_j \sigma + \delta_{ij} \pi$$

Tensor

Vector

Scalar

Coupling to light and matter

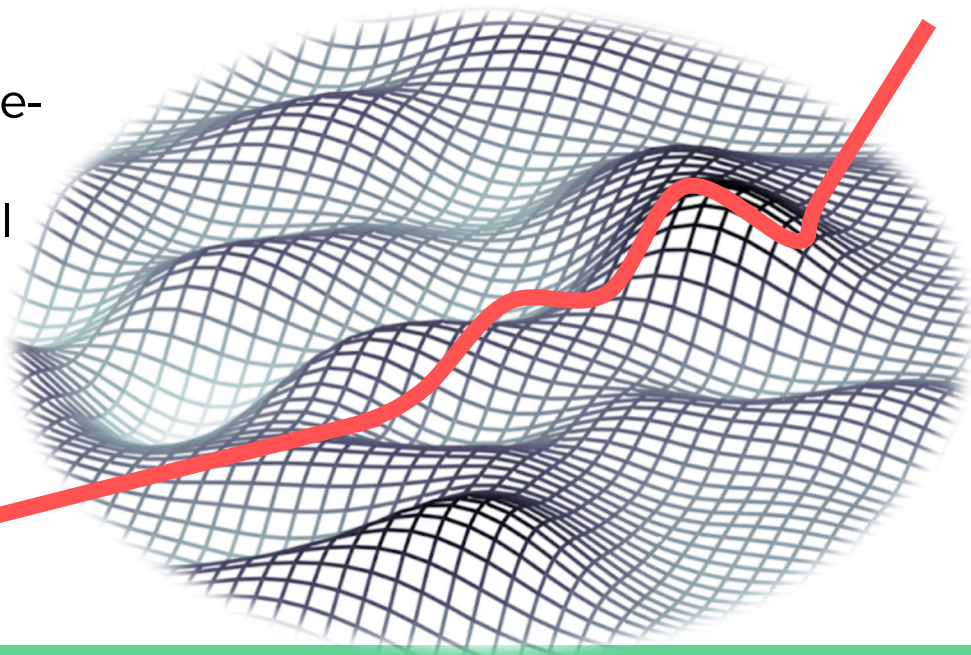
$$\begin{array}{c}
 \text{Tensor} \qquad \qquad \text{Vector} \qquad \qquad \text{Scalar} \\
 \mathcal{L}_{\text{int}} = \kappa^\phi \varphi^{\mu\nu} \mathcal{O}_{\mu\nu} \longrightarrow \kappa_t \varphi^{ij} \mathcal{O}_{ij}^t + \kappa_v \varphi^{0i} \mathcal{O}_{0i}^v + \kappa_s \varphi^{00} \mathcal{O}^s \\
 \downarrow \qquad \qquad \qquad \text{Non-relativistic limit} \qquad \qquad \downarrow \\
 \frac{\beta^{(2)}}{\Lambda} \varphi_{ij}^{\text{TT}} F^{i\sigma} F_\sigma^j \qquad \qquad \left(\frac{\beta^{(0)}}{\Lambda} F^2 + m_\psi \frac{\alpha^{(0)}}{\Lambda} \bar{\psi} \psi \right) \tilde{\pi} \\
 \text{In all theories} \qquad \qquad \qquad \text{Only in Lorentz violating theories!}
 \end{array}$$

Coupling to light and matter

Tensor modes

$$\frac{\beta^{(2)}}{\Lambda} \varphi_{ij}^{\text{TT}} F^{i\sigma} F_{\sigma}^j$$

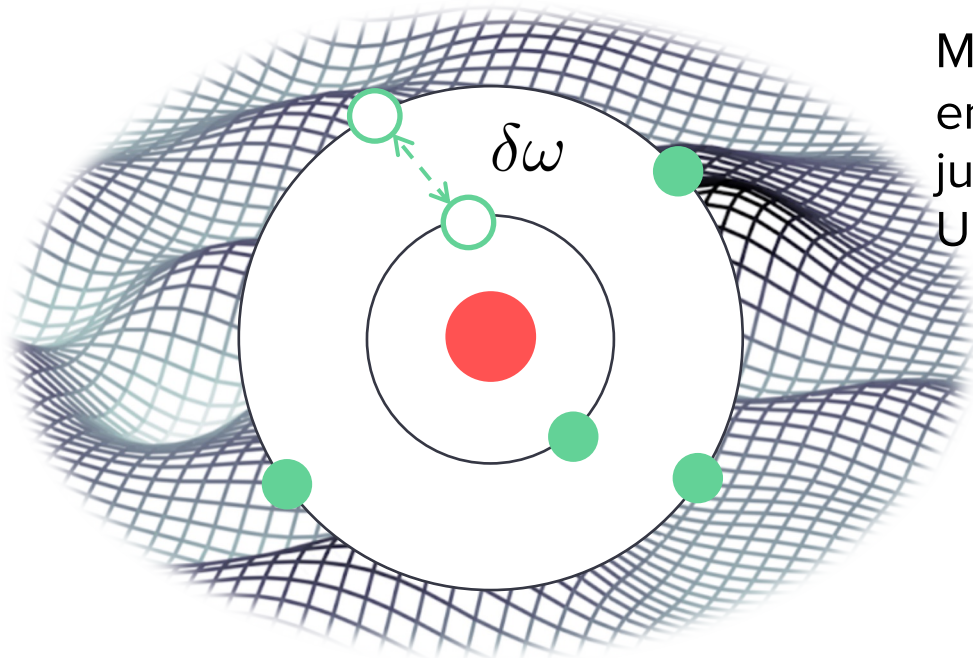
Bends space-
time like
gravitational
waves!



Scalar modes

$$\left(\frac{\beta^{(0)}}{\Lambda} F^2 + m_{\psi} \frac{\alpha^{(0)}}{\Lambda} \bar{\psi} \psi \right) \tilde{\pi}$$

Modifies atomic
energy levels
just like scalar
ULDM!



All the possible couplings

Matter couplings

$$\begin{aligned}\mathcal{H} = & \sqrt{\rho_{\text{DM}}} \left(\frac{\alpha^{(0)}}{\Lambda} X(t) + \frac{\alpha^{(1)}}{\Lambda} v_A^i V_i(t) + \frac{\alpha^{(2)}}{\Lambda} v_A^i v_A^j M_{ij}(t) \right) m_A \delta^{(3)}(\vec{x} - \vec{x}_A(t)) \\ & + \sqrt{\rho_{\text{DM}}} \left(\frac{\beta^{(0)}}{\Lambda} (F^2 Y_1(t) + F_{0i} F^{0i} Y_2(t)) + \frac{\beta^{(1)}}{\Lambda} F_{\sigma 0} F^{i\sigma} W_i(t) + \frac{\beta^{(2)}}{\Lambda} F^{i\sigma} F_{\sigma}^j N_{ij}(t) \right)\end{aligned}$$

Light couplings

All the possible couplings

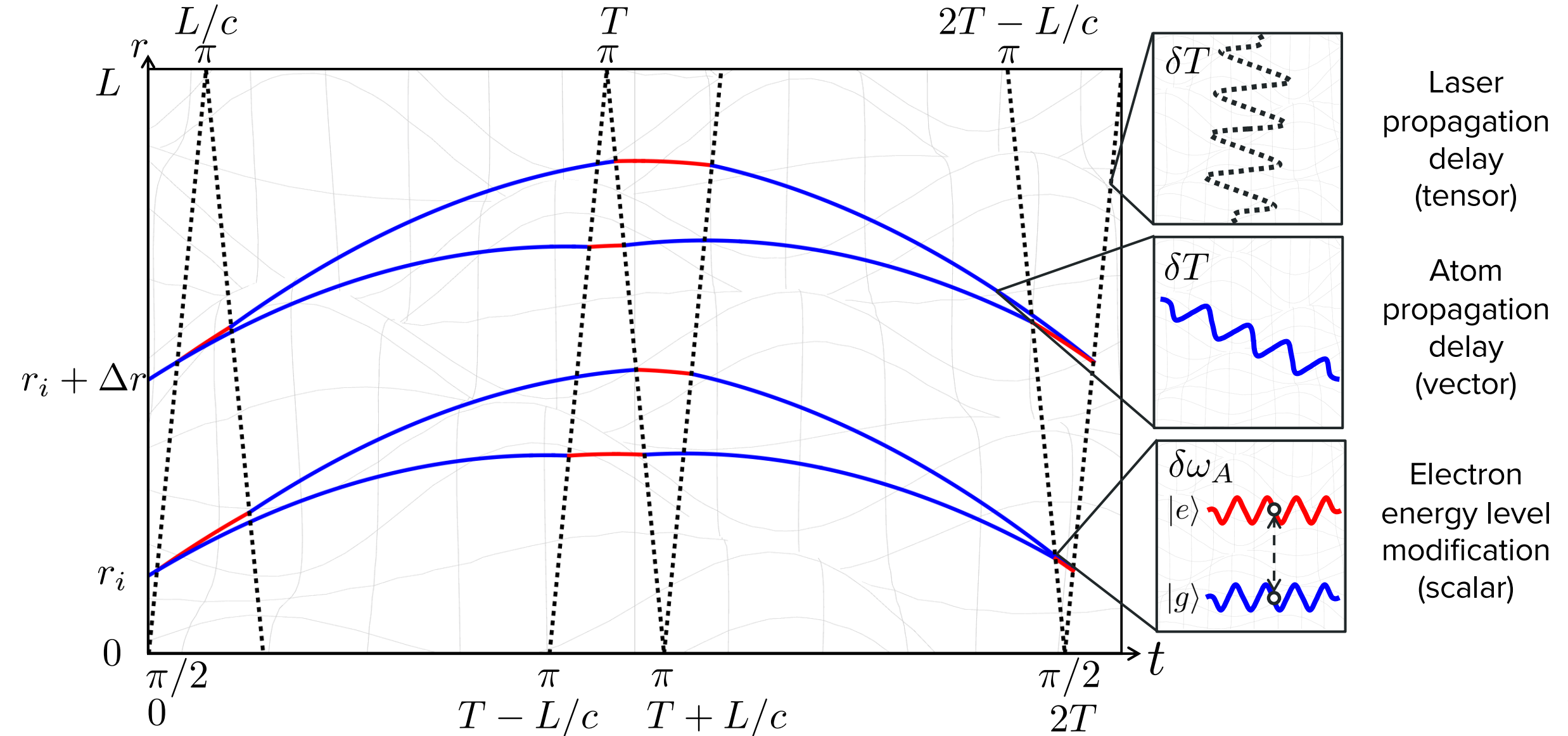
Matter couplings

$$\begin{aligned}
 \mathcal{H} = & \sqrt{\rho_{\text{DM}}} \left(\frac{\alpha^{(0)}}{\Lambda} X(t) + \frac{\alpha^{(1)}}{\Lambda} v_A^i V_i(t) + \frac{\alpha^{(2)}}{\Lambda} v_A^i v_A^j M_{ij}(t) \right) m_A \delta^{(3)}(\vec{x} - \vec{x}_A(t)) \\
 & + \sqrt{\rho_{\text{DM}}} \left(\frac{\beta^{(0)}}{\Lambda} (F^2 Y_1(t) + F_{0i} F^{0i} Y_2(t)) + \frac{\beta^{(1)}}{\Lambda} F_{\sigma 0} F^{i\sigma} W_i(t) + \frac{\beta^{(2)}}{\Lambda} F^{i\sigma} F_{\sigma}^j N_{ij}(t) \right)
 \end{aligned}$$

Electron mass variation
 Atom propagation delay
 Fine structure variation
 Laser propagation delay

Light couplings

Three sensitivity channels in atom interferometers!



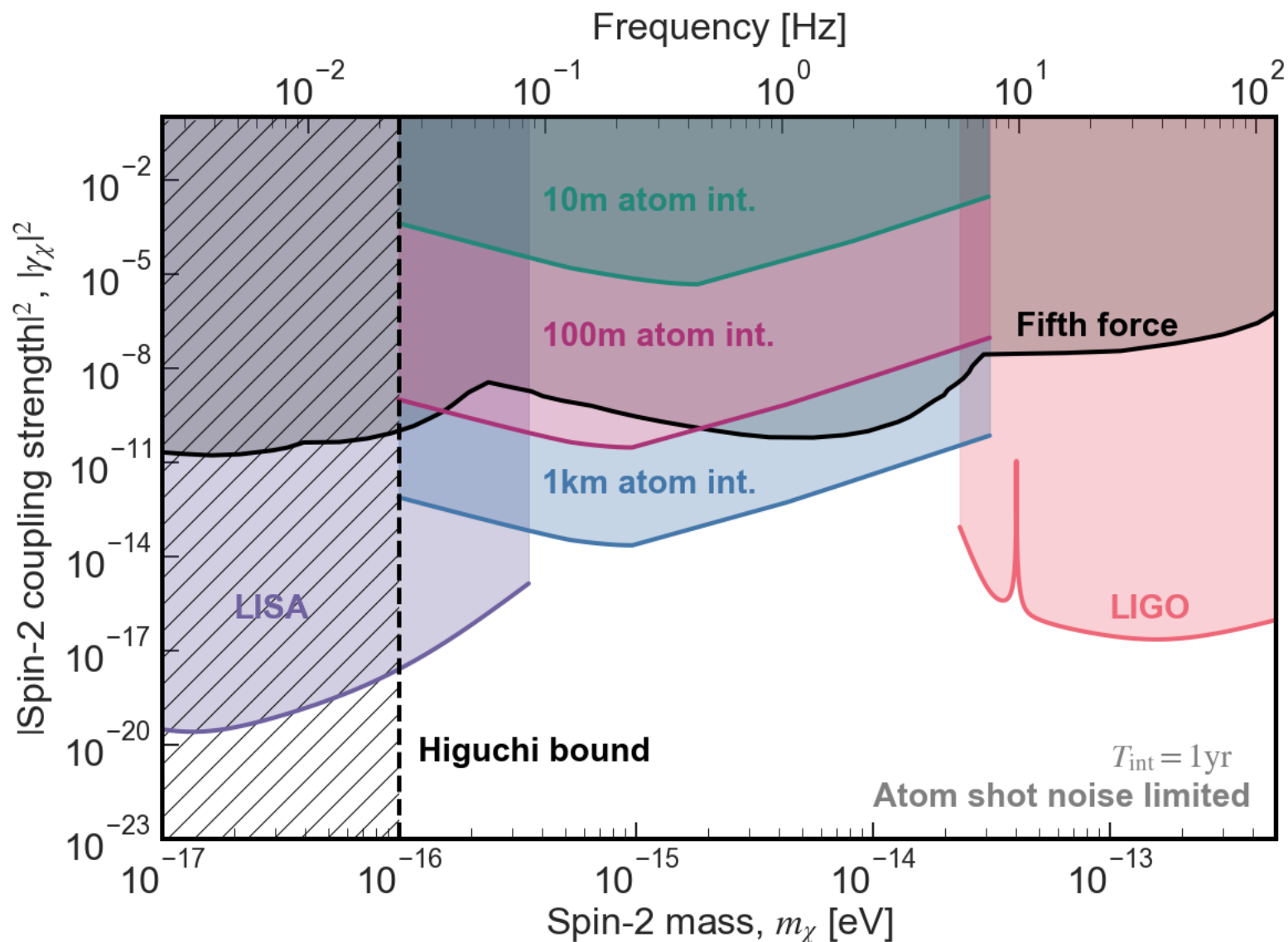
Projected detection limits

Leading constraints on scalar mode come from ‘fifth force’ experiments

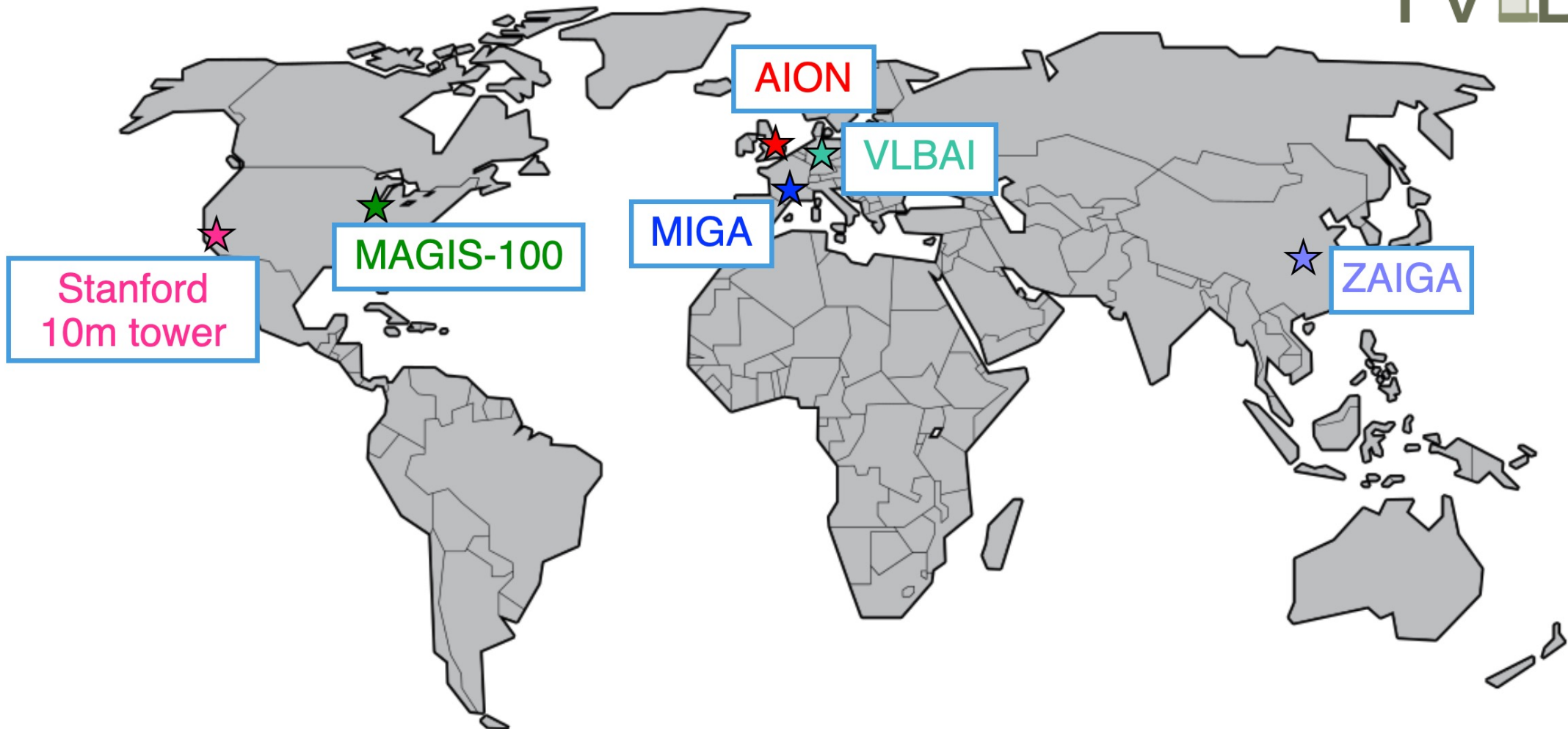
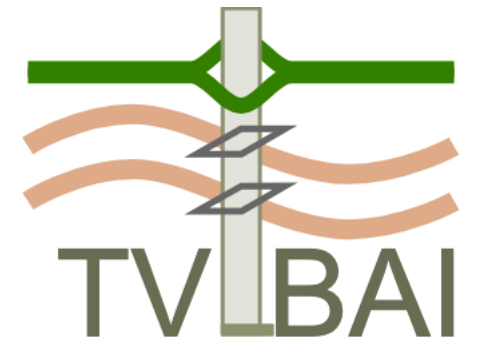
$$\delta V_{\text{Newt}} \propto (\alpha^{(0)})^2 e^{-m_s r}$$

In this range, from lunar laser ranging

In absence of scalar mode,
no constraints on vector
and tensor modes!



Part of a global network!



Dark matter in the solar system

Based on J. Carlton, S. Gardner. (In progress)

Gravitational focusing of wave dark matter

Under Schrödinger-Poisson formalism find
analytic solutions to wave dark matter scattering
analogous to Coulomb scattering

$$\psi(r, k) \propto {}_1F_1(i\xi_{\text{foc}}/2\pi, 1, ikr(1 - \hat{\mathbf{k}} \cdot \hat{\mathbf{r}}))$$

Controlled by focusing parameter

$$\xi_{\text{foc}} = \frac{\lambda_{\text{dB}}}{R_*} = \frac{\lambda_{\text{dB}}}{1/GM_{\odot}m_{\text{DM}}^2} = \frac{2\pi GM_{\odot}m_{\text{DM}}}{v_{\text{DM}}}$$

$$\xi_{\text{foc}} \ll 1$$

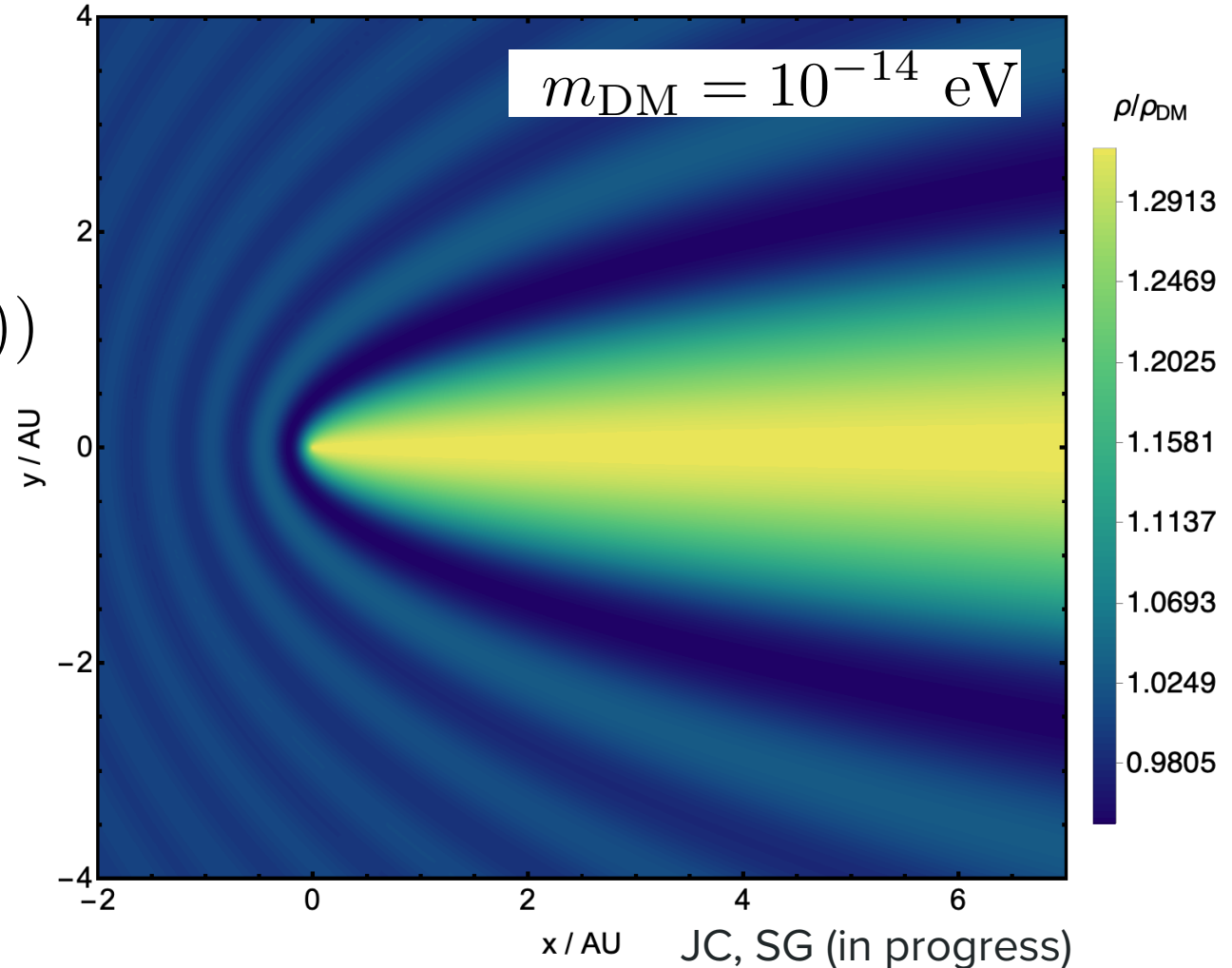
No focusing

$$\xi_{\text{foc}} \gg 1$$

Too focused

$$\xi_{\text{foc}} \sim 1$$

Just right



ULDM focused by the Sun

Sub-halo formation around celestial bodies

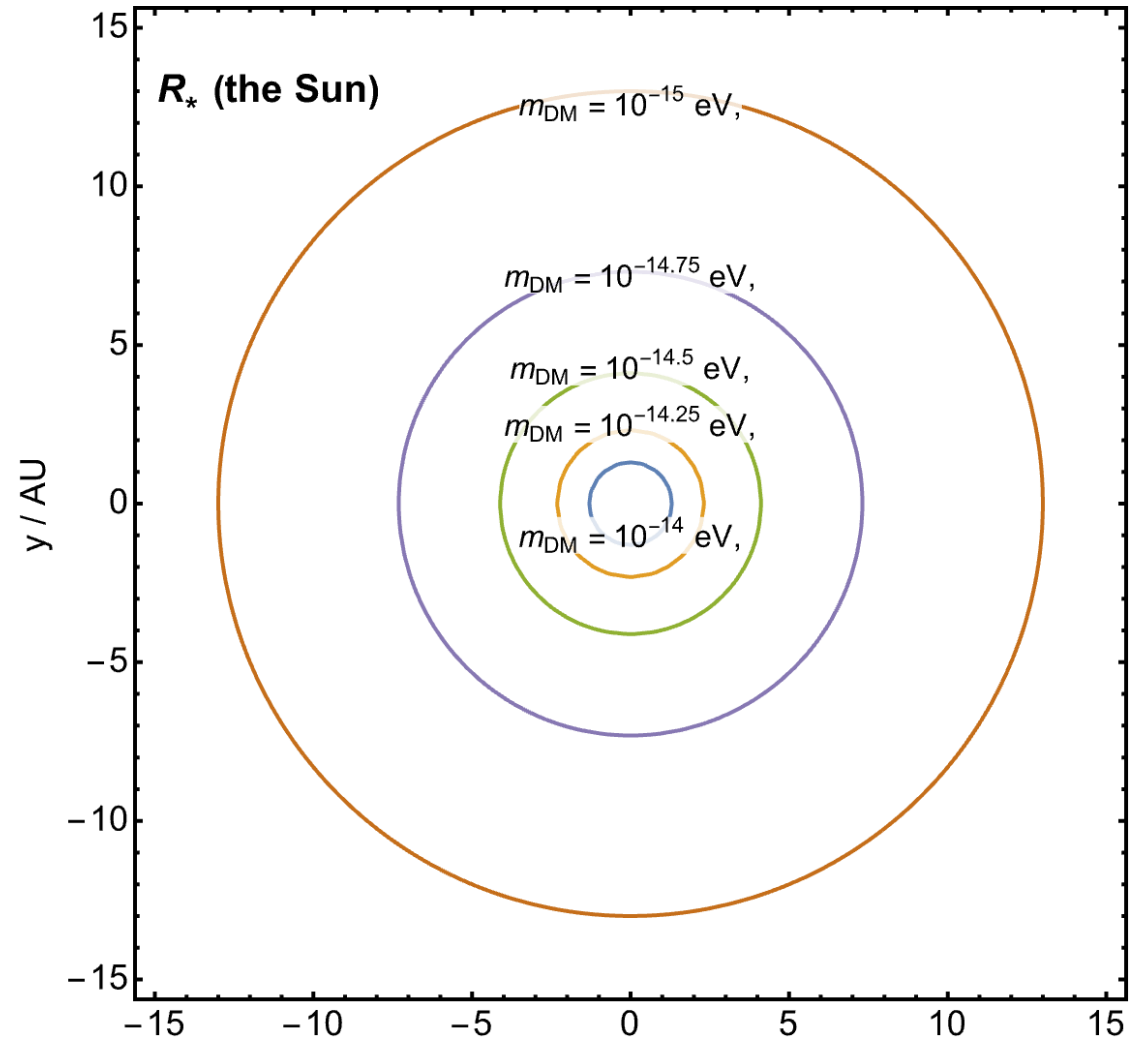
DM self-interactions can cause focused DM to slow down and become captured by celestial objects

Assume quartic self-interactions $V \supset \frac{\lambda}{4!} \varphi^4$

Where: $\lambda \equiv -m_{\text{DM}}^2 / f_a^2$

Relaxation time tracks sub-halo capture and growth process

$$\tau_{\text{rel}} \equiv \frac{64 m_{\text{DM}}^7 v_{\text{DM}}^2}{\lambda^2 \rho_{\text{DM}}^2}$$



Sub-halo formation around celestial bodies

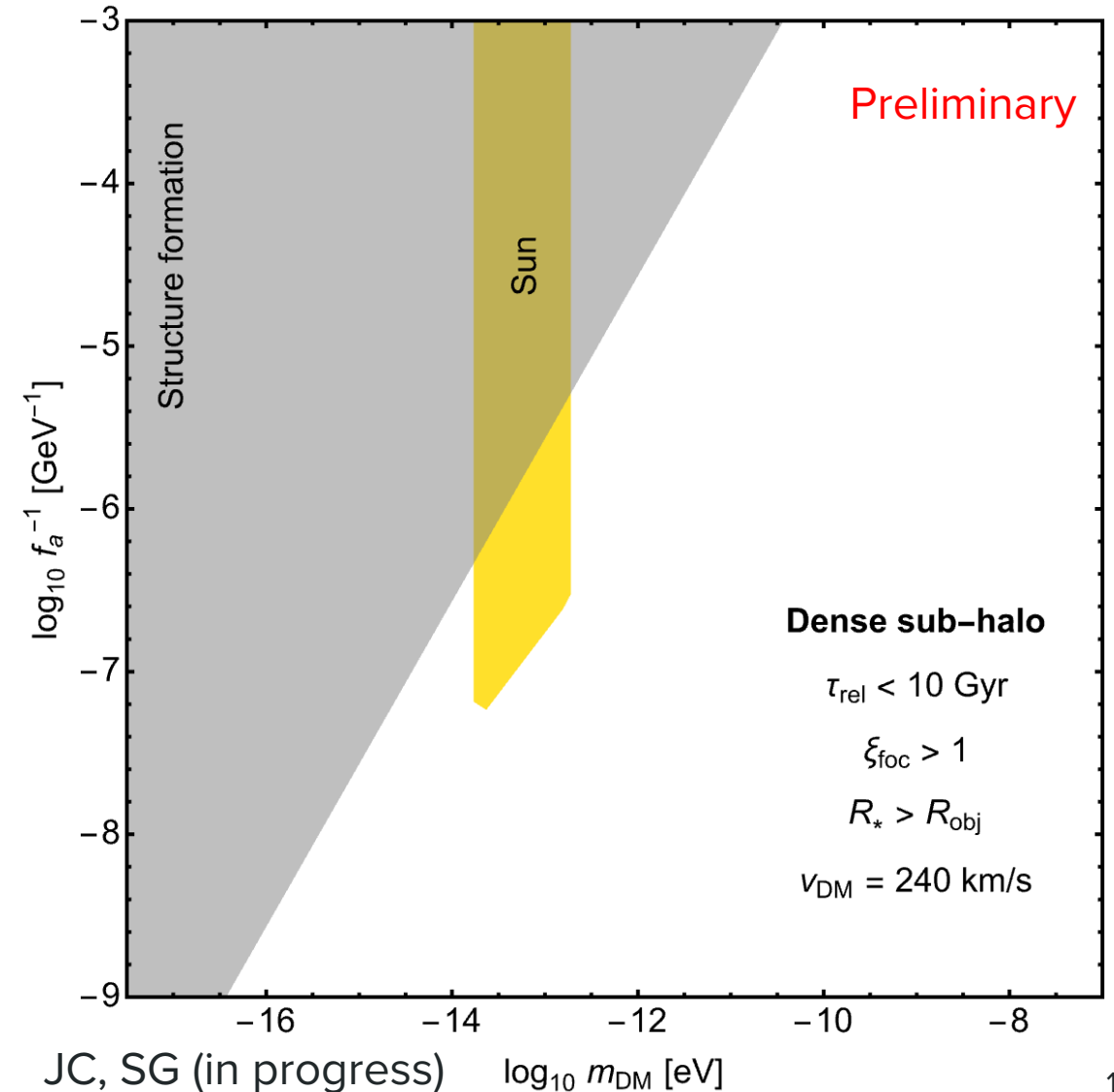
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Sub-halo formation around celestial bodies

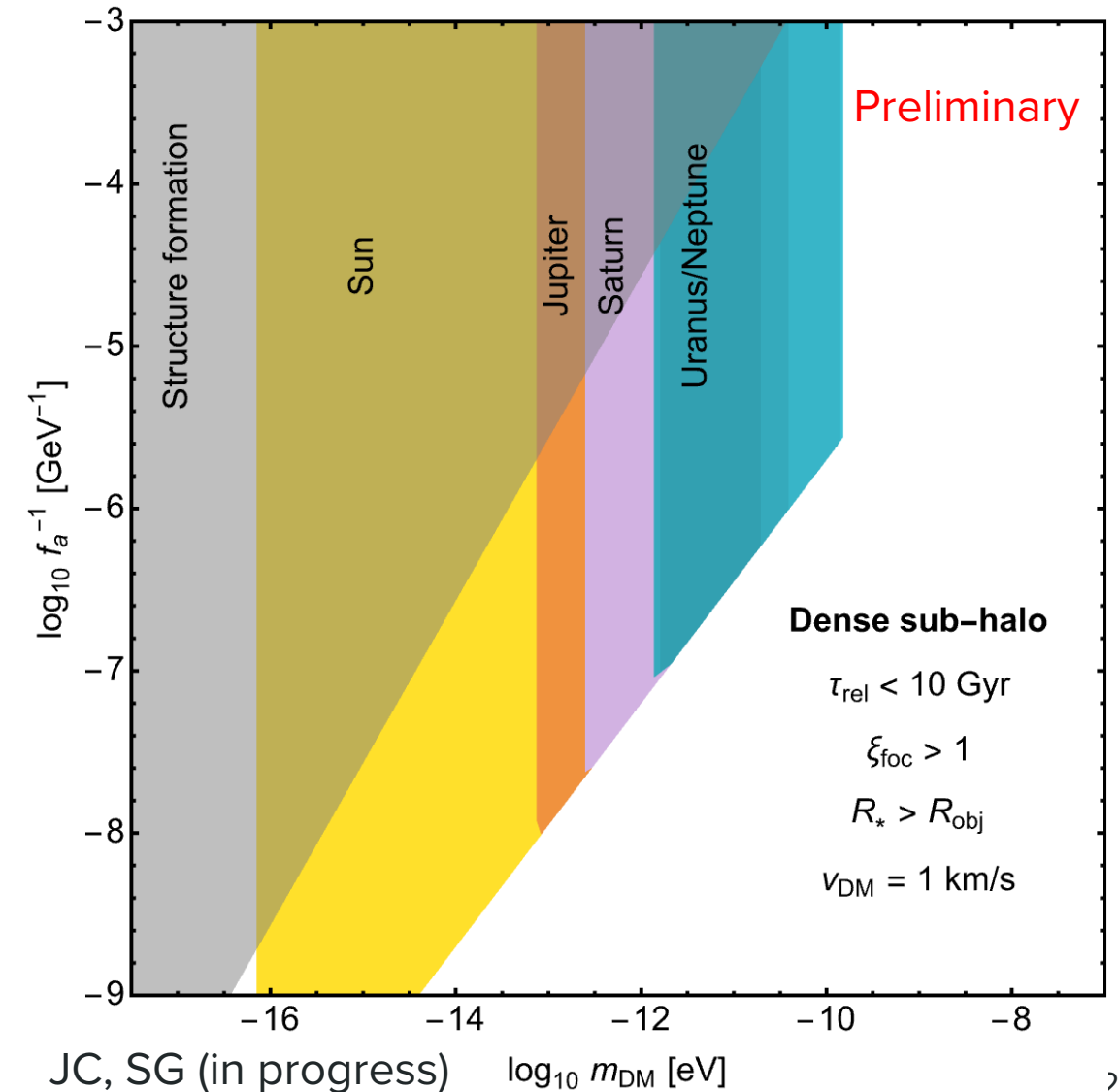
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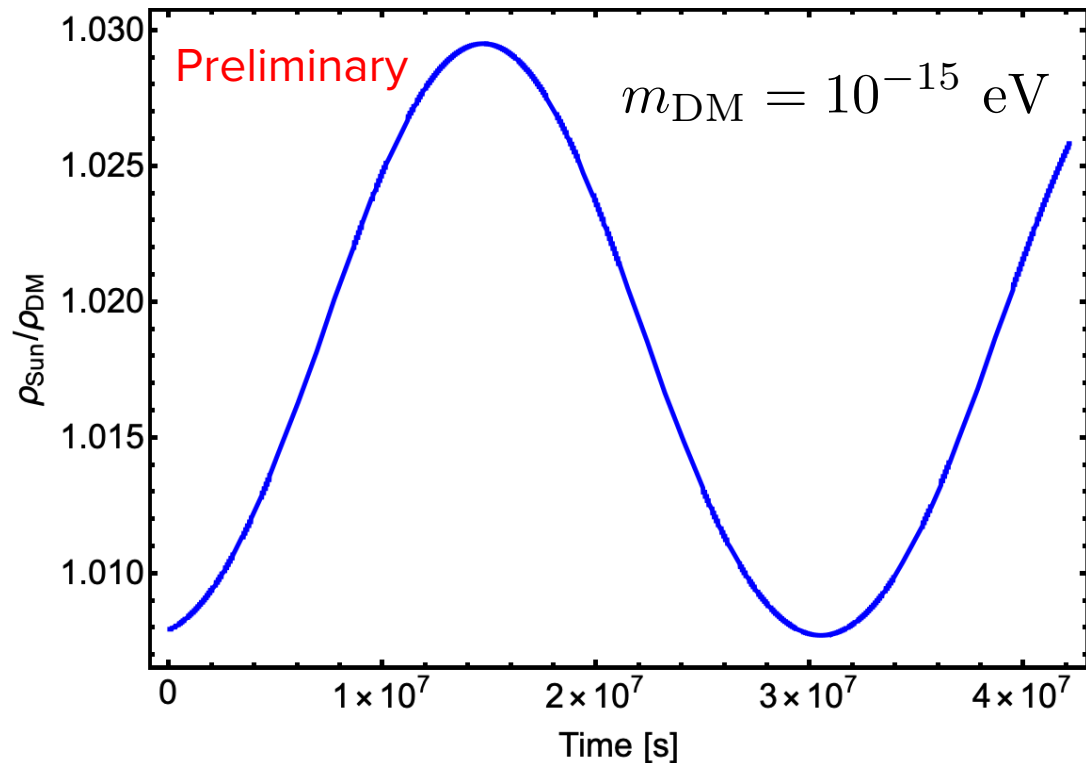
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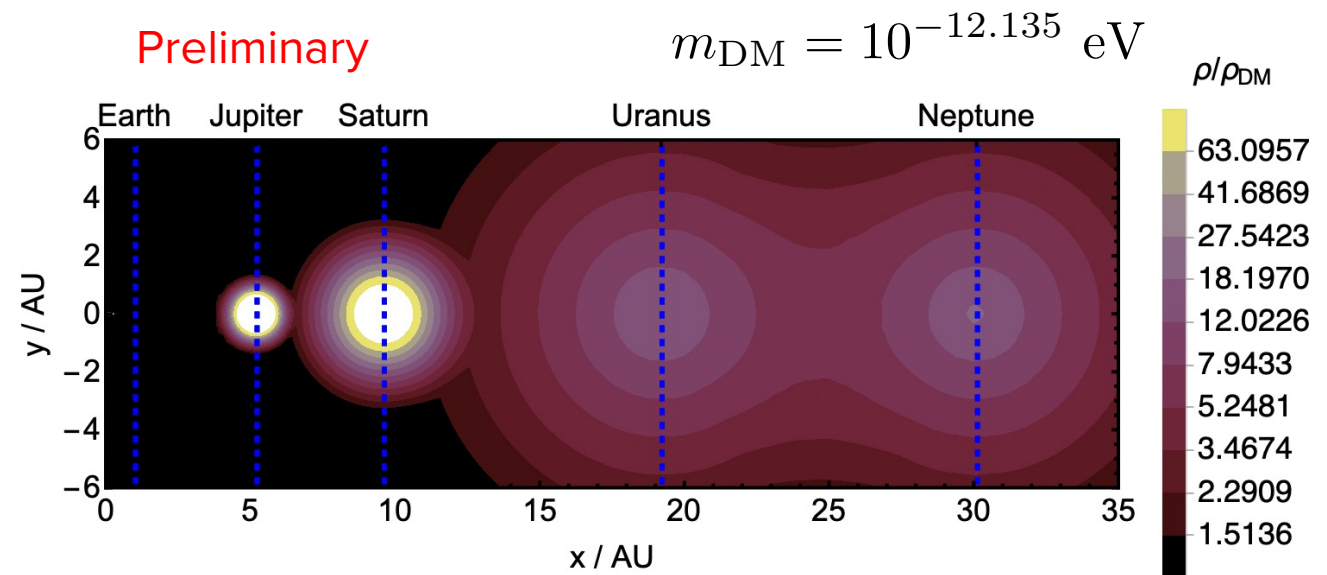
Experimental signatures – over-densities

Unbound (gravitational focusing)



Oscillating lighthouse effect of
solar-focused dark matter density on Earth

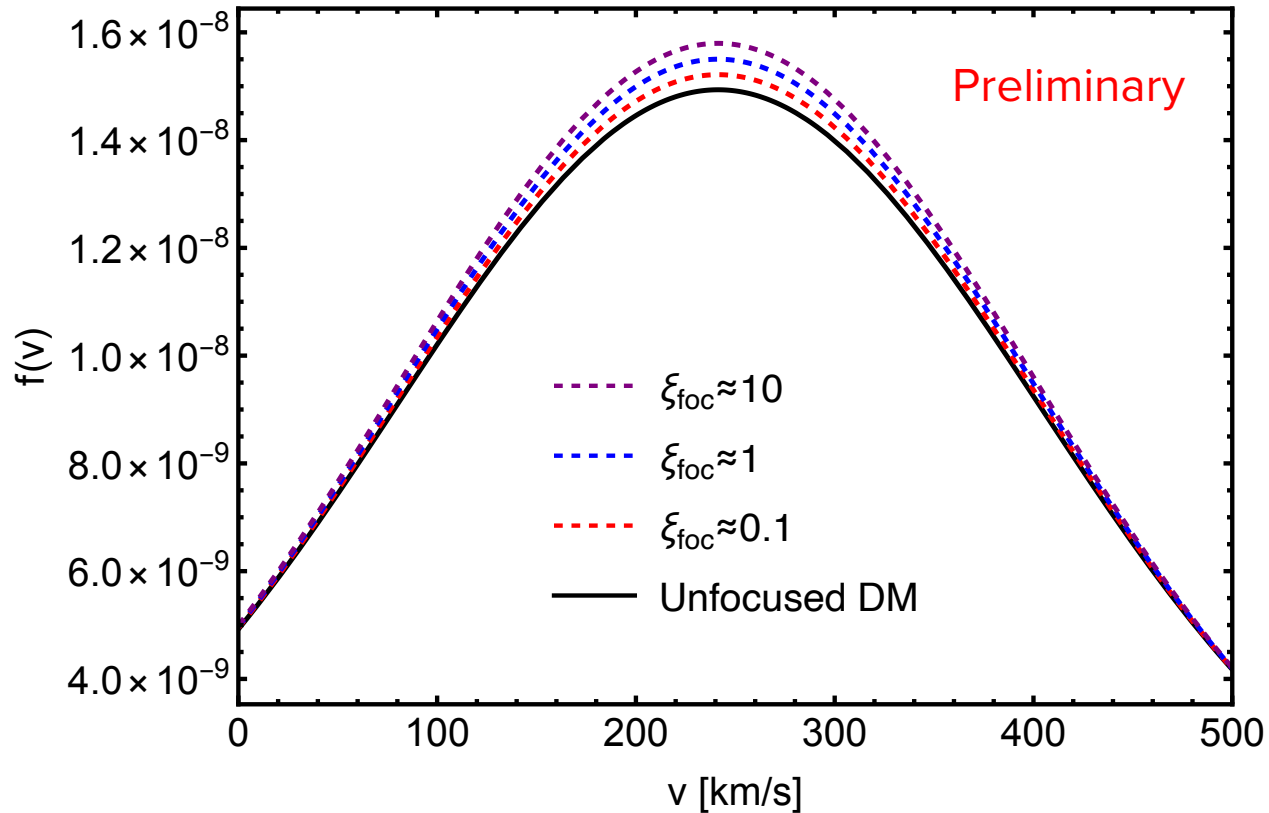
Bound (gravitational atoms)



Over-dense sub-halos form around the Sun and planets
potentially overlapping

Experimental signatures – coherence time

Unbound (gravitational focusing)



Bound (gravitational atoms)

In bound states, velocity becomes

$$v_b = \sqrt{\frac{GM_{\odot}}{R_*}}$$

Dispersion tends to zero,
coherence time tends to infinity

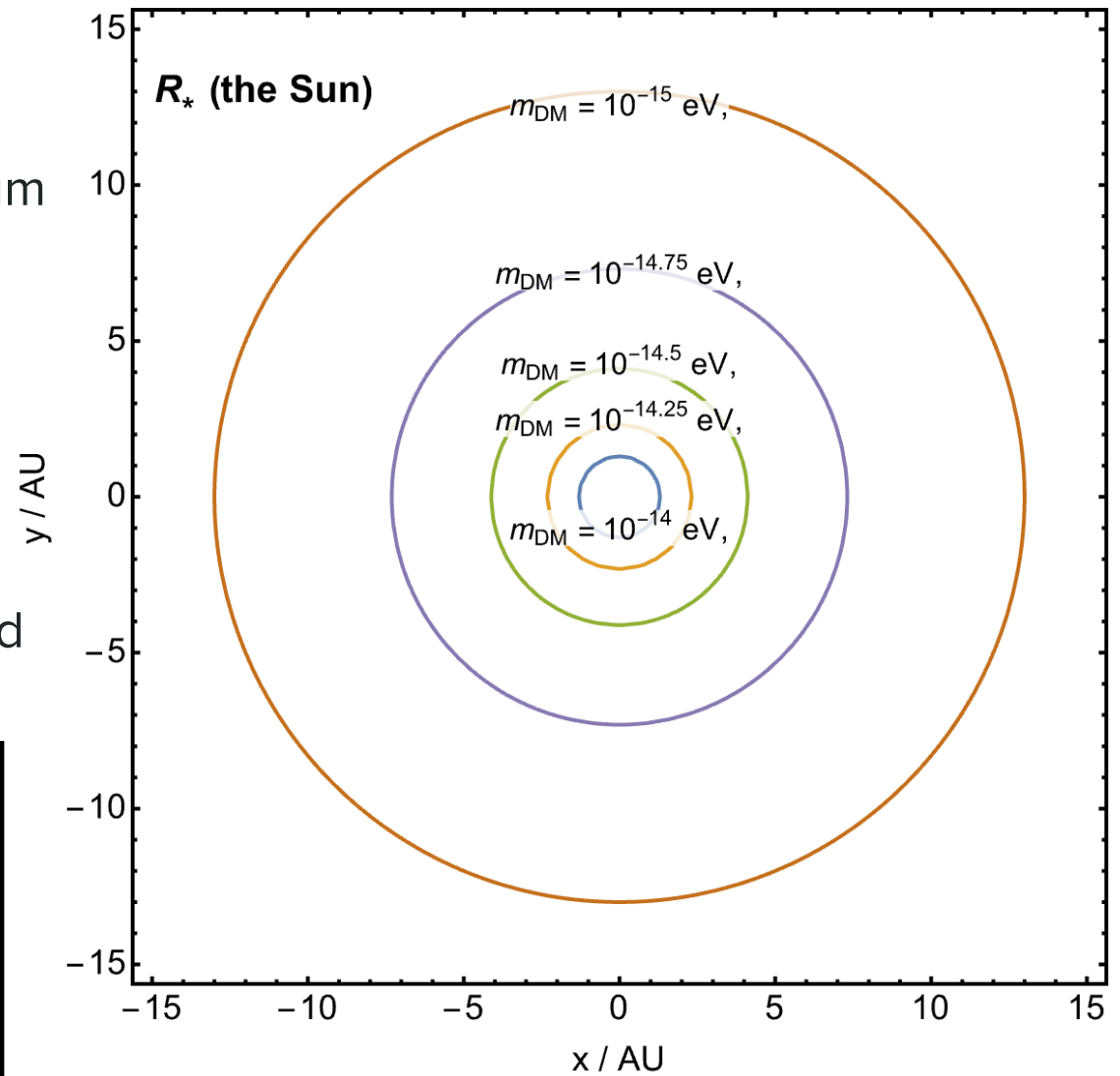
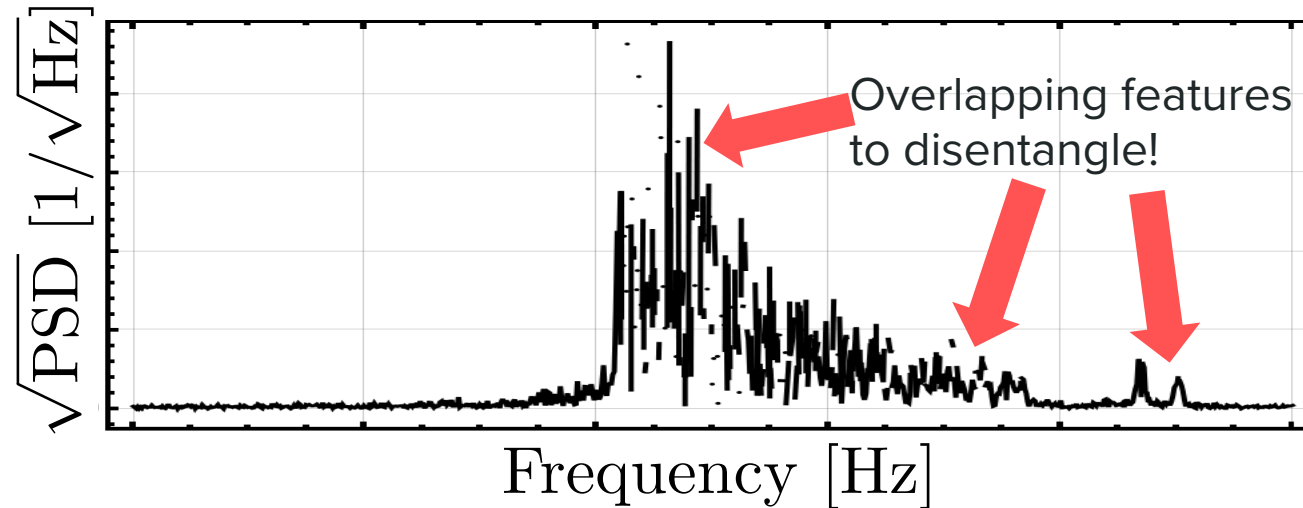
Velocity dispersion narrows, coherence time increases

Multi-axion halos and focusing

The **string axiverse** and other theories predict a spectrum of axion masses that could make up dark matter

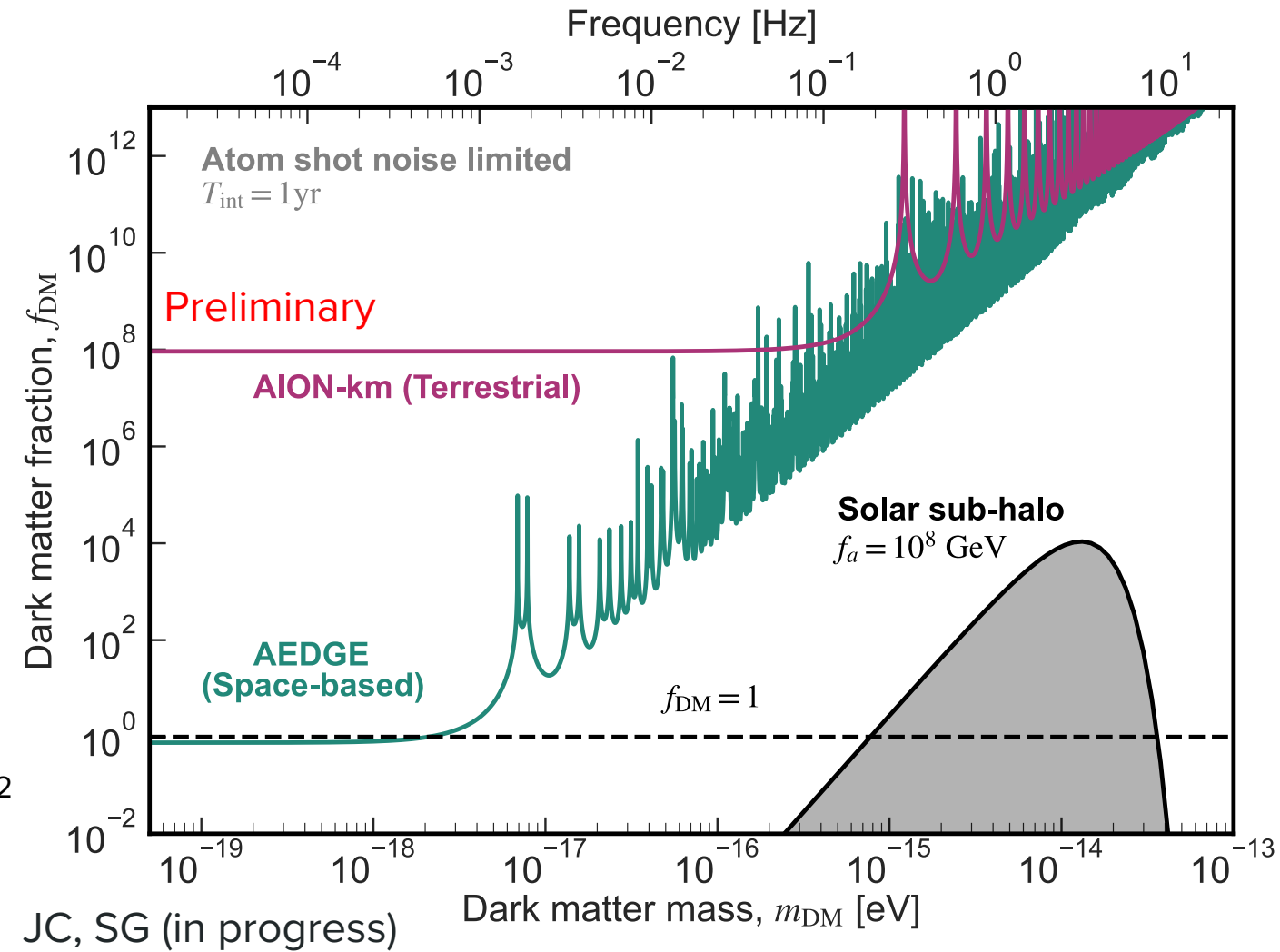
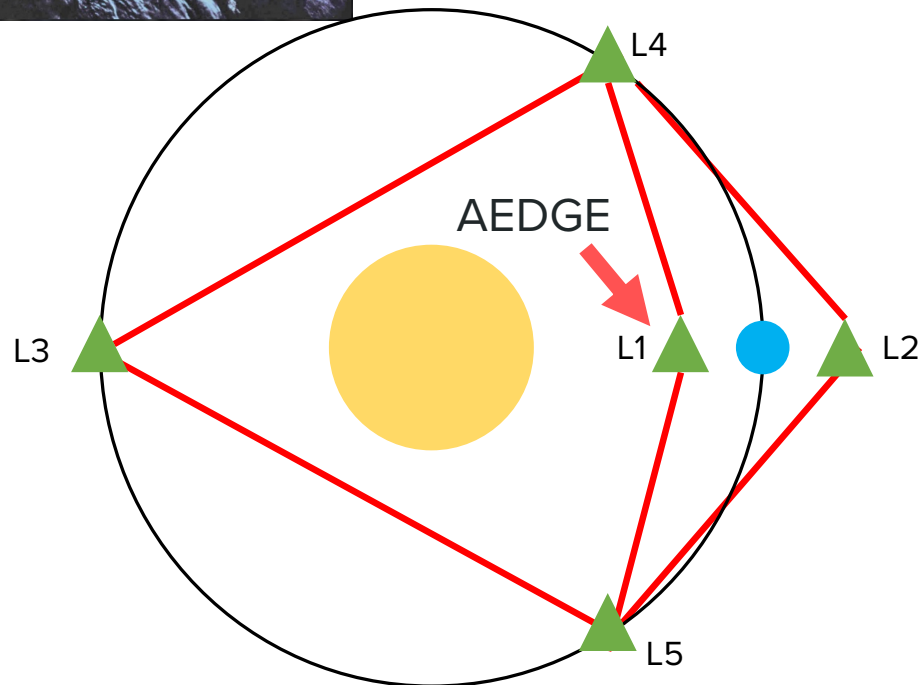
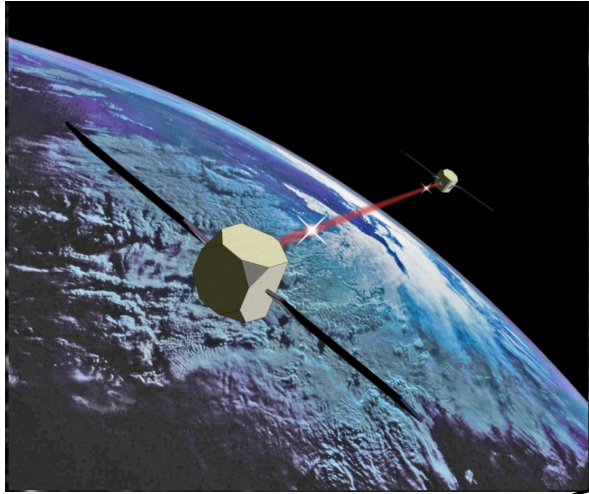
$$\rho_{\text{DM}} = \sum_i \rho_i = \sum_i \frac{1}{2} m_i^2 f_i^2 \theta_i^2$$

Each of these are a small subcomponent of the total dark matter, relaxing constraints on self-interactions and allowing many overlapping dense sub-halos to form!



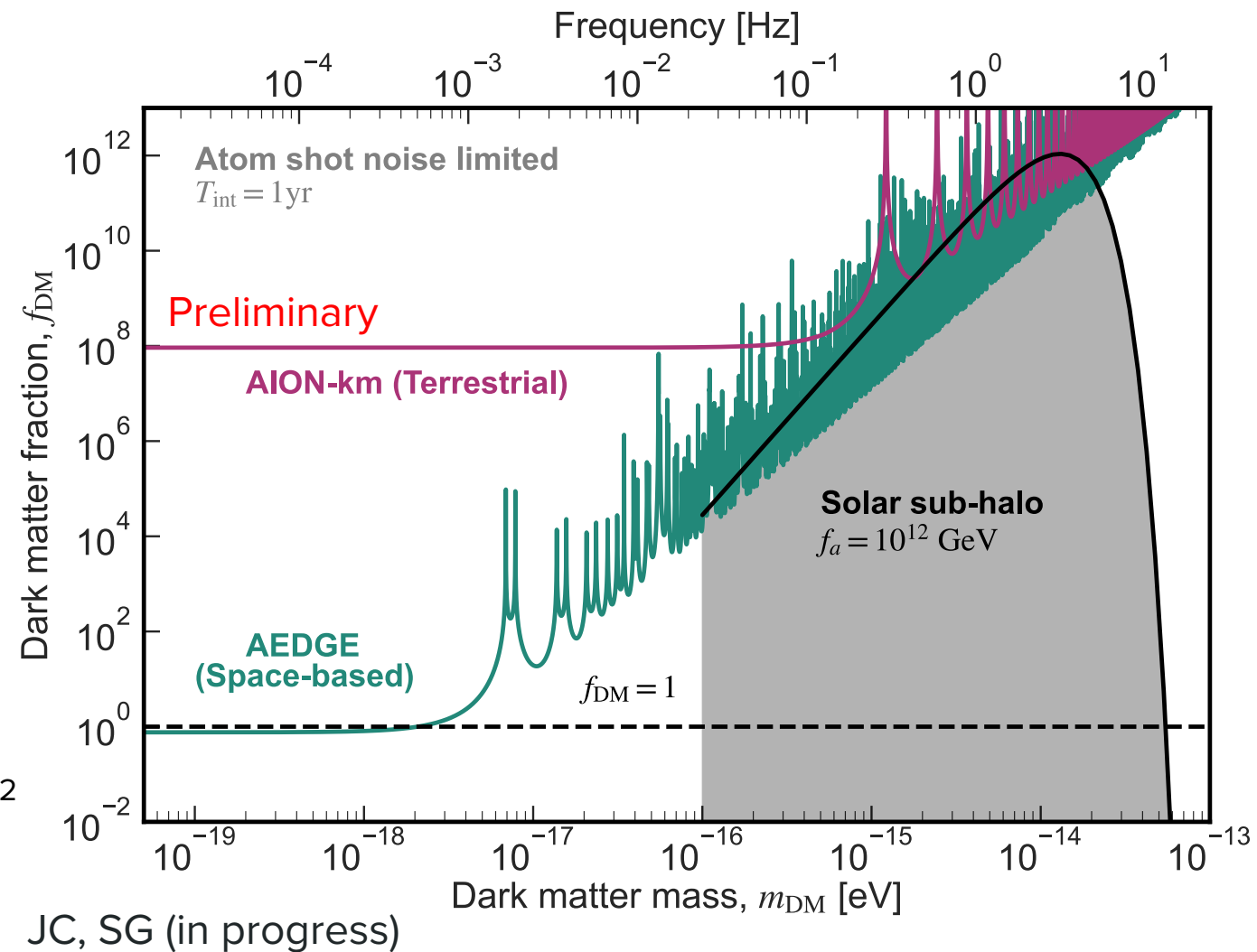
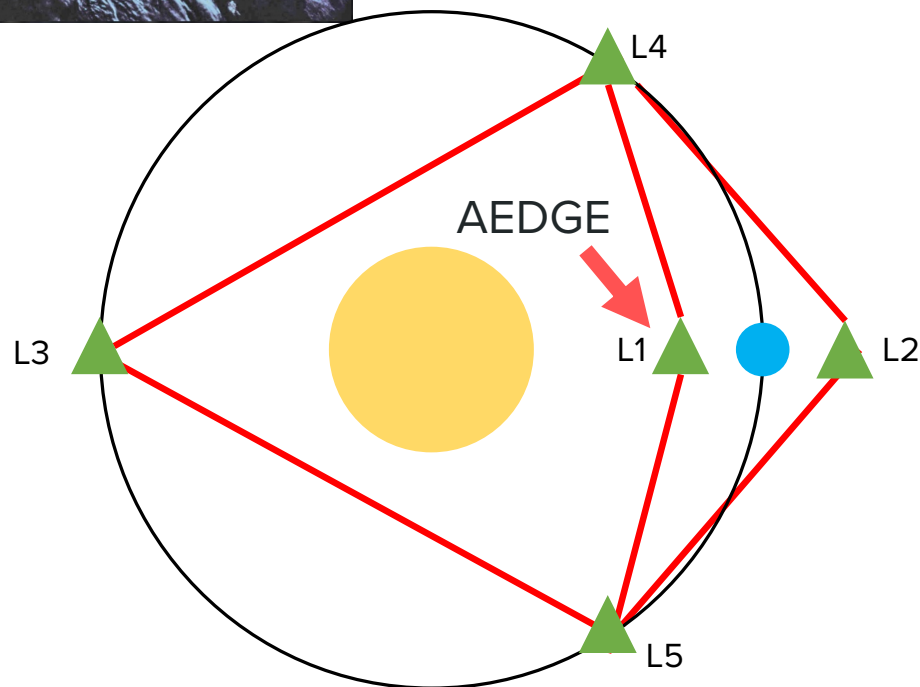
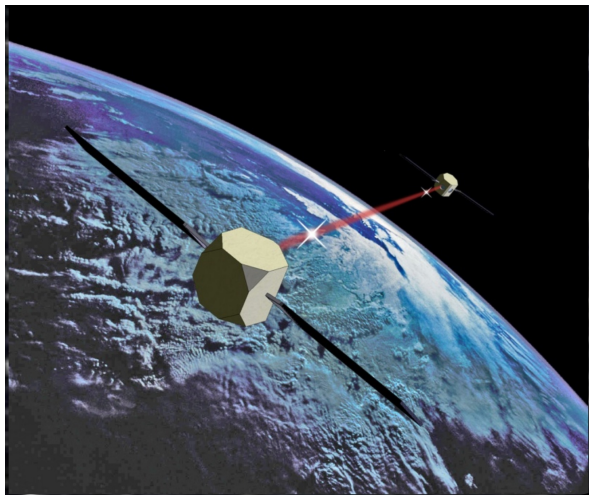
Solar system with many overlapping halos

Detection scenarios in space



Optimistic atom interferometry bounds

Detection scenarios in space



Optimistic atom interferometry bounds

Summary

Upcoming quantum sensor experiments have an increasingly rich phenomenology of candidates and signatures to explore!

Spin-2 ULDM is naturally probed by atom interferometers through several different channels! Other GW/ULDM experiments may also detect other couplings not probed by atom interferometers.

Generic features of ULDM in the solar system may lead to new search strategies and motivate space-based quantum sensors. Results are even more promising in multi-DM scenarios!

D. Blas, J. Carlton, C. McCabe. arXiv: 2412.14282

J. Carlton, S. Gardner. (In progress)

Back up

Interferometer sequence

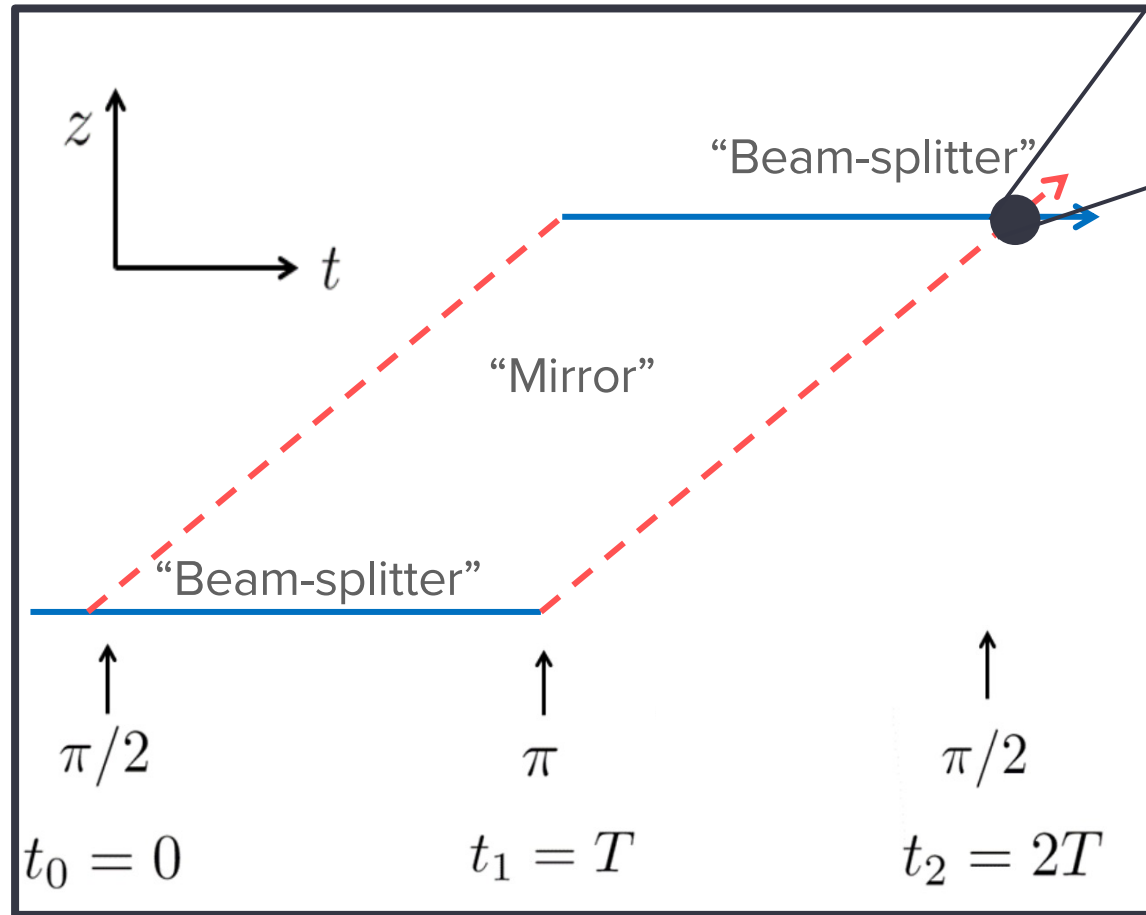


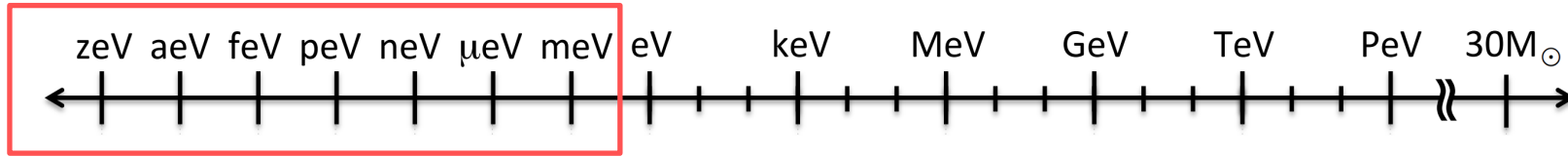
Image atom fringes
and measure phase

$$\phi_{\text{MZ}} = kgT^2$$

Leading order phase depends
on gravitational acceleration

Mach-Zehnder
interferometer

A classical ULDM field



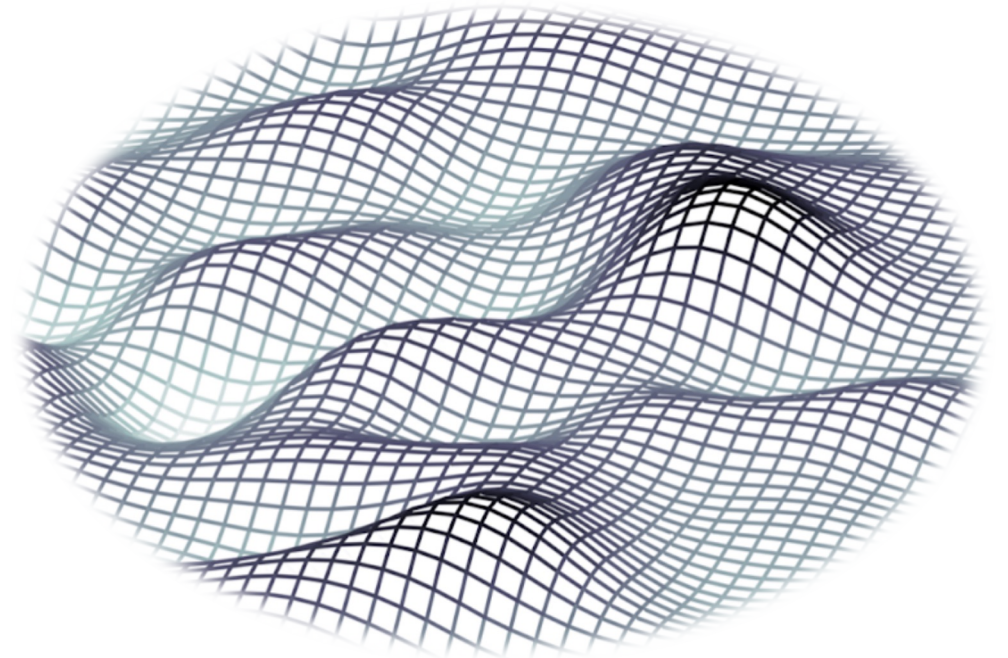
Ultralight mass means a high occupation number

Can describe as a classical field

$$\varphi(t, \mathbf{x}) \sim \cos(\omega_{\varphi} t - \mathbf{k}_{\varphi} \cdot \mathbf{x})$$

Frequency given by ULDM mass
(with small velocity correction)

$$\omega_{\varphi} \simeq m_{\varphi} \left(1 + \frac{v^2}{2} \right)$$



Atoms in a scalar ULDM field

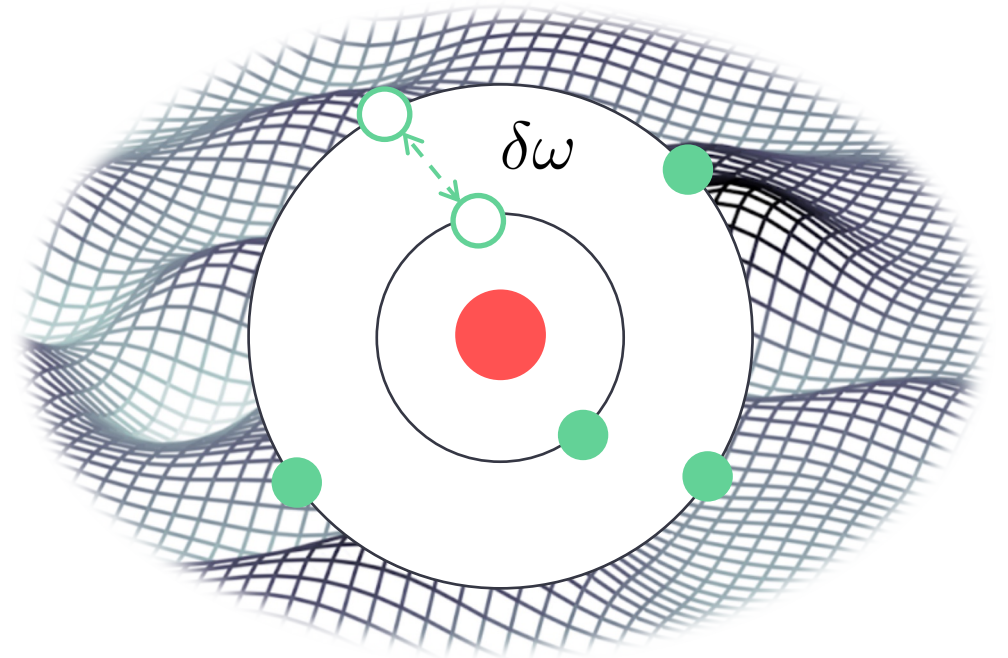
$$\mathcal{L} \supset \mathcal{L}_{\text{SM}} + \boxed{\mathcal{L}_\varphi} \longrightarrow \boxed{\mathcal{L}_\varphi \supset \varphi(t, \mathbf{x}) \sqrt{4\pi G_{\text{N}}} \left[\overset{\text{photon coupling}}{\frac{d_e}{4e^2} F_{\mu\nu} F^{\mu\nu}} - \overset{\text{electron coupling}}{d_{m_e} m_e \bar{\psi}_e \psi_e} \right]}$$

$$\alpha(t, \mathbf{x}) \approx \alpha \left[1 + d_e \sqrt{4\pi G_{\text{N}}} \varphi(t, \mathbf{x}) \right],$$

$$m_e(t, \mathbf{x}) = m_e \left[1 + d_{m_e} \sqrt{4\pi G_{\text{N}}} \varphi(t, \mathbf{x}) \right]$$

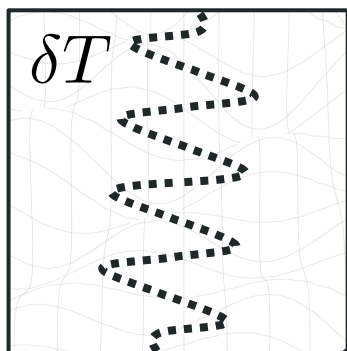
↓

$$\delta\phi \sim \delta\omega \sim \varphi(t, \mathbf{x})$$



Two sensitivity channels

Interrogation time (GWs)



Atomic transition frequency (Scalar ULDM)

